## Author's Reply to Discussion of A Prediction Technique for Immiscible Processes Using Field Performance Data

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Liu's proposed method of plotting  $N_p$  vs.  $\ln (N_p/W_p) - N_p/W_p$  to extrapolate cut vs. cumulative production plots is not based on a firm theoretical foundation. The main objective of the proposed method is to make long-range forecasts from very early performance data.

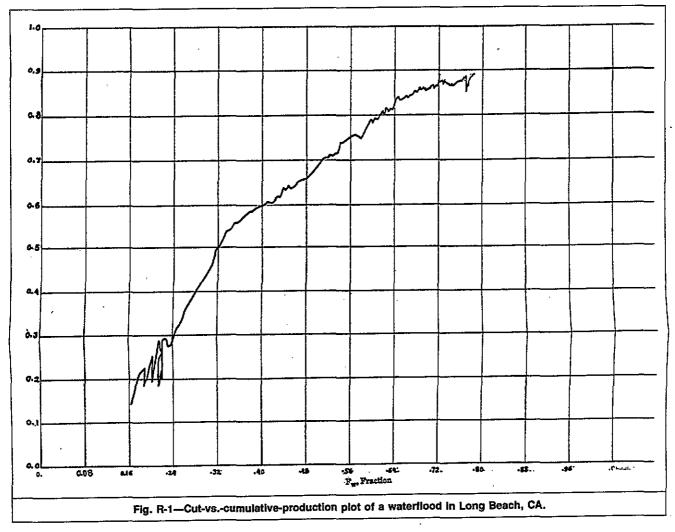
If the prediction technique is to rely on field permeability characteristics of a waterflood, then one must allow sufficient performance data to develop the appropriate trend. Field-based relative permeability characteristics of a waterflood implicitly include a measure of effective vertical and horizontal sweep efficiencies. These efficiencies cannot be reflected unless all producing layers have exhibited breakthrough. Low water cuts (below 50%) are indicative of breakthrough in subcomponents of a layered system. If one believes in the concept of frontal advance theory, then at breakthrough of all layers, water cut must be above 50% (above the point of inflection of a fractional-flow curve). Thus, applying any procedure to use water-cut data below 50% is to represent the behavior of the reservoir prematurely and can lead to erroneous projections.

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The formulation suggested by Liu uses  $E_R = mX + n$  as a starting point and substitutes cumulative water cut  $F_w = W_p/(N_p + W_p)$  for instantaneous water cut,  $f_w = W_p/(W_p - N_p)$ . This assumption is not valid because it requires a constant  $f_w$  throughout the life history. The relationship between  $F_w$  and  $f_w$  has a shape similar to that between cumulative recovery and  $f_w$ , as shown below:

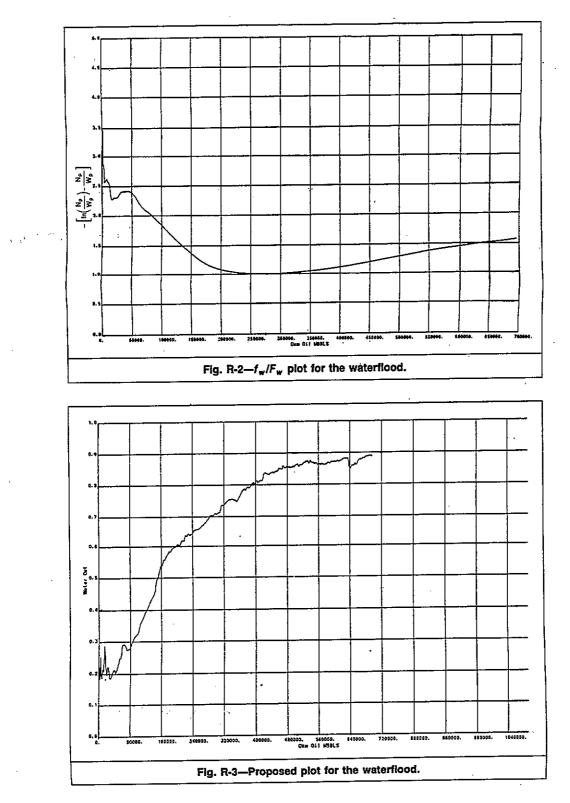
$$E_R = mX + b$$
,

 $N_p = NmX + bN$ ,



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 $F_w = 1 - (N_p/q_i \Delta t)$  (assuming constant injection rate), and  $F_w = \alpha X + \beta$ ,

where  $\alpha = -Nm/q_i \Delta t$  and  $\beta = -Nb/q_i \Delta t + 1$ .

A typical cut-vs.-cumulative-production plot for a mature waterflood is shown in Fig. R-1. Corresponding  $F_w$  vs.  $f_w$  is plotted in Fig. R-2. Note the nonlinearity of the plot. Also, the plot proposed by Liu is shown in Fig. R-3. There is a definite change in trend starting at cumulative oil production of  $32 \times 10^8$  bbl  $[5.1 \times 10^8 \text{ m}^3]$ corresponding to a cumulative cut of 50%. Extrapolation of early data would definitely have resulted in an erroneous projection. This can also be inferred from a plot of  $Z=\ln(N_p/W_p)-(N_p/W_p)$  vs.  $N_p$ , where the minimum point corresponding to  $dZ/dN_p=0$  occurs at  $N_p=W_p$  or  $F_w=0.5$ , which further delays the projection process.

## SI Metric Conversion Factor

bbl × 1.589 873

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 $E - 01 = m^3$