

NORME  
INTERNATIONALE  
INTERNATIONAL  
STANDARD

CEI  
IEC  
60193

Deuxième édition  
Second edition  
1999-11

---

---

Turbines hydrauliques, pompes d'accumulation  
et pompes-turbines –  
Essais de réception sur modèle

Hydraulic turbines, storage pumps  
and pump-turbines –  
Model acceptance tests

© IEC 1999 Droits de reproduction réservés — Copyright - all rights reserved

Aucune partie de cette publication ne peut être reproduite ni  
utilisée sous quelque forme que ce soit et par aucun procédé,  
électronique ou mécanique, y compris la photo-copie et les  
microfilms, sans l'accord écrit de l'éditeur.

No part of this publication may be reproduced or utilized in  
any form or by any means, electronic or mechanical,  
including photocopying and microfilm, without permission in  
writing from the publisher.

International Electrotechnical Commission 3, rue de Varembe Geneva, Switzerland  
Telefax: +41 22 919 0300 e-mail: [inmail@iec.ch](mailto:inmail@iec.ch) IEC web site <http://www.iec.ch>



Commission Electrotechnique Internationale  
International Electrotechnical Commission  
Международная Электротехническая Комиссия

CODE PRIX  
PRICE CODE XL

Pour prix, voir catalogue en vigueur  
For price, see current catalogue

## Éditions des publications

À partir du 1<sup>er</sup> janvier 1997, les publications de la CEI sont numérotées à partir de 60000.

## Éditions consolidées

Des versions consolidées de certaines publications de la CEI, incorporant les amendements sont disponibles. Par exemple, les numéros d'édition 1.0, 1.1 et 1.2 ont respectivement la publication de base, la publication de base incorporant l'amendement 1, et la publication de base incorporant les amendements 1 et 2.

## Validité de la présente publication

Le contenu technique des publications de la CEI est maintenu sous revue constante par la CEI afin qu'il reflète l'état de la technique.

Les informations relatives à la date de reconfirmation de la publication sont disponibles dans le catalogue de la CEI.

Des informations relatives à des questions à l'étude et aux travaux en cours entrepris par le comité technique ont été établies pour cette publication, ainsi que la liste des actions établies, se trouvent dans les documents ci-dessous :

« Site web » de la CEI\*

**Catalogue des publications de la CEI**  
Publié annuellement et mis à jour régulièrement  
(Catalogue en ligne)\*

**Bulletin de la CEI**

Disponible à la fois au « site web » de la CEI\* et comme périodique imprimé

## Terminologie, symboles graphiques et lettres

Quand il concerne la terminologie générale, le lecteur se référera à la CEI 60050: *Vocabulaire Electrotechnique International* (IEV).

Les symboles graphiques, les symboles littéraux, les signes d'usage général approuvés par la CEI, le lecteur consultera la CEI 60027: *Symboles littéraux à utiliser en électrotechnique*, la CEI 60417: *Symboles littéraux utilisables sur le matériel. Index, relevé et compilation des feuilles individuelles*, et la CEI 60617: *Symboles graphiques pour schémas*.

Le lecteur adresse « site web » sur la page de titre.

## Numbering

As from 1 January 1997 all IEC publications are issued with a designation in the 60000 series.

## Consolidated publications

Consolidated versions of some IEC publications including amendments are available. For example, edition numbers 1.0, 1.1 and 1.2 refer, respectively, to the base publication, the base publication incorporating amendment 1 and the base publication incorporating amendments 1 and 2.

## Validity of this publication

The technical content of IEC publications is kept under constant review by the IEC, thus ensuring that the content reflects current technology.

Information relating to the date of the reconfirmation of the publication is available in the IEC catalogue.

Information on the subjects under consideration and work in progress undertaken by the technical committee which has prepared this publication, as well as the list of publications issued, is to be found at the following IEC sources:

• IEC web site\*

• **Catalogue of IEC publications**  
Published yearly with regular updates  
(On-line catalogue)\*

• IEC Bulletin

Available both at the IEC web site\* and as a printed periodical

## Terminology, graphical and letter symbols

For general terminology, readers are referred to IEC 60050: *International Electrotechnical Vocabulary* (IEV).

For graphical symbols, and letter symbols and signs approved by the IEC for general use, readers are referred to publications IEC 60027: *Letter symbols to be used in electrical technology*, IEC 60417: *Graphical symbols for use on equipment. Index, survey and compilation of the single sheets* and IEC 60617: *Graphical symbols for diagrams*.

\* See web site address on title page.

# NORME INTERNATIONALE INTERNATIONAL STANDARD

CEI  
IEC

60193

Deuxième édition  
Second edition  
1999-11

Turbines hydrauliques, pompes d'accumulation  
et pompes-turbines –  
Essais de réception sur modèle

Hydraulic turbines, storage pumps  
and pump-turbines –  
Model acceptance tests



Numéro de référence  
Reference number  
CEI/IEC 60193:1999

## CONTENTS

	Page
FOREWORD .....	11
use	
General rules .....	13
1.1 Scope and object .....	13
1.1.1 Scope .....	13
1.1.2 Object .....	13
1.2 Normative references .....	15
1.3 Terms, definitions, symbols and units .....	17
1.3.1 General .....	17
1.3.2 Units .....	19
1.3.3 List of terms, definitions, symbols and units .....	21
1.4 Nature and extent of guarantees related to hydraulic performance .....	59
1.4.1 General .....	59
1.4.2 Main hydraulic performance guarantees verifiable by model test .....	61
1.4.3 Guarantees not verifiable by model test .....	67
1.4.4 Additional performance data .....	67
Execution of tests .....	69
2.1 Requirements of test installation and model .....	69
2.1.1 Choice of laboratory .....	69
2.1.2 Test installation .....	69
2.1.3 Model requirements .....	71
2.2 Dimensional check of model and prototype .....	75
2.2.1 General .....	75
2.2.2 Dimensions of model and prototype to be checked .....	95
2.2.3 Surface waviness and roughness .....	111
2.3 Hydraulic similitude, test conditions and test procedures .....	119
2.3.1 Hydraulic similitude .....	119
2.3.2 Test conditions .....	133
2.3.3 Test procedures .....	139
2.4 Introduction to the methods of measurement .....	161
2.4.1 Measurements related to the main hydraulic performance guarantees .....	161
2.4.2 Measurements related to additional data .....	165
2.4.3 Acquisition and processing of data .....	165
2.5 Physical properties .....	165
2.5.1 General .....	165
2.5.2 Acceleration due to gravity .....	165
2.5.3 Physical properties of water .....	167
2.5.4 Physical conditions of atmosphere .....	177
2.5.5 Density of mercury .....	179

Clause	Page
3 Main hydraulic performances: methods of measurement and results .....	181
3.1 Data acquisition and data processing .....	181
3.1.1 Introduction and definitions .....	181
3.1.2 General requirements .....	181
3.1.3 Data acquisition .....	185
3.1.4 Component requirements .....	187
3.1.5 Check of the data acquisition system .....	193
3.2 Discharge measurement .....	197
3.2.1 General .....	197
3.2.2 Primary methods .....	201
3.2.3 Secondary methods .....	209
3.3 Pressure measurement .....	215
3.3.1 General .....	215
3.3.2 Choice of pressure-measuring section .....	215
3.3.3 Pressure taps and connecting lines .....	217
3.3.4 Apparatus for pressure measurement .....	223
3.3.5 Calibration of pressure measurement apparatus .....	237
3.3.6 Vacuum measurements .....	237
3.3.7 Uncertainty in pressure measurements .....	239
3.4 Free water level measurement .....	239
3.4.1 General .....	239
3.4.2 Choice of water level measuring sections .....	239
3.4.3 Number of measuring points in a measuring section .....	239
3.4.4 Measuring apparatus .....	241
3.4.5 Uncertainty in free water level measurement .....	245
3.5 Determination of E and NPSE .....	245
3.5.1 General .....	245
3.5.2 Determination of the specific hydraulic energy E .....	247
3.5.3 Simplified formulae for E .....	251
3.5.4 Determination of the net positive suction specific energy NPSE .....	261
3.6 Shaft torque measurement .....	271
3.6.1 General .....	271
3.6.2 Methods of torque measurement .....	271
3.6.3 Methods of absorbing/generating power .....	273
3.6.4 Layout of arrangement .....	273
3.6.5 Checking of system .....	283
3.6.6 Calibration .....	283
3.6.7 Uncertainty in torque measurement .....	285
3.7 Rotational speed measurement .....	287
3.7.1 General .....	287
3.7.2 Methods of speed measurement .....	287
3.7.3 Checking .....	287
3.7.4 Uncertainty of measurement .....	289

Clause	Page
3.8 Computation of test results.....	289
3.8.1 General.....	289
3.8.2 Computation of power, discharge and efficiency in the guarantee range.....	299
3.8.3 Computation of steady-state runaway speed and discharge.....	329
3.9 Error analysis.....	337
3.9.1 Basic principles (see ISO 5168).....	337
3.9.2 Determination of uncertainties in model tests.....	341
3.10 Comparison with guarantees.....	351
3.10.1 General.....	351
3.10.2 Interpolation curve and total uncertainty bandwidth.....	353
3.10.3 Power, discharge and/or specific hydraulic energy and efficiency in the guarantee range.....	355
3.10.4 Runaway speed and discharge.....	363
3.10.5 Cavitation guarantees.....	363
Additional performance data – Methods of measurement and results.....	367
4.1 Introduction to additional data measurement.....	367
4.1.1 General.....	367
4.1.2 Test conditions and test procedures.....	369
4.1.3 Uncertainty in measurements.....	369
4.1.4 Model to prototype conversion.....	369
4.2 Data acquisition and processing for measurement of fluctuating quantities.....	371
4.2.1 General.....	371
4.2.2 Data acquisition.....	373
4.2.3 Data processing.....	377
4.3 Pressure fluctuations.....	379
4.3.1 General.....	379
4.3.2 Special requirements for model and installation.....	387
4.3.3 Instrumentation and calibration.....	389
4.3.4 Detailed procedures.....	391
4.3.5 Measurement.....	397
4.3.6 Analysis, presentation and interpretation of results.....	397
4.3.7 Transposition to prototype.....	403
4.3.8 Uncertainties.....	409
4.4 Shaft torque fluctuations.....	411
4.4.1 General.....	411
4.4.2 Recommendations for measurement.....	411
4.4.3 Analysis of model test results.....	411
4.4.4 Transposition to prototype.....	411
4.5 Axial and radial thrust.....	413
4.5.1 General.....	413
4.5.2 Axial thrust.....	415
4.5.3 Radial thrust.....	425

Clause	Page
4.6 Hydraulic loads on control components.....	431
4.6.1 General.....	431
4.6.2 Guide vane torque.....	433
4.6.3 Runner blade torque.....	443
4.6.4 Pelton needle force and deflector torque.....	453
4.7 Testing in an extended operating range.....	459
4.7.1 General.....	459
4.7.2 Terminology.....	459
4.7.3 Scope of tests.....	465
4.7.4 Provisions for particular tests.....	467
4.8 Differential pressure measurement in view of prototype index test.....	471
4.8.1 General.....	471
4.8.2 Purpose of test.....	473
4.8.3 Execution of test.....	473
4.8.4 Transposition to prototype conditions.....	475
4.8.5 Uncertainty.....	475
Annex A (informative) Dimensionless terms.....	477
Annex B (normative) Physical properties, data.....	479
Annex C (informative) Derivation of the equation for the specific hydraulic energy of a machine.....	495
Annex D (informative) Influence of the density of actual water $\rho_{wa}$ on measurement and calibration.....	499
Annex E (informative) Summarized test and calculation procedure.....	501
Annex F (normative) Scale-up of the hydraulic efficiency of reaction machines.....	509
Annex G (normative) Computation of the prototype runaway characteristics taking into account friction and windage losses of the unit.....	519
Annex H (informative) Example of determination of the best smooth curve: method of separate segments.....	521
Annex J (informative) Examples analysis of sources of error and uncertainty evaluation.....	527
Annex K (normative) Efficiency scale-up for Pelton turbines.....	539
Annex L (normative) Analysis of random uncertainties for a test at constant operating conditions.....	545
Annex M (normative) Calculation of plant Thoma number $\sigma_{pl}$ .....	553
Annex N (informative) Detailed flux diagram of specific hydraulic energy, flow and power.....	561
Annex P (informative) Bibliography.....	567

## INTERNATIONAL ELECTROTECHNICAL COMMISSION

# HYDRAULIC TURBINES, STORAGE PUMPS AND PUMP-TURBINES – MODEL ACCEPTANCE TESTS

## FOREWORD

The IEC (International Electrotechnical Commission) is a worldwide organization for standardization comprising all national electrotechnical committees (IEC National Committees). The object of the IEC is to promote international co-operation on all questions concerning standardization in the electrical and electronic fields. To this end and in addition to other activities, the IEC publishes International Standards. Their preparation is entrusted to technical committees; any IEC National Committee interested in the subject dealt with may participate in this preparatory work. International, governmental and non-governmental organizations liaising with the IEC also participate in this preparation. The IEC collaborates closely with the International Organization for Standardization (ISO) in accordance with conditions determined by agreement between the two organizations.

The formal decisions or agreements of the IEC on technical matters express, as nearly as possible, an international consensus of opinion on the relevant subjects since each technical committee has representation from all interested National Committees.

The documents produced have the form of recommendations for international use and are published in the form of standards, technical reports or guides and they are accepted by the National Committees in that sense.

In order to promote international unification, IEC National Committees undertake to apply IEC International Standards transparently to the maximum extent possible in their national and regional standards. Any divergence between the IEC Standard and the corresponding national or regional standard shall be clearly indicated in the latter.

The IEC provides no marking procedure to indicate its approval and cannot be rendered responsible for any equipment declared to be in conformity with one of its standards.

Attention is drawn to the possibility that some of the elements of this International Standard may be the subject of patent rights. The IEC shall not be held responsible for identifying any or all such patent rights.

International Standard IEC 60193 has been prepared by IEC technical committee 4: Hydraulic turbines.

This second edition of IEC 60193 cancels and replaces the first edition of IEC 60193 published in 1965, its amendment 1 (1977), IEC 60193A (1972), as well as IEC 60497 (1976) and IEC 60995 (1991).

Clauses 1 to 3 of this standard cover the scopes dealt with in the above-mentioned publications. Additional information is given in clause 4.

The text of this standard is based on the following documents:

FDIS	Report on voting
4/157/FDIS	4/162/RVD

All information on the voting for the approval of this standard can be found in the report on voting indicated in the above table.

Annexes B, F, G, K, L and M form an integral part of this standard.

Annexes A, C, D, E, H, J, N and P are for information only.

The committee has decided that this publication remains valid until 2004. At this date, in accordance with the committee's decision, the publication will be

reconfirmed;

withdrawn;

replaced by a revised edition, or

amended.

# HYDRAULIC TURBINES, STORAGE PUMPS AND PUMP-TURBINES – MODEL ACCEPTANCE TESTS

## 1 General rules

## 1.1 Scope and object

## 1.1.1 Scope

This International Standard applies to laboratory models of any type of impulse or reaction hydraulic turbine, storage pump or pump-turbine.

This standard applies to models of prototype machines either with unit power greater than 5 MW or with reference diameter greater than 3 m. Full application of the procedures herein prescribed is not generally justified for machines with smaller power and size. Nevertheless, this standard may be used for such machines by agreement between purchaser and supplier.

In this standard, the term "turbine" includes a pump-turbine operating as a turbine and the term "pump" includes a pump-turbine operating as a pump.

This standard excludes all matters of purely commercial interest, except those inextricably bound up with the conduct of the tests.

This standard is concerned with neither the structural details of the machines nor the mechanical properties of their components, so long as these do not affect model performance or the relationship between model and prototype performances.

## 1.1.2 Object

This International Standard covers the arrangements for model acceptance tests to be performed on hydraulic turbines, storage pumps and pump-turbines to determine if the main hydraulic performance contract guarantees (see 1.4.2) have been satisfied.

It contains the rules governing test conduct and prescribes measures to be taken if any phase of the tests is disputed.

The main objectives of this standard are:

- to define the terms and quantities used;
- to specify methods of testing and of measuring the quantities involved, in order to ascertain the hydraulic performance of the model;
- to specify the methods of computation of results and of comparison with guarantees;
- to determine if the contract guarantees, which fall within the scope of this standard, have been fulfilled;
- to define the extent, content and structure of the final report.

The guarantees can be given in one of the following ways:

- guarantees for prototype hydraulic performance, computed from model test results considering scale effects;
- guarantees for model hydraulic performance.

ever additional performance data (see 1.4.4) can be needed for the design or the ration of the prototype of the hydraulic machine. Contrary to the requirements of clauses 1 related to main hydraulic performance the information of these additional data given in use 4 is considered only as recommendation or guidance to the user (see 4.1).

particularly recommended that model acceptance tests be performed if the expected field ditions for acceptance tests (see IEC 60041) would not allow the verification of guarantees in for the prototype machine.

standard may also be applied to model tests for other purposes, i.e. comparative tests and arch and development work.

odel acceptance tests have been performed, field tests can be limited to index tests (see 60041, clause 15).

contradiction is found between this standard and any other standard, this standard shall ail.

#### Normative references

Following nonnormative documents contain provisions which, through reference in this text, stitute provisions of this International Standard. At the time of publication, the editions cated were valid. All normative documents are subject to revision, and parties to eements based on this International Standard are encouraged to investigate the possibility applying the most recent editions of the normative documents indicated below. Members of ; and ISO maintain registers of currently valid International Standards.

60041:1991, *Field acceptance test to determine the hydraulic performance of hydraulic bines, storage pumps and pump-turbines*

60609:1978, *Cavitation pitting evaluation in hydraulic turbines, storage pumps and pump-bines*

60609-2:1997, *Cavitation pitting evaluation in hydraulic turbines, storage pumps and mp-turbines – Part 2: Evaluation in Pelton turbines*

60994:1991, *Guide for field measurement of vibrations and pulsations in hydraulic chines (turbines, storage pumps and pump-turbines)*

61364:1999, *Nomenclature of hydraulic machinery*

61366 (all parts), *Hydraulic turbines storage pumps and pump-turbines – Tendering cuments*

31-3:1992, *Quantities and units – Part 3: Mechanics*

31-12:1992, *Quantities and units – Part 12: Characteristic numbers*

468:1982, *Surface roughness – Parameters, their values and general rules for specifying quirements*

1438-1:1980, *Water flow measurement in open channels using weirs and Venturi flumes – art 1: Thin-plate weirs*

ISO 2186:1973, *Fluid flow in closed conduits – Connections for pressure signal transmissions between primary and secondary elements*

ISO 2533:1975, *Standard atmosphere*  
Addendum 1: 1985

ISO 4006:1991, *Measurement of fluid flow in closed conduits – Vocabulary and symbols*

ISO 4185:1980, *Measurement of liquid flow in closed conduits – Weighing method*

ISO 4373:1995, *Measurement of liquid flow in open channels – Water level measuring devices*

ISO 5167-1:1991, *Measurement of fluid flow by means of pressure differential devices – Part 1: Orifice plates, nozzles and Venturi tubes inserted in circular cross-section conduits running full*

ISO 5168:1978, *Measurement of fluid flow – Estimation of uncertainty of a flow-rate measurement*

ISO 6817:1992, *Measurement of conductive liquid flow in closed conduits – Method using electromagnetic flowmeters*

ISO 7066-1:1997, *Assessment of uncertainty in the calibration and use of flow measurement devices – Part 1: Linear calibration relationship*

ISO 7066-2:1988, *Assessment of uncertainty in the calibration and use of flow measurement devices – Part 2: Non-linear calibration relationships*

ISO 8316: 1987, *Measurement of liquid flow in closed conduits – Method by collection of the liquid in a volumetric tank*

ISO 9104:1991, *Measurement of fluid flow in closed conduits – Methods of evaluating the performance of electromagnetic flow-meters for liquids*

VIM:1993, *International vocabulary of basic and general terms in metrology (BIPM-IEC-ISO-OIML)*

### 1.3 Terms, definitions, symbols and units

#### 1.3.1 General

For the purpose of this International Standard the following common terms, definitions, symbo's and units apply. Specialized terms are explained where they appear.

Clarification of any term, definition or unit of measure in question shall be agreed to in writing by the contracting parties in advance of the test.

##### 1.3.1.1 point

A *point* is established by one or more consecutive sets of readings and/or recordings at unchanged operating condition and settings, sufficient to calculate the performance of the machine at this operating condition and these settings

##### 1.3.1.2 test

a *test* comprises a collection of points and results adequate to establish the performance of the machine over a specified range of operating conditions

### 1.3 hydraulic performance

performance parameters attributable to the machine due to hydrodynamic effects

#### 1.4 main hydraulic performance data

subset of the hydraulic performance parameters, i.e. power, discharge and/or specific hydraulic energy, efficiency, steady-state runaway speed and/or discharge. The influence of cavitation must be considered.

#### 1.5 additional data

subset of hydraulic performance data which can be determined for information on the model (see 1.4.4). However, the prediction of the corresponding prototype data is less accurate than that achievable for the main hydraulic performance data, due to application of approximate similarity rules.

#### 1.6 guarantees

specified performance data contractually agreed to

### 2 Units

The International System of Units (SI, see ISO 31-3) has been used throughout this standard.

Terms are given in SI base units or derived coherent units<sup>1)</sup>. The basic equations are valid using these units. This has to be taken into account if other than coherent SI units are used for test data (e.g. kilowatt instead of watt for power, kilopascal or bar instead of pascal for pressure, min<sup>-1</sup> instead of s<sup>-1</sup> for rotational speed, etc.). Temperatures may be given in degrees Celsius since absolute temperatures (in kelvins) are rarely required.

Any other system of units may be used but only if agreed in writing by the contracting parties.

<sup>1)</sup> N = kg·m·s<sup>-2</sup> Pa = kg·m<sup>-1</sup>·s<sup>-2</sup> J = kg·m<sup>2</sup>·s<sup>-2</sup> W = kg·m<sup>2</sup>·s<sup>-3</sup>

### 1.3.3 List of terms, definitions, symbols and units

#### 1.3.3.1 Subscripts and symbols

Subclause	Term	Definition	Subscript or symbol
1.3.3.1.1	High pressure <sup>1)</sup> reference section	The high pressure section of the machine to which the performance guarantees refer (see figure 1)	1
1.3.3.1.2	Low pressure <sup>1)</sup> reference section	The low pressure section of the machine to which the performance guarantees refer (see figure 1)	2
1.3.3.1.3	High pressure measuring sections	Whenever possible, these sections should coincide with section 1; otherwise the measured values must be adjusted to section 1 (see 3.5.2.1.3)	1', 1" ..
1.3.3.1.4	Low pressure measuring sections	Whenever possible, these sections should coincide with section 2; otherwise the measured values must be adjusted to section 2 (see 3.5.2.1.3)	2', 2" ..
1.3.3.1.5	Specified	Subscript denoting values of quantities such as rotational speed, discharge etc. for which other quantities are guaranteed	sp
1.3.3.1.6	Maximum/minimum	Subscript denoting maximum or minimum values of any term	max min
1.3.3.1.7	Limits	Contractually defined values: – not to be exceeded – to be reached	$\overline{\quad}$ □ or $\overline{\quad}$
1.3.3.1.8	Prototype	Subscript denoting values related to the full size machine	P
1.3.3.1.9	Model	Subscript denoting values related to the model	M
1.3.3.1.10	Model at constant Reynolds number	Subscript denoting values related to a model and referred to a constant value of Reynolds number	M*
1.3.3.1.11	Reference	Subscript denoting values related to a specified reference condition	ref
1.3.3.1.12	Optimum	Subscript denoting the best efficiency point	opt
1.3.3.1.13	Ambient	Subscript referring to surrounding atmospheric conditions	amb
1.3.3.1.14	Plant	Subscript denoting values related to the operating conditions of the prototype in the plant	pl
1.3.3.1.15	Runaway	Subscript referring to runaway conditions	R

<sup>1)</sup> The terms "high pressure" and "low pressure" define the two sides of the machine irrespective of the flow direction and therefore are independent of the mode of operation of the machine.

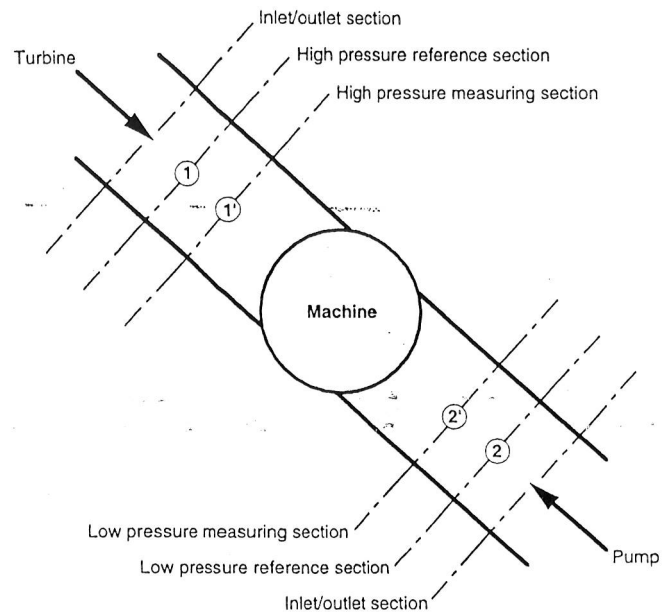
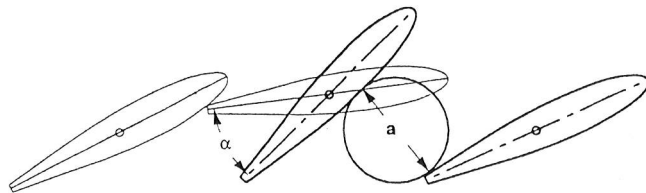


Figure 1 – Schematic representation of a hydraulic machine

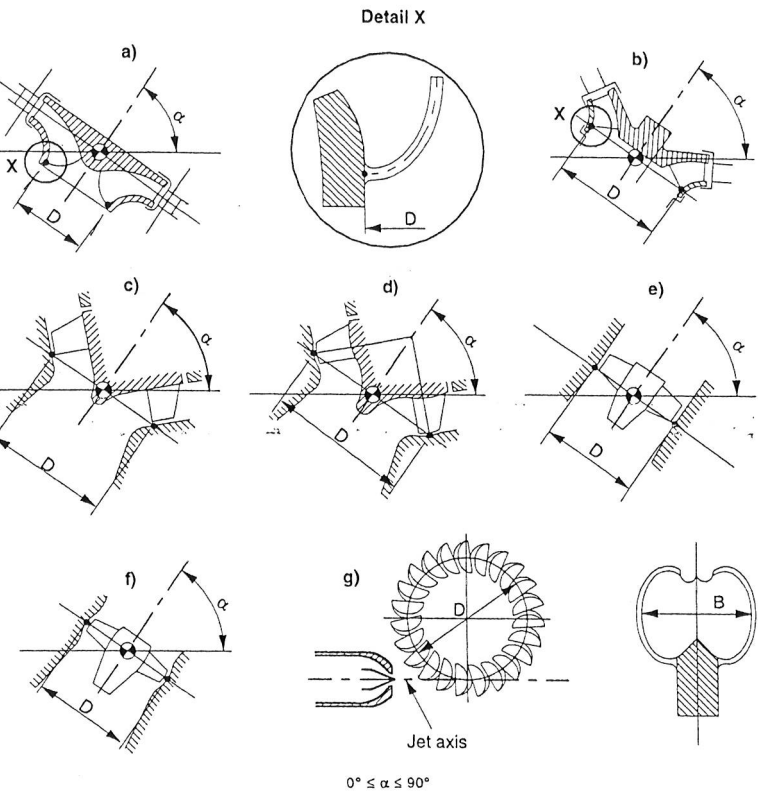


Closed position:  $\alpha = 0^\circ$  or  $a = 0 \text{ mm}$

Figure 2 – Guide vane opening and angle

## 1.3.3.2 Geometric terms

Subclause	Term	Definition	Symbol	Unit
1.3.3.2.1	Area	Net cross sectional area normal to general flow direction	A	m <sup>2</sup>
1.3.3.2.2	Guide vane opening	Average shortest distance between adjacent guide vanes (at a specified section if necessary) (see figure 2)	a	m
1.3.3.2.3	Guide vane angle	Average vane angle measured from closed position (see figure 2)	$\alpha$	°
1.3.3.2.4	Needle stroke (impulse turbine)	Average needle stroke measured from closed position	s	m
1.3.3.2.5	Runner/impeller blade angle	Average runner/impeller blade setting measured from a reference position	$\beta$	°
1.3.3.2.6	Reference diameter	Reference diameter of the hydraulic machine as given in figure 3	D	m
1.3.3.2.7	Runner outlet/impeller inlet width	Average shortest distance between two adjacent blades of runner/impeller (see figures 14 and 15)	$a_1, a_2$	m
1.3.3.2.8	Bucket width	Inside maximum width of runner bucket of a Pelton turbine (see figure 3)	B	m
1.3.3.2.9	Length scale ratio	The ratio of representative prototype to model lengths; in normal cases this is the reference diameter of the machine. In cases where it is difficult to verify this reference, then another significant length may be taken	$\lambda_L$	
1.3.3.2.10	Level	Elevation of a point in the system above the specified reference datum (usually mean sea level)	z	m



Radial machines, such as Francis turbines, radial (centrifugal) pumps and pump-turbines; for multistage machines: low-pressure stage.

Diagonal (mixed-flow, semi-axial) machines with fixed runner/impeller blades and with runner/impeller band.

Diagonal (mixed-flow, semi-axial) machines with fixed runner/impeller blades, without runner/impeller band.

Diagonal (mixed-flow, semi-axial) machines with adjustable runner/impeller blades.

Axial machines, such as propeller turbines, tubular turbines<sup>1)</sup>, axial pumps and pump-turbines with fixed runner/impeller blades.

Axial machines, such as Kaplan turbines, tubular turbines<sup>1)</sup>, axial pumps and pump-turbines with adjustable runner/impeller blades.

Pelton turbines.

Figure 3 – Reference diameter and bucket width

<sup>1)</sup>The term "tubular turbines" includes bulb, pit, rim generator and S-type units.

1.3.3.3 Physical quantities and properties

Subclause	Term	Definition	Symbol	Unit
1.3.3.3.1	Acceleration due to gravity	Local value of gravitational acceleration at the place of testing (see 2.5.2); theoretical values as a function of altitude and latitude are given in annex B, table B.1	$g$	$\text{m s}^{-2}$
1.3.3.3.2	Temperature	Thermodynamic Celsius $\theta = \Theta - 273,15$	$\Theta$ $\theta$	K °C
1.3.3.3.3	Density	Mass per unit volume a) Density of water $\rho$ is commonly used instead of $\rho_w$ . Values for distilled water $\rho_{wg}$ are given in 2.5.3.1.3 and in annex B, table B.2 b) Density of air Values for air are given in 2.5.4.1 and in annex B, table B.5 c) Density of mercury Values for mercury are given in 2.5.5 and in annex B, table B.7	$\rho$ $\rho_w$  $\rho_a$  $\rho_{Hg}$	$\text{kg m}^{-3}$ $\text{kg m}^{-3}$  $\text{kg m}^{-3}$  $\text{kg m}^{-3}$
1.3.3.3.4	Vapour pressure (absolute)	Absolute partial pressure of saturated vapour in a medium where liquid and gaseous phases of a body are in thermodynamic balance. The vapour pressure depends only on the temperature. Values for distilled water are given in 2.5.3.4 and in annex B, table B.4	$p_{va}$	Pa
1.3.3.3.5	Dynamic viscosity	A quantity characterizing the mechanical behaviour of a fluid (see ISO 31-3)	$\mu$	Pa s
1.3.3.3.6	Kinematic viscosity	Ratio of the dynamic viscosity to the density of a fluid. Values for distilled water as a function of temperature are given in 2.5.3.3 and in annex B, table B.3	$\nu$	$\text{m}^2 \text{s}^{-1}$
1.3.3.3.7	Surface tension	A quantity characterizing the mechanical behaviour of the interface between two fluids (see ISO 31-3)	$\sigma^*$	$\text{J m}^{-2}$

**.4 Discharge, velocity and speed terms**

Clause	Term	Definition	Symbol	Unit
4.1	Discharge (volume flow rate)	Volume of water per unit time passing through any section in the system	Q	m <sup>3</sup> s <sup>-1</sup>
4.2	Mass flow rate	Mass of water flowing through any section of the system per unit time. Both p and Q shall be determined at the same section and at the conditions existing in that section  NOTE – The mass flow rate is constant between two sections if no water is added or removed	(pQ)	kg s <sup>-1</sup>
4.3	Measured discharge	Volume of water per unit time flowing through any measuring section, e.g. 1' (see 1.3.3.1.3 and 1.3.3.1.4)	Q <sub>1</sub> or Q <sub>2</sub>	m <sup>3</sup> s <sup>-1</sup>
4.4	Discharge at reference section	Volume of water per unit time flowing through the reference section 1 or 2	Q <sub>1</sub> or Q <sub>2</sub>	m <sup>3</sup> s <sup>-1</sup>
4.5	Corrected discharge at reference section	Volume of water per unit time flowing through the reference section referred to the ambient condition (see 1.3.3.5.2), e.g.  $Q_{1c} = (pQ)_1 / p_{amb}$ Given the normal conditions of a model test, Q <sub>1c</sub> may be assumed equal to Q <sub>1</sub>	Q <sub>1c</sub> or Q <sub>2c</sub>	m <sup>3</sup> s <sup>-1</sup>
4.6	Discharge at steady-state runaway speed	Discharge at n <sub>R</sub> (see 1.3.3.4.12)	Q <sub>R</sub>	m <sup>3</sup> s <sup>-1</sup>
4.7	No-load turbine discharge	Turbine discharge at zero mechanical power at specified speed (usually synchronous) and specified specific hydraulic energy	Q <sub>0</sub>	m <sup>3</sup> s <sup>-1</sup>
4.8	Leakage flowrate	Volumetric loss as illustrated in figure 6	q	m <sup>3</sup> s <sup>-1</sup>
4.9	Mean velocity	Discharge Q divided by area A of the cross-section	v	m s <sup>-1</sup>
4.10	Peripheral velocity	Peripheral velocity at the reference diameter (see figure 3): $u = \pi Dn$	u	m s <sup>-1</sup>
4.11	Rotational speed	Number of revolutions per unit time	n	s <sup>-1</sup>
4.12	Steady-state runaway speed	The steady-state rotational speed at zero mechanical power at specified hydraulic conditions and specified guide vane/blade/needle opening	n <sub>R</sub>	s <sup>-1</sup>
4.13	Maximum steady-state runaway speed	The highest value of steady-state runaway speed at specified hydraulic conditions (for the prototype, see detailed definition in IEC 60041)	n <sub>Rmax</sub>	s <sup>-1</sup>

**1.3.3.5 Pressure terms**

Subclause	Term	Definition	Symbol	Unit
1.3.3.5.1	Absolute pressure	The static pressure of a fluid measured with reference to a perfect vacuum	p <sub>abs</sub>	Pa
1.3.3.5.2	Ambient pressure	The absolute pressure of the ambient air (see 2.5.4.2). Values for standard atmosphere are given as a function of elevation in annex B, table B.6	p <sub>amb</sub>	Pa
1.3.3.5.3	Gauge pressure	The difference between the absolute static pressure of a fluid at the reference level of the pressure measuring instrument and the ambient pressure at the place and time of measurement,  $p = p_{abs} - p_{amb}$	p	Pa

**1.3.3.6 Specific energy terms**

In the International System of Units, mass (kg) is one of the base quantities. The energy per unit mass, known as specific energy, is used in this standard as a primary term instead of the energy per local unit weight which is called head, and was exclusively used in previous publications.

The latter term (head) has the disadvantage that weight is a force which depends on the local value of acceleration due to gravity g, which changes mainly with latitude but also with altitude. Nevertheless, the term "head" will still remain in use because it is very common. Therefore, both related energy terms are listed, the specific energy terms in this subclause and head terms in 1.3.3.7. They differ only by the factor g, which is the local value of acceleration due to gravity.

Clause	Term	Definition	Symbol	Unit
6.1	Specific energy	The energy per unit mass of water at any section	$e$	$\text{J kg}^{-1}$
6.2	Specific hydraulic energy of machine	Specific energy of water available between the high and low pressure reference sections 1 and 2 of the machine, taking into account the influence of compressibility <sup>1) 2)</sup>  $E = \frac{P_{\text{abs } 1} - P_{\text{abs } 2}}{\bar{\rho}} + \frac{v_1^2 - v_2^2}{2} + (z_1 - z_2)g$ <p>with <math>\bar{\rho} = \frac{\rho_1 + \rho_2}{2}</math> and assuming <math>g = g_1 = g_2</math></p> <p>The value of <math>\rho_1</math> and <math>\rho_2</math> can be calculated from <math>P_{\text{abs } 1}</math> and <math>P_{\text{abs } 2}</math> respectively, taking into account <math>\theta_1</math> or <math>\theta_2</math> for both values, given the negligible influence of the difference of the temperature on <math>\rho</math></p>	$E$	$\text{J kg}^{-1}$
6.3	Zero-discharge (shut-off) specific hydraulic energy of the pump	Pump specific energy at specified speed and specified guide vane and impeller blade settings with high pressure side shut off	$E_0$	$\text{J kg}^{-1}$
6.4	Suction specific potential energy of the machine	Specific potential energy at section 2 corresponding to the difference between the reference level of the machine (see 1.3.3.7.6) and the piezometric level at section 2  $E_s = g(z_r - z_2) = g(z_r - z_2) - \frac{P_{\text{abs } 2} - P_{\text{amb}}}{\rho_2}$ (see figure 45)	$E_s$	$\text{J kg}^{-1}$
6.5	Net positive suction specific energy	Absolute specific energy at section 2 minus the specific energy due to the vapour pressure $P_{\text{va}}$ <sup>3)</sup> referred to the reference level of the machine (see figure 45)  $\text{NPSE} = \frac{P_{\text{abs } 2} - P_{\text{va}}}{\rho_2} + \frac{v_2^2}{2} - g(z_r - z_2)$ $= -E_s + \frac{P_{\text{abs } 2} - P_{\text{va}}}{\rho_2} + \frac{v_2^2}{2}$	NPSE	$\text{J kg}^{-1}$

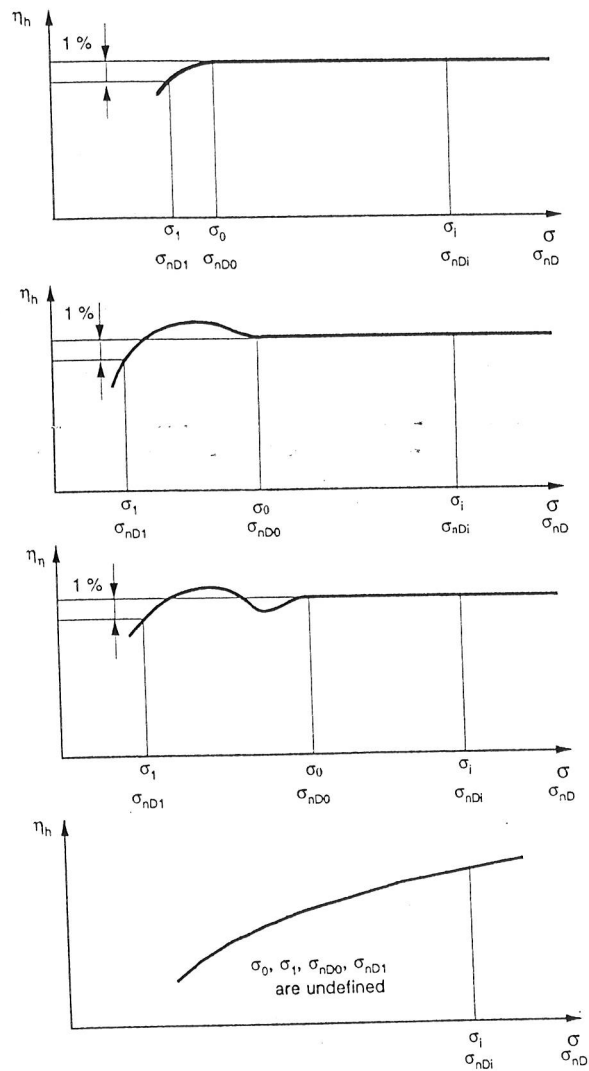
Subclause 3.5 illustrates some common cases of application of the basic formula for the specific hydraulic energy.

For derivation of  $E$ , see annex C.

See 1.3.3.3.4.

Subclause	Term	Definition	Symbol	Unit
1.3.3.6.6	Thoma number	Dimensionless term indicating the conditions of cavitation under which the machine operates. It is expressed as the ratio of net positive suction specific energy NPSE to a specific hydraulic energy $E$ (see 1.3.3.12.9)	$\sigma$	-
1.3.3.6.7	Cavitation coefficient	Dimensionless term indicating the conditions of cavitation under which the machine operates. It is expressed as the ratio of net positive suction specific energy NPSE to $n^2 D^2$ (see 1.3.3.12.10)	$\sigma_{nD}$	-
1.3.3.6.8	Thoma number zero <sup>1)</sup>	The lowest value of the Thoma number for which a chosen performance parameter (usually efficiency) remains unchanged as compared to its values at high Thoma number. In some cases, the shape of the cavitation curve $\eta_h(\sigma)$ is such that the Thoma number zero is difficult to define (see figure 4)	$\sigma_0$	-
1.3.3.6.9	Thoma number one <sup>1)</sup>	The value of the Thoma number for which a drop of one percentage point in efficiency is obtained compared with the efficiency at Thoma number zero. In some cases, the shape of the cavitation curve is such that the Thoma number one is difficult to define (see figure 4)	$\sigma_1$	-
1.3.3.6.10	Defined Thoma number <sup>1)</sup>	The value of the Thoma number associated with a defined onset of cavitation, e.g. a specified performance loss	$\sigma_d$	-
1.3.3.6.11	Incipient Thoma number <sup>1)</sup>	The value of the Thoma number associated with the beginning of visible runner/impeller cavitation usually detected by observation	$\sigma_i$	-
1.3.3.6.12	Plant Thoma number	The value of the Thoma number at the operating conditions of the prototype (see annex M)	$\sigma_{pl}$	-
1.3.3.6.13	Specific hydraulic energy loss	The specific hydraulic energy dissipated between any two sections	$E_L$	$\text{J kg}^{-1}$

1) A similar definition can be given for cavitation coefficient (see figure 4).

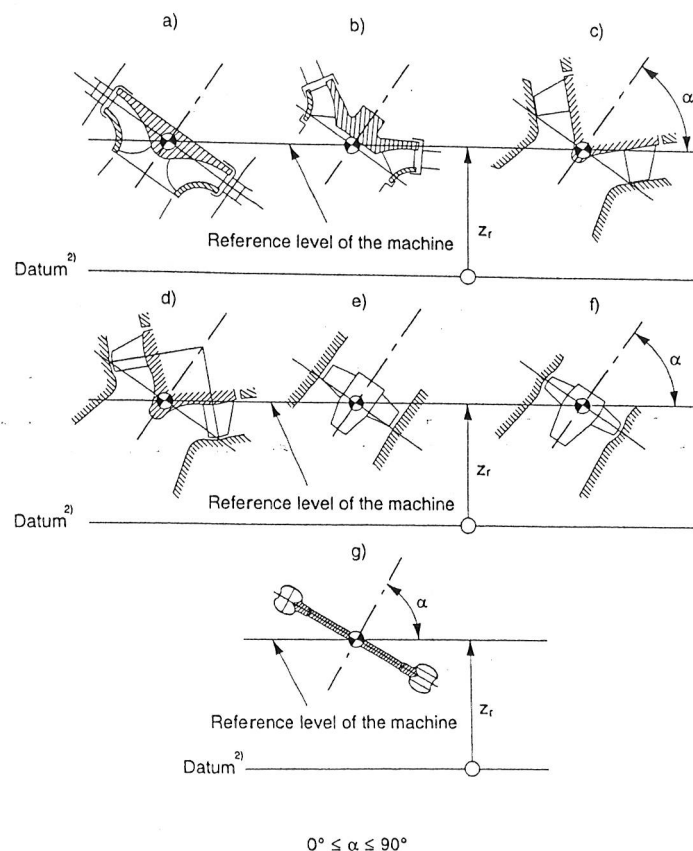
Figure 4 – Definition of  $\sigma_0$  and  $\sigma_1$ 

## 1.3.3.7 Height and head terms

Subclause	Term	Definition	Symbol	Unit
1.3.3.7.1	Head	Energy per local unit weight of water at any section $h = e/g$ For the definition of $e$ , see 1.3.3.6.1	$h$	m
1.3.3.7.2	Turbine or pump head	$H = E/g$ For the definition of $E$ , see 1.3.3.6.2	$H$	m
1.3.3.7.3	Zero discharge (shut-off) head of pump	$H_0 = E_0/g$ For the definition of $E_0$ , see 1.3.3.6.3	$H_0$	m
1.3.3.7.4	Suction height	$Z_s = E_s/g$ For the definition of $E_s$ , see 1.3.3.6.4	$Z_s$	m
1.3.3.7.5	Net positive suction head	$NPSH = NPSE/g$ For the definition of $NPSE$ , see 1.3.3.6.5	NPSH	m
1.3.3.7.6	Reference level of the machine	Elevation of a point of the machine taken as reference for the setting of the machine (see figure 5)	$z_r$	m
1.3.3.7.7	Cavitation reference level	Elevation of a point of the machine taken as reference for cavitation evaluation during model tests (see 2.3.1.5.1)	$z_c$	m
1.3.3.7.8	Reference level of the pressure measuring instrument	Elevation of a pressure measuring device (see figure 38)	$z_M$	m

## 1.3.3.8 Power and torque terms

Subclause	Term	Definition	Symbol	Unit
1.3.3.8.1	Hydraulic power	The hydraulic power available for producing power (turbine) or imparted to the water (pump) $P_h = E(\rho Q)_1$	$P_h$	W
1.3.3.8.2	Mechanical power of the machine (power)	The mechanical power delivered by the turbine shaft or to the pump shaft, assigning to the hydraulic machine the mechanical losses of the relevant bearings and shaft seals (see figure 6)	$P$	W
1.3.3.8.3	Mechanical power of runner(s)/impeller(s)	Mechanical power transmitted through the coupling of the runner(s)/impeller(s) and the shaft (see figure 6)	$P_m$	W
1.3.3.8.4	Mechanical power losses	Mechanical power dissipated in guide bearings, thrust bearings and shaft seals of the hydraulic machine (see figure 6)	$P_{Lm}$	W
1.3.3.8.5	Zero discharge (shut-off) power of the pump	Pump power at specified speed and at specified guide vane and impeller settings with high pressure side shut-off	$P_o$	W
1.3.3.8.6	Shaft torque	Torque applied to the shaft of the hydraulic machine and corresponding to the mechanical power of the machine (see 1.3.3.8.2)	$T$	N·m
1.3.3.8.7	Runner/impeller torque	Torque transmitted through the coupling of the runner/impeller and the shaft and corresponding to the mechanical power of runner/impeller (see 1.3.3.8.3)	$T_m$	N·m
1.3.3.8.8	Friction torque	Friction torque in guide bearings, thrust bearings and shaft seals of the hydraulic machine (see 1.3.3.8.4)	$T_{Lm}$	N·m



$$0^\circ \leq \alpha \leq 90^\circ$$

Radial machines, such as Francis turbines, radial (centrifugal) pumps and pump-turbines; for multistage machines; low pressure stage.

Diagonal (mixed-flow, semi-axial) machines with fixed runner/impeller blades and with runner/impeller band.

Diagonal (mixed-flow, semi-axial) machines with fixed runner/impeller blades, without runner/impeller band.

Diagonal (mixed-flow, semi-axial) machines with adjustable runner/impeller blades.

Axial machines, such as propeller turbines, tubular turbines<sup>1)</sup>, axial pumps and pump-turbines with fixed runner/impeller blades.

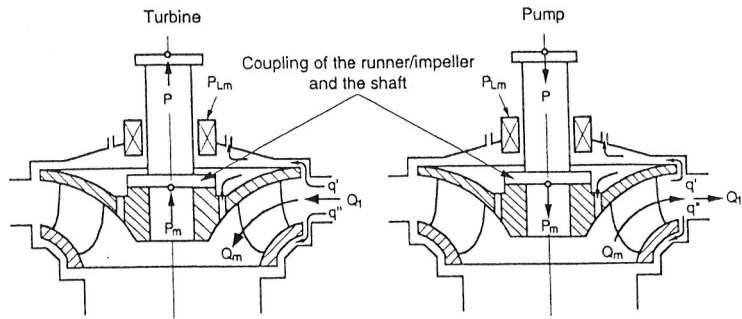
Axial machines, such as Kaplan turbines, tubular turbines<sup>2)</sup>, axial pumps and pump-turbines with adjustable runner/impeller blades.

Pelton turbines.

Figure 5 – Reference level of machine

<sup>1)</sup> The term "tubular turbines" includes bulb, pit, rim generator and S-type units.

<sup>2)</sup> See 1.3.3.2.10.



	Turbine	Pump
	$q = q' + q''$	$q' = q' + q''$
	$Q_1 = Q_m + q$	$Q_1 = Q_m - q$
	$P_h = E \cdot (\rho \cdot Q)_1$	$P_h = E \cdot (\rho \cdot Q)_1$
	$P = P_m - P_{Lm}$	$P = P_m + P_{Lm}$
volumetric efficiency	$\eta_v = \frac{Q_m}{Q_1}$	$\eta_v = \frac{Q_1}{Q_m}$
hydraulic efficiency (note 3)	$\eta_h = \frac{P_m}{P_h}$	$\eta_h = \frac{P_h}{P_m}$
efficiency	$\eta = \frac{P}{P_h}$	$\eta = \frac{P_h}{P}$

NOTES

The formulae ignore the compressibility of the water.

For detailed analysis of internal losses, refer to annex N.

The disk friction losses and leakage losses (volumetric losses) are considered as hydraulic losses in this formula. These "disk friction losses" are the friction losses of the outer surfaces of the runner/impeller not in contact with the flow  $Q_m$  passing the runner/impeller blades.

Figure 6 – Flux diagram for power and discharge

1.3.3.9 Efficiency terms

Subclause	Term	Definition	Symbol	Unit
1.3.3.9.1	Hydraulic efficiency <sup>1)</sup>	a) Turbine: ratio of mechanical power of runner to the hydraulic power $\eta_h = \frac{P_m}{P_h}$ b) Pump: ratio of hydraulic power to the mechanical power of the impeller $\eta_h = \frac{P_h}{P_m}$ See figure 6	$\eta_h$	-
1.3.3.9.2	Mechanical efficiency	a) Turbine $\eta_m = \frac{P}{P_m}$ b) Pump $\eta_m = \frac{P_m}{P}$	$\eta_m$	-
1.3.3.9.3	Efficiency	a) Turbine $\eta = \frac{P}{P_h} = \eta_h \eta_m$ b) Pump $\eta = \frac{P_h}{P} = \eta_h \eta_m$	$\eta$	-
1.3.3.9.4	Weighted average efficiency	Calculated from the formula $\eta_w = \frac{w_1 \eta_1 + w_2 \eta_2 + w_3 \eta_3 + \dots}{w_1 + w_2 + w_3 + \dots}$ where $\eta_1, \eta_2, \eta_3, \dots$ are the values of efficiency at specified operating conditions and $w_1, w_2, w_3, \dots$ are their agreed weighting factors respectively	$\eta_w$	-
1.3.3.9.5	Arithmetic average efficiency	The weighted average efficiency (1.3.3.9.4) with $w_1 = w_2 = w_3 \dots$	$\eta_a$	-

<sup>1)</sup> The disk friction losses and leakage losses (volumetric losses) are included and are considered here as hydraulic losses. The disk friction losses are the friction losses of the outer surfaces of the runner/impeller not in contact with the flow passing the blades.

### 3.10 General terms relating to fluctuating quantities

60994 provides a reference for terms relating to these quantities. The following table lists terms relevant to this standard, some of which are illustrated in figure 7:

Subclause	Term	Definition	Symbol	IEC 60994 Reference
3.3.10.1	Discrete quantity	Quantity represented by a sequence of its momentary values	X	
3.3.10.2	Fluctuation of quantity (pulsation of quantity)	Oscillatory variation of a quantity X referred to its mean value during a time interval $\Delta t$ previously selected	$\tilde{X}(t)$	2.3.1.5, etc.
3.3.10.3	Mean value	$\bar{X} = \frac{\sum_{n=1}^N X_n}{N}$	$\bar{X}$	2.3.3.1
3.3.10.4	Maximum value		$X_{\max}$	
3.3.10.5	Minimum value		$X_{\min}$	
3.3.10.6	Standard deviation (effective value referred to the mean)	$\tilde{X}_{\text{eff}} = \sqrt{\frac{\sum_{n=1}^N (X_n - \bar{X})^2}{N}}$	$\tilde{X}_{\text{eff}}$	2.3.3.2
3.3.10.7	Root-mean-square value	$X_{\text{rms}} = \sqrt{\frac{\sum_{n=1}^N X_n^2}{N}}$	$X_{\text{rms}}$	2.3.3.3
3.3.10.8	Peak-to-peak value	$\Delta X_{\text{pp}} = X_{\max} - X_{\min}$	$\Delta X_{\text{pp}}$	2.3.2.11
3.3.10.9	Amplitude	Maximum value of a sinusoidal quantity X(t): $A = \frac{1}{2} \Delta X_{\text{pp}}$	A	2.3.2.10

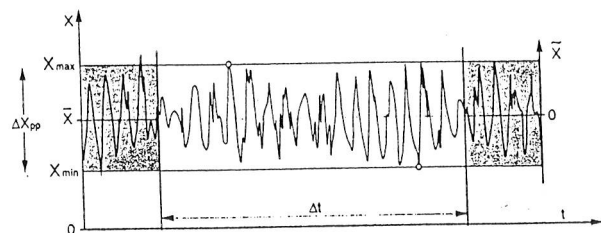


Figure 7 – Illustration of some definitions related to oscillating quantities

### 1.3.3.11 Fluid dynamic and scaling terms <sup>1)</sup>

Subclause	Term	Definition	Symbol	Unit
1.3.3.11.1	Reynolds number	Ratio of inertia forces to viscous forces $Re = \frac{Du}{\nu} \text{ or } \frac{Bv}{\nu} \text{ (see 2.3.1.1)}$	Re	-
1.3.3.11.2	Froude number <sup>2)</sup>	Square root of the ratio of inertia forces to gravity forces $Fr = \left[ \frac{E}{gD} \right]^{1/2} \text{ or } \left[ \frac{E}{gB} \right]^{1/2} \text{ (see 2.3.1.1)}$	Fr	-
1.3.3.11.3	Weber number <sup>2)</sup>	Ratio of inertia forces to surface tension forces $We = \left[ \frac{\rho L v^2}{\sigma^*} \right]^{1/2}$ where v is the velocity $\sigma^*$ is the surface tension $\rho$ is the density L is a linear dimension	We	-
1.3.3.11.4	Euler number	Ratio of pressure forces to inertia forces $Eu = \frac{\Delta p}{\rho v^2}$ where $\Delta p$ is the differential pressure	Eu	-
1.3.3.11.5	Loss distribution coefficient	Ratio of relative scalable losses to relative total losses	V	-
1.3.3.11.6	Relative scalable loss	$\delta = (1 - \eta_h) V$	$\delta$	-
1.3.3.11.7	Relative non-scalable loss	$\delta_{ns} = (1 - \eta_h) - \delta = (1 - \eta_h) \cdot (1 - V)$	$\delta_{ns}$	-
1.3.3.11.8	Relative total loss	$1 - \eta_h = \delta + \delta_{ns}$		-
1.3.3.11.9	Difference of hydraulic efficiency	Difference between the values of hydraulic efficiency at two hydraulically similar <sup>3)</sup> operating points measured at different Reynolds numbers.	$\Delta \eta_h$	-

<sup>1)</sup> See ISO 31-12.

<sup>2)</sup> Other definitions of these numbers can be found in relevant scientific works.

<sup>3)</sup> See 2.3.1.2.

## 1.12 Dimensionless terms

nine performance may be characterized by dimensionless terms based  $E = 1$ ,  $D = 1$  and  $\rho = 1$  or on  $n = 1$ ,  $D = 1$  and  $\rho = 1$ .

relations of these dimensionless terms to other existing definitions are given in annex A.

clause	Term	Definition	Symbol	Relations
3.12.1	Speed factor	$\frac{nD}{E^{0.5}}$	$n_{ED}$	$= \frac{1}{E_{nD}^{0.5}}$
3.12.2	Discharge factor	$\frac{Q_1}{D^2 E^{0.5}}$	$Q_{ED}$	$= \frac{Q_{nD}}{E_{nD}^{0.5}}$
3.12.3	Torque factor	$\frac{T_m}{\rho_1 D^3 E}$	$T_{ED}$	$= \frac{T_{nD}}{E_{nD}} = \frac{P_{ED}}{2\pi n_{ED}}$
3.12.4	Power factor	$\frac{P_m}{\rho_1 D^2 E^{1.5}}$ (see note)	$P_{ED}$	$= Q_{ED} \eta_{hT}$ (turbine) $= \frac{Q_{ED}}{\eta_{hP}}$ (pump) $= \frac{P_{nD}}{E_{nD}^{1.5}} = P_{nD} n_{ED}^3$ $= 2\pi n_{ED} T_{ED}$
3.12.5	Energy coefficient	$\frac{E}{n^2 D^2}$	$E_{nD}$	$= \frac{1}{n_{ED}^2}$
3.12.6	Discharge coefficient	$\frac{Q_1}{n D^3}$	$Q_{nD}$	$= \frac{Q_{ED}}{n_{ED}} = Q_{ED} E_{nD}^{0.5}$
3.12.7	Torque coefficient	$\frac{T_m}{\rho n^2 D^5}$	$T_{nD}$	$= \frac{T_{ED}}{n_{ED}^2} = T_{ED} E_{nD} = \frac{P_{nD}}{2\pi}$
3.12.8	Power coefficient	$\frac{P_m}{\rho_1 n^3 D^5}$ (see note)	$P_{nD}$	$= E_{nD} Q_{nD} \eta_{hT}$ (turbine) $= \frac{E_{nD} Q_{nD}}{\eta_{hP}}$ (pump) $= \frac{P_{ED}}{n_{ED}^3} = P_{ED} E_{nD}^{1.5} = 2\pi T_{nD}$
3.12.9	Thoma number	$\frac{NPSE}{E}$	$\sigma$	$= \frac{\sigma_{nD}}{E_{nD}} = \sigma_{nD} n_{ED}^2$
3.12.10	Cavitation coefficient	$\frac{NPSE}{n^2 D^2}$	$\sigma_{nD}$	$= \sigma E_{nD} = \frac{\sigma}{n_{ED}^2}$
3.12.11	Specific speed	$\frac{n Q^{0.5}}{E^{0.75}}$	$N_{QE}$	$= n_{ED} Q_{ED}^{0.5} = \frac{Q_{nD}^{0.5}}{E_{nD}^{0.75}}$

NOTE – Reference is made to the mechanical power of the runner/impeller, usually measured on the model.

Units: H (m); D (m); E (J kg<sup>-1</sup>); n (s<sup>-1</sup>);  $\rho$  (kg m<sup>-3</sup>); T (N m); P (W); Q (m<sup>3</sup> s<sup>-1</sup>).

## 1.3.3.13 Dimensionless terms relating to oscillating quantities

For presentation and analysis of the measured oscillating quantities, it is recommended to use dimensionless terms as defined hereafter and in 4.3 to 4.6. They are identified by the symbol of the measured quantity with subscripts denoting the machine component and the quantities taken as unity; for instance  $T_{G,ED}$  will denote the guide vane torque factor, i.e. the torque acting on the guide vanes based on specific hydraulic energy of the machine and reference diameter equal to unity. The symbols used to define the measurements are listed below.

- Measured quantities are:
  - F force;
  - M moment;
  - p pressure;
  - T torque.
- Subscripts for machine components are:
  - B runner blade;
  - D Pelton deflector;
  - G guide vane;
  - N Pelton needle.
- Subscripts for force and torque components are:
  - a axial;
  - r radial;
  - x,y,z cartesian coordinates related to the machine.

The following table lists the dimensionless terms relating to oscillating quantities.

Subclause	Term	Definition	Symbol
1.3.3.13.1	Torque factor	$T_{ED} = \frac{T}{\rho D^3 E}$	$T_{ED}$
1.3.3.13.2	Force factor	$F_{ED} = \frac{F}{\rho D^2 E}$	$F_{ED}$
1.3.3.13.3	Torque coefficient	$T_{nD} = \frac{T}{\rho n^2 D^5}$	$T_{nD}$
1.3.3.13.4	Force coefficient	$F_{nD} = \frac{F}{\rho n^2 D^4}$	$F_{nD}$
1.3.3.13.5	Factor of pressure fluctuation	$\tilde{p}_E = \frac{\tilde{p}}{\rho E}$	$\tilde{p}_E$

## 1 Nature and extent of guarantees related to hydraulic performance

### 1.1 General

#### 1.1.1 Design data and co-ordination

The purchaser shall be responsible for specifying the data on which guarantees are based (including, for example, reference sections, water levels, specific hydraulic energies (see 1.3.3.6.2), and specific hydraulic energy losses. The purchaser is also responsible for co-ordinating efforts to determine interactions between the waterways and the electrical and mechanical parts of the machine.

The purchaser shall arrange for the machine supplier to be provided with data, accurate and efficient in detail, to cover the following:

- operating water levels in all reservoirs;
- hydraulic losses of each part of the water conduit from intake to outlet;
- design drawings of water conduits associated with the hydraulic machine including valves and gates;
- any information relevant to the water flow in the conduit, such as any results of model tests of the conduits;

In the case of rehabilitation of existing machines, particular attention is to be paid to the limitations imposed by the existing equipment (for example openings).

Attention shall be paid to flow conditions at the model inlet and outlet (see 2.1.2.4 and 2.1.3.3). In most cases, it will be sufficient to extend the model just beyond the high and low pressure reference sections. These sections shall be included for the model tests in order to conform to the standard. If the prototype installation is such that there is reason to believe that the total flow pattern through the waterways is not fully represented by the model, the contract shall specify the steps to be taken, which may include specifying the extent of the water passages to be modelled. In some other cases, the validity of the approach conditions shall have been verified by the purchaser through the test of a partial model of the plant prior to the test of the model machine.

#### 1.1.2 Definition of the hydraulic performance guarantees

The contract for both regulated<sup>1)</sup> and non-regulated prototype machines shall contain, as a minimum, guarantees covering power, discharge and/or specific hydraulic energy, efficiency, maximum momentary overspeed and maximum/minimum momentary pressure and maximum steady-state runaway speed (reverse runaway speed for a pump), as well as guarantees related to cavitation.

For a pump, the guarantee may also cover the maximum specific hydraulic energy (head) and a power at zero discharge, the latter with the impeller rotating in water and/or air at the specified speed.

The guarantees shall be given for one or more operating points (see 1.4.2.2). These points correspond to performance curves of the machine, which are usually submitted by the supplier. In some cases (e.g. small hydro), a table may be sufficient.

If the current state of the art permits the verification of some of these prototype guarantees by model test (see 1.4.2), while others cannot be verified by model tests (see 1.4.3). Moreover, additional data may be obtained from the model as an indication of the expected prototype operation (see 1.4.4).

<sup>1)</sup> "Regulated" as used in this standard refers to the control of the discharge through variations of guide vane opening, needle stroke and/or runner/impeller blade angle.

### 1.4.1.3 Guarantees of correlated quantities

It is recommended that the contract does not fix more than one guarantee for correlated quantities; for example in the case of a regulated turbine, efficiency shall be guaranteed versus either discharge or power, but not both.

#### 1.4.1.4 Form of guarantees

Either of the following two forms of guarantees may be applied when the performance of a prototype machine is to be accepted on the basis of a model test:

- a) Guarantees for the hydraulic performance of the prototype, computed from model test results with allowance for scale effect. For reaction machines, the scale effect is to be taken into account in accordance with 3.8. For impulse turbines, when it is agreed in the contract, the scale effect should be taken into account in accordance with annex K.
- b) Guarantees for the hydraulic performance of the model referred to a Reynolds number (Reynolds, Froude and Weber numbers for impulse turbines) to be specified in the contract.

In each case, the similitude requirements of 2.3.1 shall be met.

### 1.4.2 Main hydraulic performance guarantees verifiable by model test

#### 1.4.2.1 Guaranteed quantities for any machine

The main hydraulic performance guarantees of the prototype or model that can be verified by model tests are described in detail in 1.4.2.1.1 to 1.4.2.1.5 below.

##### 1.4.2.1.1 Power

The term "power" usually refers to the mechanical power of the runner/impeller (see 1.3.3.8.3). When the mechanical power of the machine (see 1.3.3.8.2) is guaranteed for the prototype, the mechanical power losses (see 1.3.3.8.4) are to be taken into account.

##### 1.4.2.1.2 Discharge and/or specific hydraulic energy

This refers either to the discharge at the reference section (see 1.3.3.4.4), obtained when operating under specified specific hydraulic energies, or to the specific hydraulic energy obtained when operating with specified discharges.

##### 1.4.2.1.3 Efficiency

The term "efficiency" refers to the hydraulic efficiency (see 1.3.3.9.1) unless otherwise specified. When the prototype efficiency (see 1.3.3.9.3) is guaranteed, the mechanical power losses (see 1.3.3.8.4) or the mechanical efficiency (see 1.3.3.9.2) is to be taken into account.

In reaction machines, the relationship between model and prototype hydraulic efficiencies due to the Reynolds number scale effect is well documented at and around the point of best efficiency, as explained in 3.8. The currently accepted convention is to apply this relationship to the entire range of guaranteed efficiencies (see annex F), however recognizing the decreased reliability the further away the point to be checked is from the point of best efficiency.

#### 4.2.1.4 Steady-state runaway speed and/or discharge

guarantee for maximum steady-state runaway speed (see 1.3.3.4.12) or for the reverse runaway speed in case of pumps is required. An additional guarantee for maximum discharge under runaway conditions may be required.

The no-load discharge for turbine operation shall be determined as part of the characteristic runaway-curve (see figure 55).

#### 4.2.1.5 Influence of cavitation on hydraulic performance

The contract shall clearly state the hydraulic conditions (specific hydraulic energies and net positive suction specific energies) for which the hydraulic performances are to be guaranteed.

The guarantees of the hydraulic performance of the prototype shall include the influence of cavitation. According to current engineering practice, this influence is determined by the model tests performed in accordance with 2.3.1.5.1, 2.3.3.3.6, 3.8.2.3.7 and 3.8.3.2.

The application of efficiency scale-up due to Reynolds number is limited to the range of values specified in 3.8.2.4.2. The contract shall specify the procedure to be used if  $\sigma_{pi}$  falls outside this range.

In some cases, the contract may contain an additional clause on cavitation specifying that the measured value of the Thoma number chosen as criterion ( $\sigma_d$ ) shall be lower than the plant Thoma number  $\sigma_{pi}$  by a safety margin (see 3.10.5). The criterion and the safety margin shall be specified in the contract.

### 4.2.2 Specific application

#### 4.2.2.1 Regulated turbine (see 3.10.3.1)

Power: to be reached at one or more specified specific hydraulic energies.  
 Discharge: to be reached at one or more specified specific hydraulic energies.  
 Efficiency: guarantees may be required for one or more specified specific hydraulic energy as follows:  
 – at one or more specified power or discharge,  
 or  
 – as weighted average efficiencies over a specified range of power or discharge,  
 or  
 – as arithmetic average efficiencies<sup>1)</sup> over a specified range of power or discharge.

Runaway speed: guaranteed steady-state runaway speed not to be exceeded when operating under maximum or any other specified specific hydraulic energy.

In the case of double regulated machines, it shall be stated if the guarantee refers to the condition in which the optimum relationship between guide vane opening and runner blade angle is maintained (on-cam condition) or/and to the maximum runaway speed occurring in the worst possible off-cam condition.

<sup>1)</sup> Weighted or arithmetic average efficiencies and a series of individual efficiencies shall not be guaranteed simultaneously.

Cavitation: guarantees as outlined in 1.4.2.1.5 may be required for one or more specified specific hydraulic energy, discharge or power, usually for the corresponding minimum  $\sigma_{pi}$  value.

#### 1.4.2.2.2 Non-regulated turbine (see 3.10.3.2)

Power: power to be reached and power not to be exceeded over a specified range of specific hydraulic energies<sup>1)</sup>.  
 Discharge: discharge to be reached and/or not to be exceeded over a specified range of specific hydraulic energies. This guarantee is usually replaced by the corresponding power guarantee.  
 Efficiency: guarantees may be required as follows  
 – at one or more specified specific hydraulic energy,  
 or  
 – as a weighted average efficiency over a specified range of specific hydraulic energy,  
 or  
 – as an arithmetic average efficiency<sup>2)</sup> over a specified range of specific hydraulic energy.  
 Runaway speed: guaranteed steady-state runaway speed not to be exceeded when operating under maximum specific hydraulic energy.  
 Cavitation: guarantees as outlined in 1.4.2.1.5 may be required for one or more specified specific hydraulic energy, usually for the corresponding minimum  $\sigma_{pi}$  value.

#### 1.4.2.2.3 Non-regulated/regulated pump (see 3.10.3.3)

Power: power not to be exceeded over a specified range of specific hydraulic energy or discharge.  
 Discharge and/or specific hydraulic energy: discharge over a specified range of specific hydraulic energy or specific energy over a specified range of discharge, including values to be reached and/or not to be exceeded.  
 Efficiency: guarantees may be required for one or more specified specific hydraulic energy or discharge as follows:  
 – at one or more specified specific hydraulic energy or discharge,  
 or  
 – as a weighted average efficiency over a specified range of specific hydraulic energy or discharge,  
 or  
 – as an arithmetic average efficiency<sup>2)</sup> over a specified range of specific hydraulic energy or discharge.  
 Runaway speed: guaranteed maximum steady-state reverse runaway speed not to be exceeded when operating under maximum specified specific hydraulic energy.

In the case of double regulated machines, it shall be stated if the guarantee is referred to the condition in which the optimum relationship between guide vane opening and runner blade angle is maintained (on-cam condition) or/and to the maximum runaway speed occurring in the worst possible off-cam condition.

<sup>1)</sup> For the contractual limits of the power corresponding to the specified specific hydraulic energies, see 3.10.3.2.

<sup>2)</sup> Weighted or arithmetic average efficiencies and a series of individual efficiencies shall not be guaranteed simultaneously.

itation: guarantees as outlined in 1.4.2.1.5 may be required for one or more specified specific hydraulic energy, discharge or power, usually for the corresponding minimum  $\sigma_{pi}$  value.

### 1.3 Guarantees not verifiable by model test

ere are certain guarantees that cannot be checked by model tests. Amongst them are:

#### 1.3.1 Guarantees on cavitation erosion

e amount of cavitation pitting is to be guaranteed for the prototype only. Evaluation of this arantee on the prototype shall be carried out in accordance with the recommendations of C 60609.

e model test may reveal some of the potential areas of cavitation erosion by visual pection during the tests (see 2.3.3.3.6).

#### 1.3.2 Guarantees on maximum momentary overspeed and maximum momentary pressure rise

mentary overspeed (including momentary runaway speed) and pressure depend primarily on water conduit geometry (penstock length, surge tank, etc.), the inertia of the rotating part the unit and the operating law of the guide vanes. They can therefore not be determined ectly by a dynamic test on the model which does not reproduce either the full extent of the plicable waterways, the inertia of the unit or the characteristics of the speed governor. vertheless, the steady-state model test data, transferred to the prototype, provide values abling calculation of the transient phenomena with sufficient accuracy.

#### 1.3.3 Guarantees covering noise and vibration

etermination of prototype noise and vibration by model tests lies outside the scope of this indard. This standard should be used only as a guide for the modelling of the hydraulic urces of these phenomena (i.e. through determination of the pressure fluctuations or other namic loads).

### 1.4 Additional performance data

ditional data may be obtained from the model as an indication of expected prototype eration:

pressure fluctuations (see 4.3);

shaft torque fluctuations (see 4.4);

hydraulic thrust, both radial and axial (see 4.5);

hydraulic torque on guide vanes and adjustable runner/impeller blades or hydraulic forces on needles and deflectors over the full operating range (see 4.6);

characteristics in four quadrant operation including power and specific hydraulic energy at zero discharge (shut-off conditions) of a pump with impeller rotating in water or air (see 4.7);

differential pressure measurements in view of prototype index tests (see 4.8);

cam relationship for optimum performance in the case of double regulated machines (relation between guide vane and runner/impeller blade openings) (see 3.8).

may also be specified to determine other additional data, such as velocity or pressure tribution in various components of the machine, etc.

## 2 Execution of tests

### 2.1 Requirements of test installation and model

#### 2.1.1 Choice of laboratory

Any laboratory satisfying the criteria set out in this standard concerning general layout, capacity and quality of instrumentation should be deemed suitable. An independent laboratory is sometimes preferable, particularly when comparative tests are required with models from different manufacturers.

#### 2.1.2 Test installation

##### 2.1.2.1 General characteristics of the test circuit

The test circuit shall be such that when cavitation appears in the model, it shall not occur elsewhere to an extent whereby it affects the stability or the satisfactory operation of the installation or of the model performance measurement.

Any entrained air bubbles produced by cavitation in the model shall not affect the functioning of instrumentation, particularly the flow measuring device and the pressure measurement lines.

The circuit shall be designed in such a manner that no leakage or addition of water may occur between the flow measuring instrument and the model. This criteria should be easily verifiable.

##### 2.1.2.2 Capacity of the test installation

The capacity of the test installation (i.e. power, pressure, specific hydraulic energy, discharge and NPSE) shall be such that the minimum values for model size and the required test conditions as listed in 2.3.2.2 can be met.

The operation shall be stable and steady without surging or fluctuating effects (see 2.3.2.3).

##### 2.1.2.3 Condition of the water

The test water shall be clean, clear and free of any solid material in suspension and any chemical impurities which may have an influence on the water properties such as viscosity and vapour pressure. Free gas and air bubbles should be removed as far as possible before testing.

The gas content (see 2.3.1.6.2), including both entrained and dissolved gas, of the water used in the test rig, should be recorded for the test, especially with respect to repeatability of cavitation test results and for comparison purposes. It shall be measured at the inlet, close to the model (see 2.5.3.2).

Experience in closed circuits indicates that dissolved air may produce nuclei in the water and the nuclei content plays a major role in travelling cavitation<sup>1)</sup>. It may strongly influence the cavitation pattern and the resulting cavitation characteristics (see 2.3.1.5, 2.3.1.6.2 and figures 71 and 72).

Cavitation similitude should be respected by performing the test using an appropriate specific hydraulic energy or/and nuclei injection.

<sup>1)</sup> Nuclei are small air or gas bubbles with diameter less than 50  $\mu\text{m}$ . Travelling cavitation has the aspect of bubbles moving with the flow. Travelling cavitation is typical at the outlet of Francis turbines (see [1], annex P, Bibliography).

The water temperature should in principle not exceed 35 °C and should not vary significantly during the tests (e.g. 5 °C per day). Large differences between the water temperature and the ambient temperature of instruments should be avoided, as they could influence the accuracy of the measurements.

#### 1.1.2.4 Flow conditions given by the installation

At the model inlet, the test installation shall ensure favourable hydraulic conditions free from vortices, undue turbulence and unsteadiness.

At the model outlet, the flow pattern shall not be influenced by the layout or construction of the test facility.

#### 1.1.2.5 Measuring instruments

The measuring equipment used to determine the main parameters shall satisfy the specified conditions of this standard.

The traceability of each instrument to a recognized national or international standard shall be ensured. All instruments should be calibrated *in situ*, especially discharge and torque measuring instruments.

The measuring instruments should be such that a direct reading, independent of the data acquisition system, is possible in order to permit an easy verification.

#### 1.1.3 Model requirements

The model shall meet the following conditions:

##### 1.1.3.1 Model size

The minimum values for model size are prescribed in 2.3.2.2.

Normally, models shall be as large as practical but never less than the values stated. The same model should be used for all tests related to main hydraulic performance guarantees and influence of cavitation (see 1.4.2). Comparative model tests shall be performed with models of the same size.

##### 1.1.3.2 Layout and mechanical design of the model

The layout and mechanical design of the model shall comply with the specified items of testing. The following points shall be carefully considered:

- deformations due to loading under the chosen test head shall be minimized by appropriate design and choice of material;
- elements used to vary machine geometry (runner/impeller blades, guide vanes, nozzles) shall be capable of repeating and maintaining a set position;
- bearing system, shaft and stationary parts shall have sufficient rigidity to avoid contact in the labyrinth during normal operation. Blade tip and seal labyrinth clearances of less than 0,15 mm are not recommended for mechanical reasons;
- hydraulically smooth surfaces of the water passages are recommended;
- in addition to general requirements for surface conditions, great care should be given to the proper matching of joints in order to avoid any local flow separation;
- materials should be chosen to avoid oxidation and electrochemical corrosion. The water passage surfaces should remain in good condition for the test duration;

- provision shall be made for easy cleaning or repairing of water passages;
- a transparent cone or windows should be provided for observation of the flow in the runner/impeller and in the adjacent portion of the draft tube (at the low pressure stage in case of a multistage machine);
- wherever shaft seals and shaft bearings are required to be a part of the model (e.g. multistage machines) when comparative model tests are performed, these parts are to be of identical design;
- for comparative tests of the same model, but with different impeller/runner, provisions shall be made that all runners/impellers can be tested with the same clearances;
- where additional data have to be measured (such as pressure fluctuations, guide vane torque, velocity distribution) the model shall permit easy installation and checks of the corresponding measuring equipment;
- if any non-homology exists (e.g. differences in runner band/crown thickness, seal design, etc.), any analytical procedures adopted to account for these differences shall be mutually agreed.

#### 2.1.3.3 Extent of model

The position of reference sections and the extent of the water passages from inlet to outlet to be included in the model (at least the part between the high pressure and low pressure reference sections) shall be clearly defined in the contract (see figure 1 and as an example figure 44).

All the water passages influencing the performance of the prototype, i.e. inflow and outflow conditions, should as far as possible be included in the model.

Especially for low specific hydraulic energy turbines, it is recommended that the model extends from the prototype inlet to the outlet section of the draft tube.

Upstream or downstream gate slots are not required, unless they are located between the measuring or reference sections of the machine. Information on the influence of these parts on the hydraulic behaviour of the machine may be obtained from tests in addition to the model acceptance tests.

#### 2.1.3.4 Geometric similarity of model and prototype

##### 2.1.3.4.1 General requirements

A basic requirement for determining prototype performance from model tests is to have geometrical similarity (homology) between model and prototype. Therefore it is necessary to compare on both machines the geometrical dimensions and the surface finish of all components in contact with the flow.

The geometric similarity between model and prototype is to be checked in accordance with 2.2.

Unless otherwise specified, the model shall be geometrically similar (homologous) to the prototype in all wetted parts within the limits defined in 2.1.3.3. This also includes details that may have a measurable influence on the performance. However, in particular cases where some minor deviations from the similarity cannot be avoided, an agreement shall be reached whether the results are to be corrected or not.

In the case of acceptance tests on both model and prototype, the same measuring sections should be used if possible.

For comparative model tests, all models shall rotate in the same direction.

### 1.3.4.2 Multistage machines

Normally the model test should be performed with the same number of stages as the prototype.

or a prototype with four or more stages, in exceptional cases, the model may be tested with a reduced number of stages, for instance a three-stage model for a four-stage prototype.

### 1.3.4.3 Labyrinth seals and thrust balancing provisions

For mechanical reasons, it may not be possible or desirable (especially for large scale ratios) for the shaft and runner/impeller seal clearances and the thrust balancing provision to be either geometrically similar or hydraulically equivalent between the model and the prototype. In such cases, seal leakage losses and thrust coefficient will differ between model and prototype. The differences shall either be negligible or be accurately estimated so that the hydraulic efficiency and the thrust of the prototype can be computed.

An agreement should be reached before the tests concerning the monitoring and measuring of average flow rate  $q'$  (see figure 6) and whether or not it should be taken into account in determining machine performance.

## 2 Dimensional check of model and prototype

### 2.1 General

As stated in 2.1.3.4, the geometrical similarity between model and prototype shall be checked. The checking procedure and admissible tolerances are described below.

This applies even in the case where the model is manufactured according to an existing machine and hence the prototype is the starting point of the process.

#### 2.1.1 Explanation of terms used for model and prototype

##### 1) individual value

The value resulting from:

the measurement of the **same** dimension of the **same** component taken at **different** locations (e.g. reference diameter of a runner/impeller);

or:

the measurement of the **same** dimension of **different recurrent** components taken at the **same** location (e.g. maximum thickness of guide vanes).

##### 2) average value

The value is the arithmetical mean value calculated from several individual values.

##### 3) theoretical value

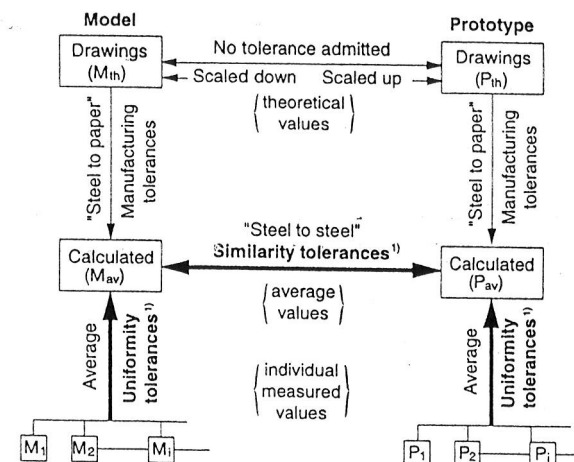
The design value indicated on a drawing. Corresponding model and prototype dimensions  $L_M$  and  $L_P$  are linked by the scale length ratio  $\lambda_L$  (see 1.3.3.2.9).

#### 2.1.2 Purpose of dimensional checks

Dimensional checking:

- 1) ascertains the main dimensions of model and prototype;

- 2) checks the uniformity of model and prototype in their recurrent components, i.e. compares the relative deviation between the individual values and the corresponding average value. The permissible maximum deviations are given in the "uniformity tolerance" columns of 2.2.2.1.7 and 2.2.2.2.5;
- 3) checks the geometrical similarity between prototype and model, i.e. compares the relative deviation between the average prototype value and the corresponding average model value scaled up by  $\lambda_L$ . The permissible maximum deviations are given in the "similarity tolerance" columns of 2.2.2.1.7 and 2.2.2.2.5.



1) Numerical values of similarity tolerances and uniformity tolerances are given in 2.2.2.1.7 and 2.2.2.2.5.

Figure 8 – Procedure for dimensional checks, comparison of results and application of tolerances for model and prototype

#### 2.2.1.3 Procedure

Figure 8 illustrates schematically the application of the geometrical tolerances given by this standard, on individual and average values of model and prototype.

##### a) Checking the uniformity of model and prototype components

By comparing the measurement of individual values with the corresponding average value, it is possible to determine if the uniformity requirement has been met.

If the uniformity requirement is not fulfilled, agreement shall be reached on what components are to be corrected or remanufactured.

In the case where the difference between the average value and the theoretical value is outside the uniformity tolerance, it shall be agreed whether the theoretical value or the geometry of the component shall be corrected.

Where spot-checks are performed, i.e. when not all recurrent components or dimensions are checked, it may be agreed that the individual values are compared directly with the theoretical value.

##### b) Checking the geometric similarity between prototype and model

By comparing the corresponding average values of model and prototype and considering the similarity tolerances as given by this standard, it can be determined whether the geometric similarity requirement has been met. If agreed, the corresponding theoretical values may be substituted for the average values.

If the deviations are greater than the similarity tolerances, further steps shall be agreed which could include a new test with the corrected model.

For some dimensions (e.g. overall dimensions) which are difficult to measure on the model and/or prototype, it may be agreed that, instead of average values of model and/or prototype, theoretical values can be used for comparison, provided that the sum of manufacturing and installation tolerances is less than the similarity tolerance.

#### 2.1.4 Application for different types of machines

For turbines, dimensional tolerances are listed for Francis, Kaplan and Pelton turbines.

The tolerances for Francis turbines apply also to diagonal flow machines with fixed blades.

The tolerances for Kaplan turbines apply also to diagonal flow machines with adjustable blades (Deriaz turbines), and to axial flow machines with fixed or adjustable blades (propeller, tubular, etc.).

The tolerances for Pelton turbines can be adapted to inclined jet impulse turbines.

For pumps and pump-turbines, dimensional tolerances are given for centrifugal, mixed flow and axial machines.

#### 2.1.5 Methods

To measure the shape of runner/impeller blades, guide vanes and stay vanes, several methods are suitable, including three dimensional co-ordinate measuring machines, optical measuring systems, templates, etc.

The inspection for homology of the hydraulic profiles using three dimensional co-ordinate measuring machines or optical systems can be made either by measuring points along curves or by measuring points on the surface:

Curves are essentially the equivalent of mechanical templates and their use and interpretation are similar to the currently prevailing practice using mechanical templates;

Surfaces are represented by a number of measuring points sufficient to define the complete profile positioned either in geometrically similar locations on the prototype and the model or at random. Computer algorithms must be available to adjust the "surface" so that the resulting measured "error" is minimized for the total surface. Such adjustment is however limited by the permissible tolerances shown in 2.2.2.1.7 and 2.2.2.2.5.

Considering the manufacturing and measuring methods of the runner/impeller, the manufacturer shall propose the most appropriate method in agreement with the customer to demonstrate the geometric similarity between prototype and model.

Figures 9 to 19 give examples showing schematically the location and extent of the geometric checking.

In some cases it is not possible to measure the relevant dimension directly, e.g. if a point of intersection is covered by a fillet. In such cases the measurement shall be made in an agreed location.

In order to protect the confidentiality of the manufacturer's hydraulic design, the manufacturer need only submit the differences between the measured and the theoretical profile and not the actual values of the co-ordinates of the profile. For checking purposes, the measured absolute values of profiles are available from the manufacturer.

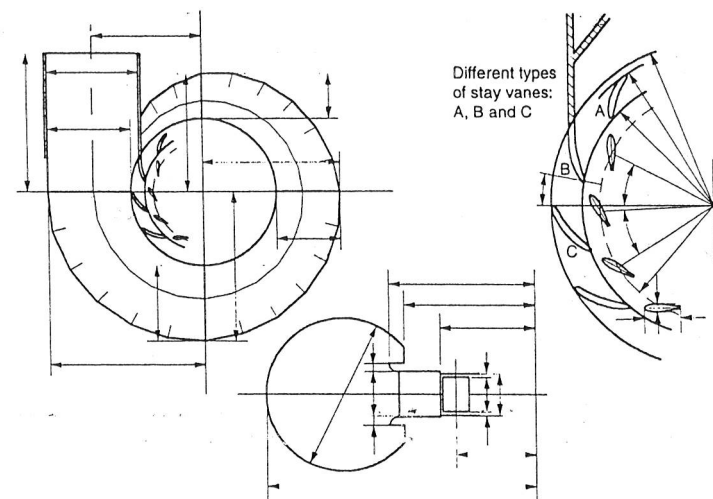


Figure 9 – Example of spiral case and distributor dimensions to be checked

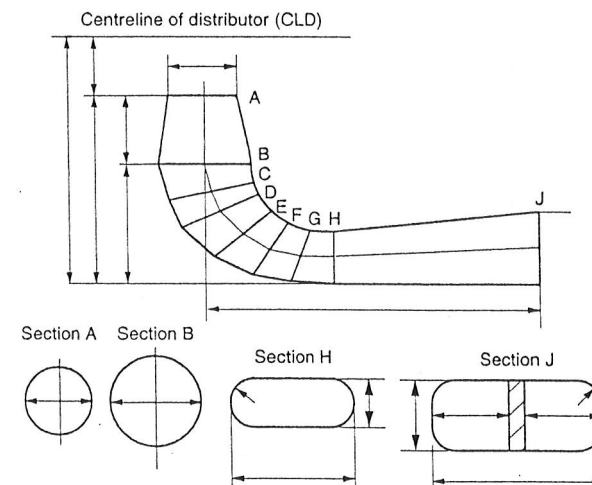


Figure 10 – Example of draft tube dimensions to be checked

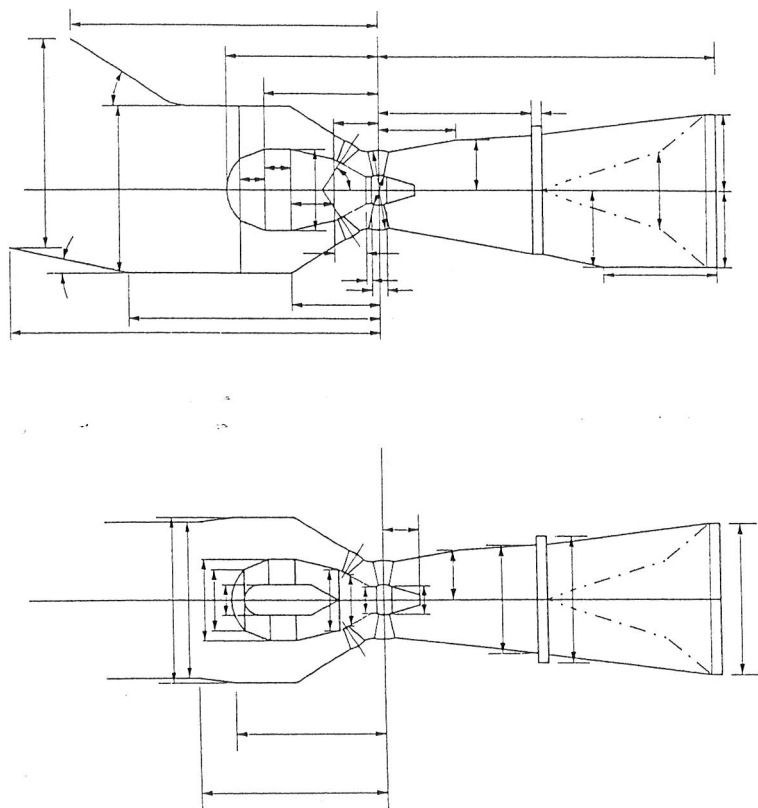


Figure 11 – Example of the dimensions to be checked on a bulb unit

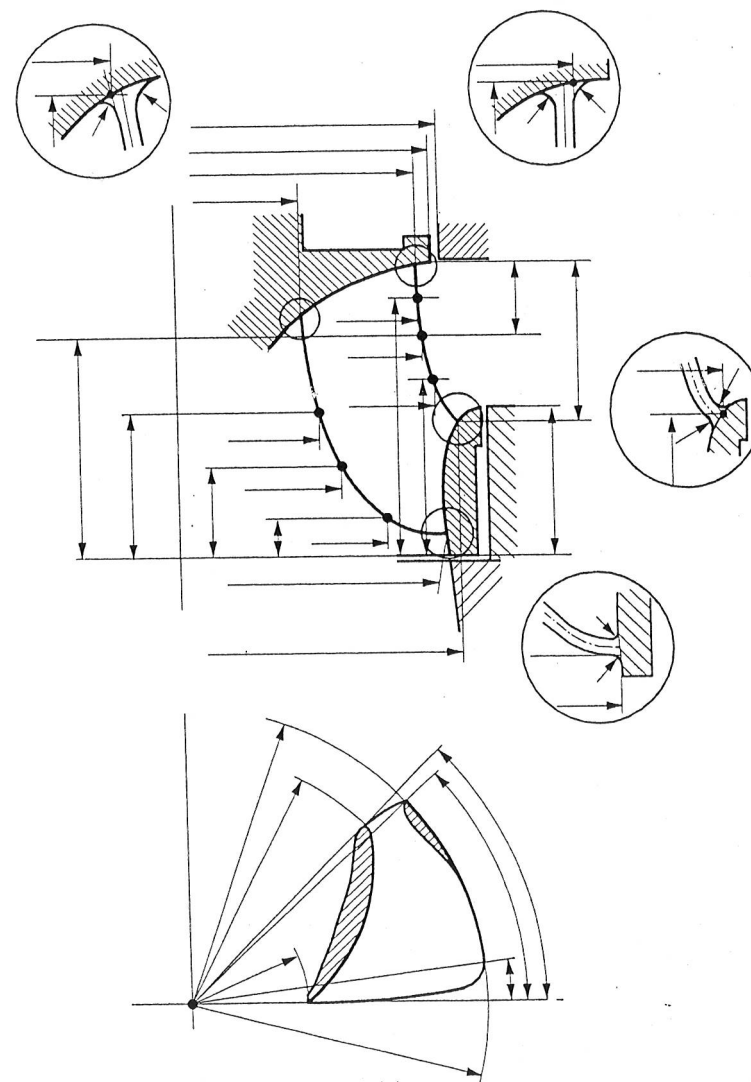
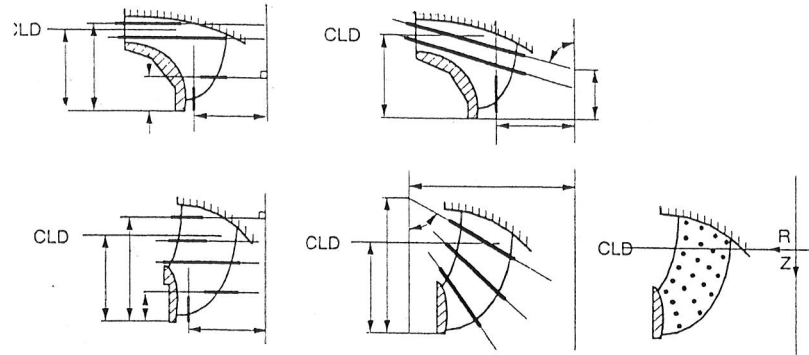


Figure 12 – Example of the dimensions to be checked on the runner/impeller of a radial flow machine



(CLD: Centre line of distributor)

Figure 13 – Runner/impeller of radial flow machine. Examples of locations for blade profile measuring sections or measuring points

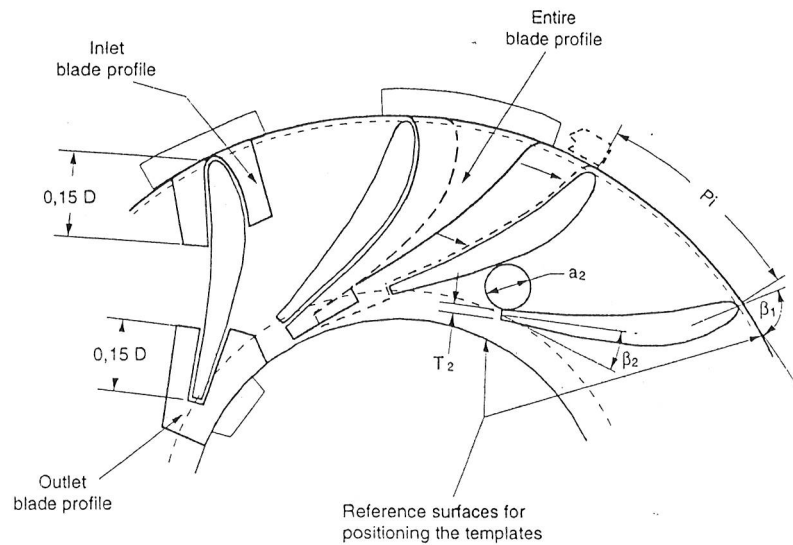


Figure 14 – Runner/impeller of radial flow machine. Check of outlet width and blade profiles by means of templates or co-ordinate system as illustrated on a Francis runner

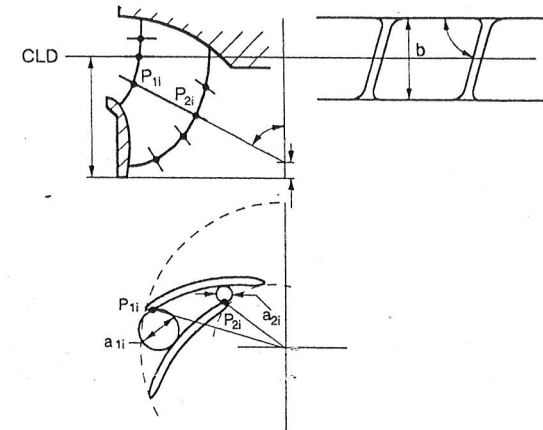


Figure 15 – Runner/impeller of radial flow machine. Check of inlet and outlet widths between blades (example of a pump-turbine runner)

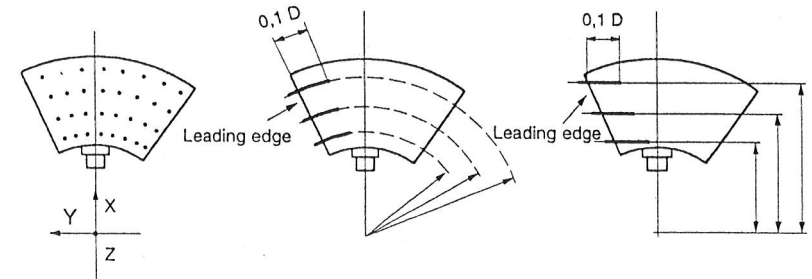


Figure 16 – Runner/impeller of axial flow machine. Example of locations for blade profile measuring sections or measuring points

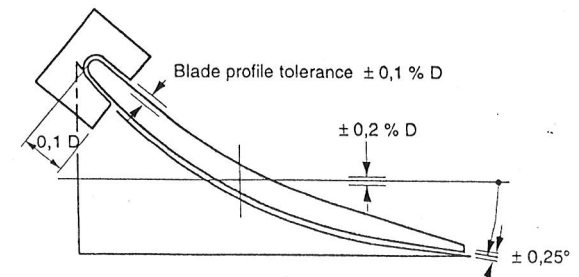


Figure 17 – Runner/impeller of axial flow machine. Definition of blade adjustment and of blade profile tolerances

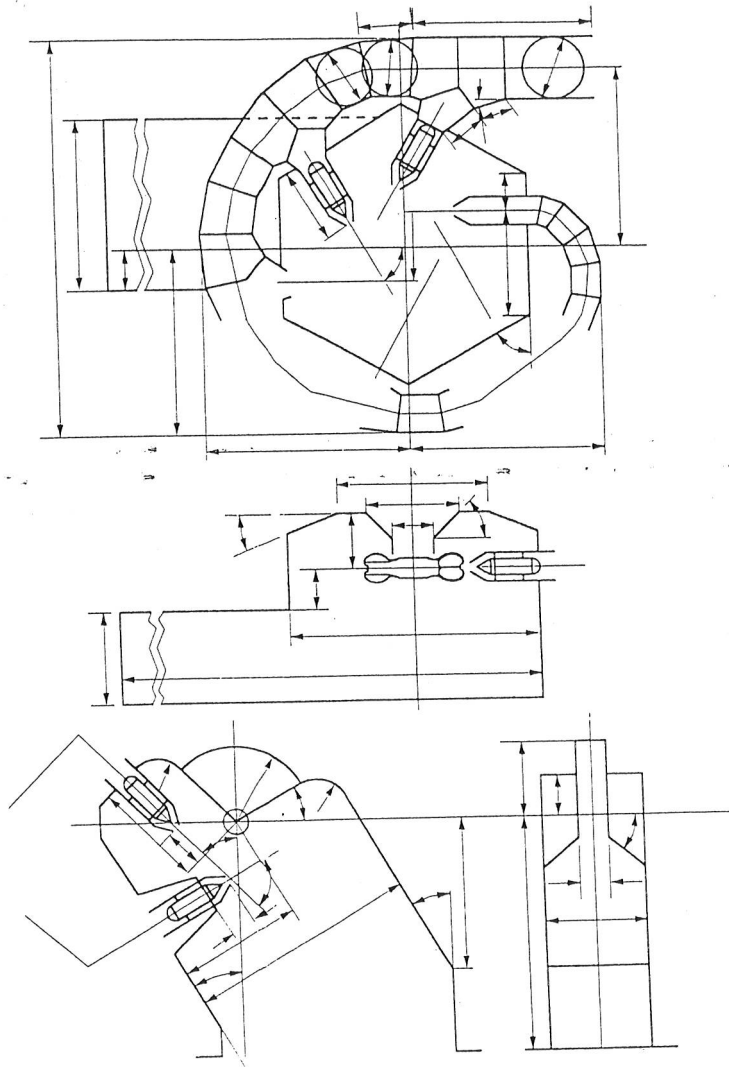


Figure 18 – Pelton turbine: Example of dimensions to be checked on the distributor and the housing of vertical and horizontal shaft machines

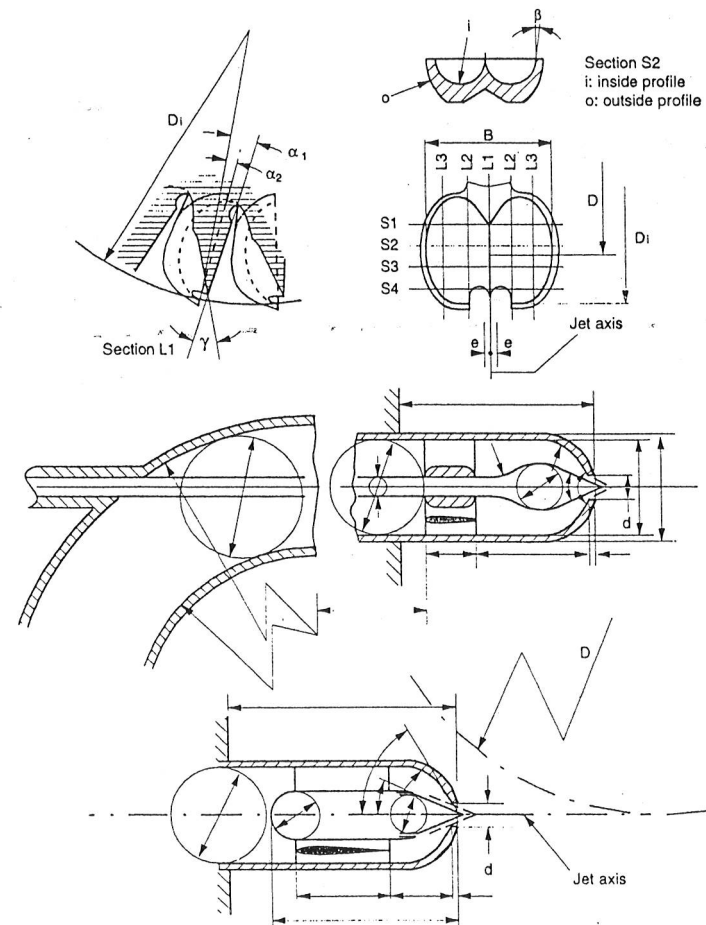


Figure 19 – Pelton turbine: Example of dimensions to be checked on the buckets and nozzles

## 2.2 Dimensions of model and prototype to be checked

a) dimensions of all significant components defining the water passages shall be checked to extent agreeable to the parties concerned.

a) relevant dimensions and their permitted tolerances for turbines, pumps and pump-turbines defined in 2.2.2.1 and 2.2.2.2. When a location is defined by more than one dimension, the tolerance applies to only one dimension.

check of geometric similarity comprises both:

a) a check on the homology of the individual components before assembly. For practical reasons the dimensions shall be referred to the component itself;

a) a check on the homology of the whole machine, i.e. with the components assembled. The relevant overall dimensions are usually referred to the runner axis and/or to the centre line of the distributor. Special attention shall be paid to water passages formed by the transition between adjacent components, stationary or rotating, for which no general value of tolerance can be prescribed in this standard.

a) meridional contour of the runner/impeller shall be checked with templates or by other appropriate measuring techniques, such as three-dimensional co-ordinate measuring machines optical measuring systems.

appropriate checking of the runner/impeller blade profile and its geometric location, the profile angles are properly determined.

the following subclauses 2.2.2.1 and 2.2.2.2 the permissible maximum deviations are either referred to the corresponding scaled model average value or to the following reference dimensions:

maximum thickness of guide vanes, stay vanes or runner blades for each measuring section;

reference diameter (see figure 3);

blade inlet pitch for Francis runners (see figure 14);

nozzle orifice diameter (see figure 19);

maximum inside width of runner bucket (see figure 19);

a<sub>2</sub>) opening between two adjacent blades at high pressure and low pressure side of the runner/impeller (see figures 14 and 15). The opening can be defined either on a blade profile measuring section or as the distance from a given point of the blade edge to the adjacent blade surface.

the terms used in the following subclauses to indicate the various components of hydraulic machines are defined in IEC 61364.

### 2.2.1 Turbines

#### 2.2.1.1 Main components

Reaction turbines:

- the principal dimensions of the spiral casing (or intake in the case of a tubular turbine), the stay ring, the distributor, the draft tube and if necessary the space between runner and head cover (see for example figures 9 and 10);
- the principal dimensions of the runner including inlet and outlet diameters, inlet height, runner band and crown, and hub in case of Kaplan turbine runners;
- the number of runner blades, guide vanes and stay vanes;

- the form of the runner water passages and of the guide and stay vanes, including the maximum thickness of stay vanes, guide vanes and, if applicable, of the runner blades;
- the seal and blade tip clearances of runner and end clearances of guide vanes;
- the roughness of all components of the machine (see 2.2.3.3);
- the waviness of runner blades, guide vanes and stay vanes (usually only relevant for prototype) (see 2.2.3.2).

b) Impulse turbines:

- the principal dimensions of the runner, manifold, housing and nozzles (see figure 18);
- the number of buckets;
- the form of buckets, nozzles and needles (see figure 19);
- the alignment of the jets to the runner;
- the roughness and waviness of the buckets, nozzles and needles (usually only relevant for the prototype).

#### 2.2.2.1.2 Francis turbine runners

- The blade inlet profile shall be checked at least at two sections for low specific speed turbines and at three sections for high specific speed turbines. The inlet section shall extend from the nose of the blade to a distance of 0,15<sup>1)</sup> of the reference diameter along both pressure and suction sides of the blade (see figures 13 and 14 for examples).
- The entire blade profile (from inlet edge to outlet edge) shall be measured, if possible, depending on the runner specific speed, at least for one section or randomly on the whole surface (see figures 13 and 14).
- The blade inlet angles shall be checked at the same sections as for inlet profiles. The inlet angle can be measured, for example, by using a template extending from the nose of the blade to a distance of 0,15<sup>1)</sup> of the reference diameter along both sides of the blade and located to give the best fit to both sides of the blade simultaneously<sup>2)</sup> (see figure 14).
- The blade outlet profiles shall be measured at least at three sections. The outlet section shall extend from the trailing edge of the blade to a distance of 0,15<sup>1)</sup> of the reference diameter back along both sides of the blade (see figure 14).
- The location of the runner leading and trailing edges shall be checked at least at two or three points depending on the specific speed (see figure 12).
- Outlet width between blades shall be checked at least at four points on each blade (see figures 14 and 15).

For fabricated prototype runners (assembled by welding of prefabricated components) it may be agreed that the check of blade profiles can be made prior to assembly, i.e. after having completed machining of the individual blades. After assembly, it is sufficient to check the blade position (e.g. as outlined in figure 12) the fillets and the outlet width.

<sup>1)</sup> This value can be reduced to 0,1 depending on specific speed and profile length.

<sup>2)</sup> Where the blade surface is sufficiently well represented, the independent determination of angles can be omitted (see 2.2.2).

### 2.2.1.3 Kaplan turbine runners

Blade profiles shall be measured at least at three sections along the entire profile (either along cylindrical or plane sections), on both the pressure and suction sides of the blade or randomly on the whole surface (see figure 16).

The nose profile of each of the measured sections shall be checked. The nose profile shall extend from the nose of the blade to a distance 0,1 D along the blade. In making these checks, the best fit between blade and each reference profile may be obtained by rotating the reference profile, provided the angular and axial adjustment do not exceed the values defined in 2.2.2.1.7 compared with the correct location of the reference profile. These adjustments shall be allowed only once for each section and all check measurements shall be made in this position on both the pressure side and the suction side of the section considered (see figure 17).

With the blades mounted in the hub, the inclination of the blades with respect to each other shall be checked. For this purpose, the inclination of the outer measured profiles shall be compared. The difference of recorded blade angles shall not exceed  $\pm 0,25^\circ$ .

### 2.2.1.4 Pelton turbine runners

The profile of each bucket shall be checked at least at four transverse and four longitudinal sections or randomly on the whole surface (see figure 19).

The discharge angle  $\beta$  of each bucket shall be checked at four points on each side (see figure 19).

The form of the cutout, the angle  $\gamma$  of the back of the cutout, the splitter edge and the bucket inclination  $\alpha$  shall be checked on each bucket (see figure 19).

The bucket inside width and profile shall be checked.

The bucket outside profile shall also be checked to ensure that the interference between the jet and the bucket on the prototype is always less than that on the model, the tolerances of the outside profile (see 2.2.2.1.7) shall be applied to the bucket discharge area which can influence this interference.

### 2.2.1.5 Guide vanes

For a cylindrical distributor arrangement, the profile shall be measured at least at one section and, for conical arrangements, at least at two sections.

### 2.2.1.6 Clearances

For runner/impeller seal clearances, blade tip clearances and guide vane-end clearances on action turbines shall be checked.

For prototype clearances shall not exceed the scaled model clearances.

The possible influence of the pressure on the guide vane end clearance should be considered for model and prototype.

The extension (length) of the prototype runner/impeller seals shall not be smaller than that of the scaled model.

### 2.2.2.1.7 Permissible maximum deviations in geometrical similarity between prototype and model turbines

	Permissible maximum deviation		
	Uniformity tolerance		Similarity tolerance
	Model	Prototype	Prototype/Model
	Individual value to average value	Individual value to average value	Prototype average value to scaled model average value ( $L_p \cdot \lambda_L \cdot L_M$ ) / (reference value) <sup>1)</sup>
<b>Principal dimensions of hydraulic passages</b>			
Metallic or concrete passages (casing, draft tube, etc.) <sup>2)</sup>	$\pm 2 \%$	$\pm 2 \%$	$\pm 1 \%$
Stay ring diameters	$\pm 1 \%$	$\pm 1 \%$	$\pm 1 \%$
Length of stay vanes	$\pm 2 \%$	$\pm 2 \%$	$\pm 2 \%$
Maximum thickness of guide vanes T'	$\pm 5 \%$	$\pm 5 \%$	$\pm 5 \%$
Maximum thickness of stay vanes T*	$\pm 5 \%$	$\pm 8 \%$	$\pm 5 \%$
Stay ring height	$\pm 2 \%$	$\pm 2 \%$	$\pm 2 \%$
Distributor height	$\pm 0,3 \%$	$\pm 0,3 \%$	$\pm 0,2 \%$
Guide vane pitch circle diameter	$\pm 0,2 \%$	$\pm 0,2 \%$	$\pm 0,2 \%$
Relative position between stay vanes and guide vanes (for example expressed as an angle)	$\pm 1^\circ$	$\pm 1^\circ$	$\pm 1^\circ$
Guide vane profile	$\pm 3 \%$ T'	$\pm 5 \%$ T'	$\pm 3 \%$ T'
Stay vane profile	$\pm 3 \%$ T*	$\pm 8 \%$ T*	$\pm 5 \%$ T*
Maximum guide vane opening	$\pm 1,5 \%$	$\pm 2 \%$	$\geq 0$
<b>Clearances</b>			
Seal and blade tip clearance	$\pm 50 \%$	$\pm 50 \%$	$\leq 0$
Seal clearance length	-	-	$\geq 0$
Guide vane end clearances	$\pm 50 \%$	$\pm 50 \%$	$\leq 0$
<b>Francis runners</b>			
Blade profile:			
inlet and outlet edges	$\pm 0,1 \%$ D	$\pm 0,1 \%$ D	$\pm 0,1 \%$ D
remaining part of the surface	$\pm 0,2 \%$ D	$\pm 0,2 \%$ D	$\pm 0,2 \%$ D
Inlet pitch $P_1$	$\pm 0,2 \%$ D	$\pm 0,5 \%$ D	-
Inlet angle $\beta_1$ <sup>3)</sup>	$\pm 1,5^\circ$	$\pm 2^\circ$	$\pm 1,5^\circ$
Outlet angle $\beta_2$ <sup>3)</sup>	$\pm 1^\circ$	$\pm 1,5^\circ$	$\pm 1^\circ$
Outlet opening a	$\pm 3 \%$	$\pm 5 \%$	$\pm 3 \%$
Maximum blade thickness T <sup>4)</sup>	$\pm 3 \%$	$\pm 5 \%$	$\pm 3 \%$
Blade thickness near the outlet edge	$\pm 6 \%$	$\pm 8 \%$	$\pm 6 \%$
Inlet and outlet diameter and other runner dimensions <sup>5)</sup>	$\pm 15 \%$	$\pm 15 \%$	$\pm 15 \%$
	$\pm 0,25 \%$ D	$\pm 0,5 \%$ D	$\pm 0,25 \%$ D

<sup>1)</sup> The reference value is taken to be the scaled model average value ( $\lambda_L \cdot L_M$ ) unless otherwise indicated. Angular tolerance is the difference between prototype and model angles.

<sup>2)</sup> For concrete surfaces, uniformity tolerances should be progressively changed from  $\pm 2 \%$  to  $\pm 1 \%$  on machines with prototype runner diameter between 3 m and 1 m. Also for concrete surfaces, abrupt changes resulting from shifting formwork, interface between concrete and metallic surfaces, etc., should be limited to 6 mm on prototype machines greater than 3 m runner diameter and progressively decreasing to 3 mm for machines between 3 m and 1 m runner diameter.

<sup>3)</sup> Where the blade surface is sufficiently well represented, the independent determination of angles can be omitted (see 2.2.2).

<sup>4)</sup> Not required if complete profile data are provided.

<sup>5)</sup> In certain cases, it may be appropriate to agree upon increased tolerances for the trailing edge dimensions (e.g. some radii shown in figure 12) while maintaining the required tolerances for outlet width.

	Permissible maximum deviation		
	Uniformity tolerance		Similarity tolerance
	Model	Prototype	Prototype/Model
	Individual value to average value	Individual value to average value	Prototype average value to scaled model average value $(L_P \cdot \lambda_L L_M) / (\text{reference value})^1$
<b>axial and diagonal flow runners</b>			
blade profile	$\pm 0,1 \% D$	$\pm 0,1 \% D$	$\pm 0,1 \% D$
case profile	$\pm 0,1 \% D$	$\pm 0,1 \% D$	$\pm 0,1 \% D$
maximum blade thickness <sup>2) T</sup>	+3 % -6 %	+5 % -8 %	+3 % -6 %
blade thickness near the outlet edge	$\pm 15 \%$	$\pm 15 \%$	$\pm 15 \%$
discharge ring diameter D	$\pm 0,1 \%$	$\pm 0,1 \%$	$\pm 0,2 \%$
other runner dimensions	$\pm 0,25 \% D$	$\pm 0,5 \% D$	$\pm 0,25 \% D$
angular difference of the profile	$\pm 0,25^\circ$	$\pm 0,25^\circ$	$\pm 0,25^\circ$
axial adjustment of the profile	$\pm 0,2 \% D$	$\pm 0,2 \% D$	$\pm 0,2 \% D$
maximum blade angle	$\pm 0,25^\circ$	$\pm 0,25^\circ$	$\geq 0^\circ$
<b>centrifugal turbines</b>			
leading and nozzle diameter	$\pm 0,3 \% d$	$\pm 0,3 \% d$	$\pm 0,3 \% d$
leading and nozzle profile	$\pm 0,1 \% d$	$\pm 0,1 \% d$	$\pm 0,1 \% d$
nozzle angle	$\pm 0,5^\circ$	$\pm 1^\circ$	$\pm 1^\circ$
leading angle	$\pm 1^\circ$	$\pm 2^\circ$	$\pm 1^\circ$
bucket inside width B	$\pm 0,3 \%$	+0,8 % -0,5 %	+0,8 % -0,5 %
bucket outside profile	$\pm 0,5 \% B$	+1 % -0,8 %	+1 % -0,8 %
bucket inside profile	$\pm 0,5 \% B$	$\pm 0,5 \% B$	$\pm 0,5 \% B$
bucket inclination $\alpha$	$\pm 1^\circ$	$\pm 1^\circ$	$\pm 1^\circ$
bucket discharge angle $\beta$	$\pm 1^\circ$	$\pm 1^\circ$	$\pm 1^\circ$
cut-out profile	$\pm 1 \% B$	$\pm 1 \% B$	$\pm 1 \% B$
angle $\gamma$ of face at the back of cut-out	$\pm 1^\circ$	0 ° -3 °	0 ° -3 °
jet circle diameter D	$\pm 0,2 \%$	$\pm 0,2 \%$	$\pm 0,2 \%$
Offset of jet to runner e	$\pm 0,5 \% B$	$\pm 0,5 \% B$	$\pm 0,25 \% B$
Alignment of jet to runner $\delta$	$\pm 0,5^\circ$	$\pm 0,5^\circ$	$\pm 0,5^\circ$
bucket pitch at outer diameter	$\pm 1 \% B$	$\pm 1,5 \% B$	-
Diameter $D_i$ (figure 18)	$\pm 0,3 \% D$	$\pm 0,3 \% D$	$\pm 0,2 \% D$

<sup>1)</sup> The reference value is taken to be the scaled model average value ( $\lambda_L L_M$ ), unless otherwise indicated. Angular tolerance is the difference between and model angles.

<sup>2)</sup> Not required if complete profile data are provided.

## 2.2.2.2 Pumps and pump-turbines

### 2.2.2.2.1 Main components

As a minimum, the following parts shall be checked to show compliance with tolerances stated:

- the principal dimensions of the casing, diffuser, suction pipe and space between impeller/runner and head cover when necessary (figures 9 and 10);
- the principal dimensions of the impeller/runner including inlet and outlet diameters<sup>1)</sup>, outlet height, impeller/runner band and crown (figures 12 and 15);
- the number of impeller/runner blades, diffuser vanes/guide vanes and stay vanes;
- the form of the impeller/runner water passages and of the diffuser vanes/guide vanes and stay vanes, including the maximum thickness of stay vanes, diffuser vanes and impeller/runner blades;
- the seal and blade tip clearances of the impeller/runner and end clearances of guide vanes, if any;
- the roughness of all components of the machine (see 2.2.3.3);
- the waviness of diffuser vanes, guide vanes if any, and impeller/runner blades (usually only relevant for the prototype).

### 2.2.2.2.2 Centrifugal and mixed-flow impellers/runners

The requirements for centrifugal and mixed-flow impellers/runners are, for convenience, expressed in terms of a single-flow single-stage machine. For double-flow and multi-stage machines, additional measurements shall be taken of all inlets and stages.

- Blade inlet profiles shall be measured at least at three sections. The inlet section shall extend from the nose of the blade to a distance of 0,15<sup>2)</sup> of the reference diameter D for both sides along the blade (see figure 14).
- Blade outlet profiles shall be checked at least at two sections for low specific speed machines and at three sections for high specific speed machines. The outlet section shall extend from the trailing edge of the blade to a distance of 0,15<sup>2)</sup> of the reference diameter back along both pressure and suction sides of the blade (see figures 13 and 14).
- Entire blade profile (from inlet edge to outlet edge) shall be measured at least for one section, if possible, depending on the impeller/runner specific speed or randomly on the whole surface (see figures 13 and 14).
- Blade inlet angles shall be checked at the same sections as for inlet profiles. The inlet angle can be measured, for example, by using a template extending from the leading edge of the blade to a distance of 0,15<sup>2)</sup> of the reference diameter along the blade and located to give the best fit to both sides of the blade simultaneously<sup>3)</sup>.
- The location of the impeller/runner inlet and outlet edges shall be checked at two or three points depending on the specific speed (see figure 12).
- Inlet width between blades shall be checked at least at four points on each blade (see figure 15).
- For the outlet section of the impeller/runner, the following procedure is recommended (see figures 13 and 15):

<sup>1)</sup> "Inlet/Outlet" for pump-turbines refers to pump mode.

<sup>2)</sup> This value can be reduced to 0,1 depending on specific speed and profile length.

<sup>3)</sup> Where the blade surface is sufficiently well-represented, the independent determination of angles can be omitted (see 2.2.2).

- 1) measurement of blade outlet profiles at two or more sections depending on specific speed;
- 2) measurement of the heights (b) between shrouds of the individual blade passages for impeller/runner;
- 3) determination of the outlet width (a) where the maximum inscribed circle is tangential to the pressure and suction faces at the outlet.

For fabricated prototype runners (assembled by welding of prefabricated components) it may be agreed that the check of blade profiles can be made prior to assembly, i.e. after having completed machining of the individual blades. After assembly it is sufficient to check the blade position, (e.g. as outlined in figure 12), the fillets and inlet width.

### 2.2.2.3 Axial flow impellers /runners

Blade profiles shall be checked using the same procedure given in 2.2.2.1.3 for Kaplan turbine runners.

### 2.2.2.4 Guide vanes and clearances

For guide vane profiles and clearances, see 2.2.2.1.5 and 2.2.2.1.6.

### 2.2.2.2.5 Permissible maximum deviations in geometrical similarity between prototype and model pumps/pump-turbines

	Permissible maximum deviation		
	Uniformity tolerance		Similarity tolerance
	Model	Prototype	Prototype/Model
	Individual value to average value	Individual value to average value	Prototype average value to scaled model average value ( $L_p/L_M$ )(reference value) <sup>1)</sup>
<b>Principal dimensions of hydraulic passages</b>			
Metallic or concrete passages (casing, draft tube, etc.)	±2 %	±2 %	±1 %
Stay ring diameters	±1 %	±1 %	±1 %
Length of diffuser vanes/stay vanes	±2 %	±2 %	±2 %
Maximum thickness of guide vanes T'	±5 %	±5 %	±5 %
Maximum thickness of stay vanes T*	±5 %	±8 %	±5 %
Stay ring/diffuser height	±2 %	±2 %	±2 %
Distributor height	±0,3 %	±0,3 %	±0,2 %
Guide vane pitch circle diameter	±0,2 %	±0,2 %	±0,2 %
Relative position between stay vanes and guide vanes (for example expressed as an angle)	±1°	±1°	±1°
Guide vane/stay vane/diffuser profile	±3 % T	±5 % T	±3 % T
Maximum guide vane opening	±1,5 %	±2 %	≥0
<b>Clearances</b>			
Seal and blade tip clearance	±50 %	±50 %	≤0
Seal clearance length	-	-	≥0
Guide vane end clearances	±50 %	±50 %	≤0
<b>Radial impellers/runners<sup>2)</sup></b>			
Blade profile:			
inlet and outlet edges	±0,1 % D	±0,1 % D	±0,1 % D
remaining part of the surface	±0,2 % D	±0,2 % D	±0,2 % D
Inlet pitch P <sub>i</sub>	±0,2 % D	±0,5 % D	-
Inlet angle β <sub>2</sub> <sup>3)</sup>	±1,5°	±1,5°	±1°
Outlet angle β <sub>1</sub>	±1°	±1,5°	±1°
Inlet and outlet width a	±3 %	+5 % -3 %	+3 % -1 %
Maximum blade thickness T <sup>4)</sup>	+3 % -6 %	+5 % -8 %	+3 % -6 %
Blade thickness near the outlet edge	±15 %	±15 %	±15 %
Inlet and outlet diameters and other impeller/runner dimensions	±0,25 % D	±0,5 % D	±0,25 % D
<sup>1)</sup> The reference value is taken to be the scaled model average value ( $L_p/L_M$ ) unless otherwise indicated. Angular tolerance is the difference between prototype and model angles. <sup>2)</sup> "Inlet/outlet" for pump-turbines refers to pump mode. <sup>3)</sup> Where the blade surface is sufficiently well represented, the independent determination of angles can be omitted (see 2.2.2). <sup>4)</sup> Not required if complete profile data are provided.			

	Permissible maximum deviation		
	Uniformity tolerance		Similarity tolerance
	Model	Prototype	Prototype/Model
	Individual value to average value	Individual value to average value	Prototype average value to scaled model average value to reference value $(L_P \cdot \lambda_L L_M) / (\text{reference value})^1$
axial flow impellers/runners			
blade profile	$\pm 0,1 \% D$	$\pm 0,1 \% D$	$\pm 0,1 \% D$
case profile	$\pm 0,1 \% D$	$\pm 0,1 \% D$	$\pm 0,1 \% D$
maximum blade thickness $T^2$	$+3$ $-6$ %	$+5$ $-8$ %	$+3$ $-6$ %
blade thickness near the outlet edge	$\pm 15$ %	$\pm 15$ %	$\pm 15$ %
discharge ring diameter $D$	$\pm 0,1 \% D$	$\pm 0,1 \% D$	$\pm 0,2 \% D$
other runner dimensions	$\pm 0,25 \% D$	$\pm 0,5 \% D$	$\pm 0,25 \% D$
angular difference of the profile	$\pm 0,25^\circ$	$\pm 0,25^\circ$	$\pm 0,25^\circ$
axial adjustment of the profile	$\pm 0,2 \% D$	$\pm 0,2 \% D$	$\pm 0,2 \% D$
maximum blade angle	$\pm 0,25^\circ$	$\pm 0,25^\circ$	$\geq 0^\circ$

1) The reference value is taken to be the scaled model average value  $(\lambda_L L_M)$  unless otherwise indicated. Angular tolerances are the difference between prototype and model angles.

2) Not required if complete profile data are provided.

## 2.3 Surface waviness and roughness

### 2.3.1 Definitions

#### 2.3.1.1 Waviness

Waviness is the deviation of a surface profile from a smooth curve to which a flexible stick could readily conform. Waviness is expressed as the ratio of maximum deviation to distance over which the deviation from the smooth curve occurs. This is the ratio  $X/U$  of figure 20. In order to distinguish waviness from surface roughness,  $U$  should be not less than 50 mm. The point of maximum deviation  $X$  should be in the middle third of  $U$ .

It should be noted that bumps on the surface are sometimes more difficult to assess than hollows. However, bumps are relatively easier to correct.

#### 2.3.1.2 Surface roughness

Surface roughness is the characteristic quality of the surface due to small departures from its general form such as those produced by the cutting action of tool edges, abrasive grains, feed marks from the machine, coating and painting or originally produced by the fabrication (welding) process.

It is characterized by the roughness criterion  $R_a$  (arithmetical mean deviation from the mean line of the profile) as defined in ISO 468.

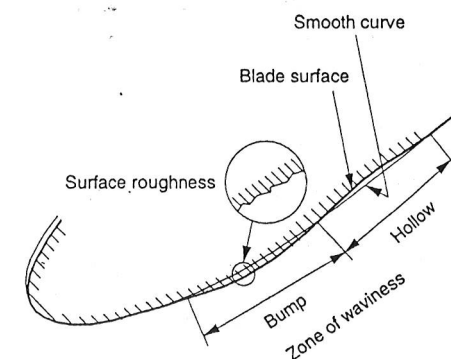
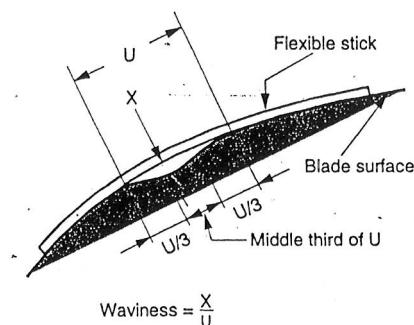


Figure 20 – Definition of waviness and surface roughness

#### 2.2.3.2 Waviness requirements

The whole surface of the blades, including the defined profile sections and the runner/impeller crown and band shall be checked to establish that profiles are smooth continuous curves with a waviness of less than  $\pm 0,02$ . A flexible stick may be used for this purpose.

On surfaces subject to cavitation, the waviness shall be less than  $\pm 0,01$ .

#### 2.2.3.3 Prototype roughness requirements

Rough surfaces in the water passages of both model and prototype machines reduce the efficiency below the value which is potentially obtainable.

The model should be such that a hydraulically smooth flow (see [2], annex P) is achieved, even if it is not normally the case in the most significant prototype components. It is conventionally agreed to apply the efficiency scale-up formulae described in 3.8 despite the fact that these formulae are valid only for hydraulically smooth flows.

ie prototype roughness shall be specified taking into account the economic value of efficiency, the cost of manufacture, the size of the machine, the likelihood of quick damage of a initial surface finish due to erosion or corrosion during on site operation, etc.

ible 1 indicates guidance values of prototype surface roughness.

bject to the above considerations, the recommendations for surface roughness values are lit into two groups. The boundary of these groups, in terms of specific hydraulic energy  $E$ , is ven in table 1 for various types of machines, corresponding approximately to machines with ver to medium specific speed (medium to high head machines) and to machines with higher ecific speed (low head machines).

ie values of prototype surface roughness are valid for the finished condition of the surface. is means that if the hydraulic wetted components have painted or coated surfaces, this ndition shall be checked.

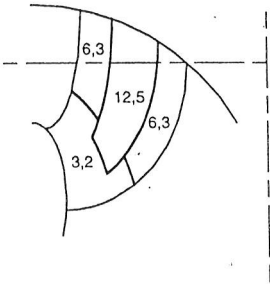
oreover, the finish required may be chosen at some locations to improve cavitation resistance for fatigue reasons; then the choice of finish is not related to model-to-prototype dimensional milarity.

determining the surface roughness of fabricated components in the inlet and outlet structure, iral case, draft tube cone and inlet chamber of tubular turbines, the welds, due to their small rtion of the whole surface area, are not to be included in the surface checking. However, this ssumes that the welds are clean without contour edges. This also means that for machines th lower heads (left hand column in table 1), those welds need not be ground.

Table 1 – Recommended prototype surface roughness  $R_a$   
(finished surfaces, eventual painting included)

Type of machine		Component	$R_a$ $\mu m$	
Reaction machine	Axial	Runner/impeller blades Guide and diffuser vanes Spiral case, stay ring, discharge ring, draft tube cone and tubular machine intake	$E < 300 \text{ J}\cdot\text{kg}^{-1}$	$E > 300 \text{ J}\cdot\text{kg}^{-1}$
			$\leq 6,3$ $\leq 12,5$ $\leq 25,0$	$\leq 3,2$ $\leq 6,3$ $\leq 12,5$
	Radial or diagonal	Runner/impeller blades Guide and diffuser vanes Spiral case, stay ring (including return vanes for multi-stage machines), facing plates and draft tube cone	$E < 2\,000 \text{ J}\cdot\text{kg}^{-1}$	$E > 2\,000 \text{ J}\cdot\text{kg}^{-1}$
			$\leq 6,3$ $\leq 12,5$ $\leq 25,0$	$\leq 3,2$ $\leq 6,3$ $\leq 12,5$
Pelton turbine		Inside of buckets and exit of nozzle Nozzle Manifold	$E < 5\,000 \text{ J}\cdot\text{kg}^{-1}$	$E > 5\,000 \text{ J}\cdot\text{kg}^{-1}$
			$\leq 3,2$ $\leq 12,5$ $\leq 25,0$	$\leq 1,6$ $\leq 6,3$ $\leq 12,5$

NOTE – The values given are average values for the total surface of the component involved. Due to local hydraulic conditions, deviations up to  $\pm 1$  class of  $R_a$  may be accepted in certain areas (for instance, from  $R_a = 3,2 \mu m$  to  $R_a = 12,5 \mu m$  instead of the recommended mean value  $R_a = 6,3 \mu m$  for the runner blades of a radial turbine, see sketch).



## Hydraulic similitude, test conditions and test procedures

### 1 Hydraulic similitude

#### 1.1 Theoretical basic requirements and similitude numbers

heory, to achieve hydrodynamic similitude between two hydraulic turbomachines A and B (where A can stand for model and B for prototype) the following conditions should be met:

geometrical similitude between machines A and B;

identical ratios of the various forces, acting between the fluid and the components of each machine.

These ratios are defined by dimensionless terms and are identified by similitude numbers.

In the context of this standard, the major similitude numbers are summarized in table 2:

Table 2 – Similitude numbers

Similitude number (symbol)	Ratio of forces	General definition	Definition used in this standard
Reynolds (Re)	$\frac{\text{inertia}}{\text{viscosity}}$	$\frac{v_c \cdot L_c}{\nu}$	See 1.3.3.11.1
Euler (Eu)	$\frac{\text{pressure}}{\text{inertia}}$	$\frac{\Delta p_c}{\rho \cdot v_c^2}$	See 1.3.3.11.4
Thoma ( $\sigma$ )		$\frac{NPSE}{E}$	See 1.3.3.6.6
Froude (Fr)	$\frac{\text{inertia}}{\text{gravity}}$	$\frac{v_c}{(g \cdot L_c)^{1/2}}$	See 1.3.3.11.2
Weber (We)	$\frac{\text{inertia}}{\text{surface tension}}$	$\frac{\rho \cdot L_c \cdot v_c^2}{\sigma}$	See 1.3.3.11.3 (identical to general definition)

$L_c$  is the characteristic length;  
 $v_c$  is the characteristic velocity;  
 $\Delta p_c$  is the characteristic differential pressure;  
 $\sigma$  is the surface tension of fluid.

Usually, it is impossible to choose the test conditions to satisfy the various similitude numbers simultaneously. Therefore, the similitude condition to be considered should be the one with the greatest influence on the results.

In most model tests, it is not possible to achieve the corresponding prototype similitude number. Therefore, corrections have to be applied to the model results when they are transformed to prototype conditions. Such corrections will also be required if the Reynolds number for model performance data is different from a specified Reynolds number.

#### 2.3.1.2 Conditions for hydraulic similitude as used in this standard

From the above basic requirements, it can be derived that two machines A and B are operated under hydraulically similar operating conditions if the following conditions are met:

- the requirements of geometric similarity between A and B stipulated in 2.1.3.4 and in 2.2 are fulfilled;
- the ratios of corresponding flow velocity components at any homologous point of both machines are identical, making the corresponding velocity triangles at the runner/impeller (defined by the absolute, circumferential and relative velocity components) geometrically similar.

As a consequence, both machines have, at corresponding operating points, identical discharge, energy and cavitation coefficients (see 1.3.3.12):

$$\text{same discharge coefficient} \quad (Q_{nD})_A = (Q_{nD})_B$$

$$\text{and same energy coefficient} \quad (E_{nD})_A = (E_{nD})_B$$

$$\text{and same cavitation coefficient} \quad (\sigma_{nD})_A = (\sigma_{nD})_B$$

or identical discharge and speed factors and Thoma number (see 1.3.3.12):

$$\text{same discharge factor} \quad (Q_{ED})_A = (Q_{ED})_B$$

$$\text{and same speed factor} \quad (n_{ED})_A = (n_{ED})_B$$

$$\text{and same Thoma number} \quad \sigma_A = \sigma_B$$

The equality of these coefficients and factors characterizes the hydraulic similitude of both machines. This is important with respect to "hydraulic" characteristics and/or data which are guaranteed or specified according to 1.4.

Other similitude conditions which are important for "mechanical" aspects (e.g. hydroelasticity etc.) are not covered by this standard.

#### 2.3.1.3 Similitude requirements for various types of model tests

Table 3 gives an overview of similitude conditions which should be observed when performing tests on a model whose results are related to a prototype machine.

Independent of the type of test, as a minimum, the similitude conditions for discharge, specific hydraulic energy or speed and cavitation (if a cavitation influence is expected) shall be fulfilled according to 2.3.1.2 b), in order to achieve hydraulic similitude between model and prototype.

The following subclauses 2.3.1.4, 2.3.1.5 and 2.3.1.6 give detailed information on the influence of the various similitude conditions covered by this standard.

Table 3 – Similitude requirements for various types of model tests

Reaction machines	
Type of test	Similitude conditions to be observed and comments
<i>Performance test</i>	<p>The possible influence of cavitation on discharge, specific hydraulic energy, efficiency and power shall be checked by cavitation tests (<math>\sigma</math>-variations) at selected operating points, independent of the agreement to perform these tests at <math>\sigma_M = \sigma_{pl}</math> or <math>\sigma_M &gt; \sigma_{pl}</math>.</p> <p>Efficiency, power:</p> <p>The influence of Re shall be considered within the guarantee range (see 2.3.1.4.1). Because usually <math>Re_M &lt; Re_P</math>, corrections have to be applied for efficiency and power: see 3.8.2.4.</p> <p>Discharge, specific hydraulic energy:</p> <p>It is assumed that Re and Fr have no influence.</p>
<i>Cavitation test</i>	The influence of Fr, Re and water quality (see 2.3.1.6) shall be considered. If $Fr_M \neq Fr_P$ then at least $\sigma_M = \sigma_{pl}$ shall be observed (see 2.3.1.5). See note.
<i>Runaway test</i>	It is assumed that Re and Fr have no influence. The influence of cavitation shall be considered
<i>Four-quadrant and additional tests</i>	It is assumed that Re and Fr have no influence. In some cases cavitation influence shall be checked in certain ranges of operation
Impulse turbines	
Type of test	Similitude conditions to be observed and comments
<i>Performance test</i>	<p>It is recommended that Fr similitude be respected for performance tests (see 2.3.1.5.2).</p> <p>Efficiency, power:</p> <p>The influences of Fr, We and Re are considered according to 3.8.2.4 and annex K</p> <p>Discharge, specific hydraulic energy:</p> <p>It is assumed that Fr, We and Re have no influence</p>
<i>Cavitation test</i>	Usually not performed
<i>Runaway test</i>	It is assumed that only Fr similitude shall be respected
<i>Additional tests</i>	It is assumed that Fr, We, Re and cavitation have no influence
NOTE – It is assumed that there is a lower limit for $\sigma$ below which the influence of the Reynolds number on performance need no longer be considered, because the influence of two-phase flow is dominant (see 3.8.2.4.2).	

## 2.3.1.4 Reynolds similitude

## 2.3.1.4.1 Reaction machines

Friction losses are mainly dependent on the Reynolds number provided that flow conditions are hydraulically smooth. Because the Reynolds number of the model, referred to the reference diameter of the machine (or to a characteristic length of a component) is usually smaller than that of the prototype, the ratio of friction losses to total losses for the model becomes larger than the corresponding ratio for the prototype. Therefore, in most cases, model efficiency is somewhat lower than prototype efficiency.

As a consequence, within the guarantee range, where the ratio of friction losses to total losses is important, model efficiencies and power factors or coefficients shall be corrected when they are referred to a Reynolds number different from that experienced during testing, for example if model results are scaled up to prototype conditions (see 3.8).

The influence of the Reynolds number is not considered:

- in the range of guaranteed efficiencies, if the influence of cavitation effects a drop of more than 0,5 % of efficiency (see 3.8.2.4.2);
- outside the range of guarantee, i.e. at extreme off-design operation, where the ratio of friction losses to total losses becomes small. This is, for example, the case for
  - runaway conditions;
  - shut off conditions of a pump;
  - four-quadrant operation of a pump-turbine (except within the guaranteed operating range).

## 2.3.1.4.2 Impulse turbines

The influence of the Reynolds number on hydraulic efficiency is considered according to annex K and 3.8.2.4.

## 2.3.1.5 Froude similitude and cavitation tests

Froude similitude should be respected mainly for model tests conducted under the following operating conditions:

- two-phase flow (e.g. large zones of cavitation on runner impeller blades, draft tube vortices, or in the housing of a Pelton turbine with water discharging and splashing in air);
- flow with a free surface (e.g. pump inlets with the possibility of free vortices).

The influence of the Froude number could be especially important for impulse turbines and reaction machines of low specific hydraulic energy, when performance at plant conditions becomes influenced by cavitating flow attached to runner/impeller blades or which appears as vortex cavities in a turbine draft tube.

For cavitation tests, the application of Froude similitude should be considered only when the vertical distance between the highest and lowest points of the full size runner/impeller blades becomes significant in relation to the plant turbine/pump head. This can be the case for large horizontal axis machines operating at low specific hydraulic energy.

### 1.5.1 Cavitation tests on reaction machines

Cavitation reference level  $z_c$

The cavitation reference level  $z_c$  shall be chosen to correspond to the location where the relevant cavitation occurs. This may result in the cavitation reference level  $z_c$  (see 1.3.3.7.7) deviating from the machine reference level  $z_r$ , as defined in 1.3.3.7.6, because the location with maximum cavitation is not necessarily at elevation  $z_r$ . The geometrical relation between  $z_r$ , which defines the setting of the machine, and  $z_c$  is illustrated by figure 21, and the relation between the corresponding  $\sigma$ -values is given by the following formula which applies to both model and prototype.

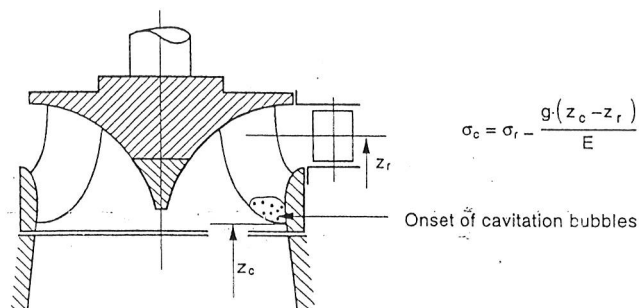


Figure 21 – Relation between the setting level  $z_r$  of a Francis turbine and the cavitation reference level  $z_c$

Cavitation tests with application of Froude similitude

The cavitation test may be performed, unless otherwise agreed in the contract, on a large-size model, installed with the axis in the same position as that of the prototype (e.g. horizontal or vertical) and under a specific hydraulic energy as required by Froude similitude.

As a consequence, for any corresponding elevation of model and prototype, the same Thoma number or cavitation coefficient results, provided that homologous cavitation reference levels  $z_c$  are used as illustrated by figures 21 and 22.

Cavitation tests without full application of Froude similitude

If the prototype machine dimensions are not significant in relation to the plant turbine/pump head, for the model test, it is sufficient to use  $\sigma_p$  to achieve a sufficient similitude for the cavitation pattern between model and prototype. However, it is essential that on model and prototype, homologous cavitation reference levels  $z_c$  are used (see figures 21 and 22).

The Froude condition cannot be applied, when it would result in excessively large models and/or very low test specific hydraulic energies compared with the minimum values indicated in 2.3.2.2.

In all cases where Froude similitude cannot be respected, the equality of Thoma number  $\sigma$  cannot be attained simultaneously for all homologous elevations on model and prototype. It is recommended that the homologous reference levels  $z_{cP}$  and  $z_{cM}$  in the prototype and model (for which the equality of Thoma numbers  $\sigma_{cP} = \sigma_{cM}$  shall be observed) be selected by mutual agreement before the test (see figure 22).

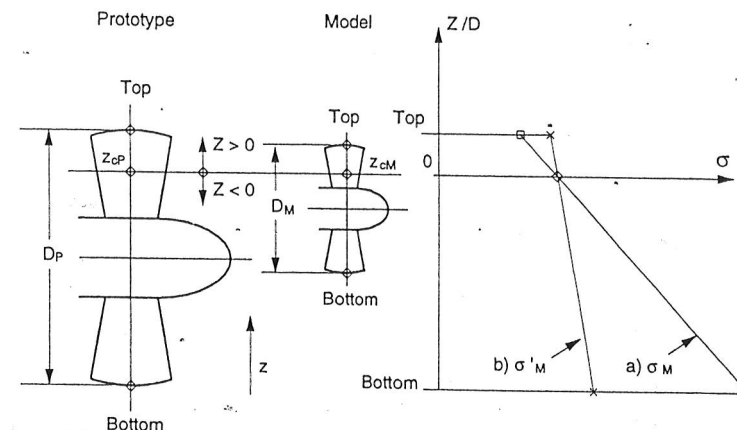


Figure 22 – Dependence of  $\sigma$ -values on level  $z$  for model and prototype, if:

- a) Froude similitude is respected:  $Fr_M = Fr_P$  then  $\sigma_M = \sigma_P$
- b) Froude similitude is not respected:  $Fr_M > Fr_P$  then  $\sigma'_M \neq \sigma_P$

The variation of  $\sigma$  for model and prototype between the lowest and highest points for a tubular turbine with horizontal shaft as illustrated by figure 22 is as follows:

$$\sigma_{\text{bottom}} = \sigma_c - \frac{g \cdot (z_{\text{bottom}} - z_c)}{E} = \sigma_c - \frac{g \cdot z_{\text{bottom}}}{E}$$

$$\sigma_{\text{top}} = \sigma_c - \frac{g \cdot (z_{\text{top}} - z_c)}{E} = \sigma_c - \frac{g \cdot z_{\text{top}}}{E}$$

If the Froude condition between model and prototype is respected, i.e.  $Fr_M = Fr_P$  then on all homologous elevations the ratios:

$$\frac{g \cdot (z - z_c)}{E} \text{ or } \frac{g \cdot z}{E}$$

are identical for both model and prototype, and consequently, identical  $\sigma$ -values result.

If the Froude condition between model and prototype is not respected, i.e.  $Fr_M \neq Fr_P$  then on homologous elevations  $z \neq z_c$  the difference  $\sigma_P - \sigma'_M$  results<sup>1)</sup>:

$$\sigma_P - \sigma'_M = g \cdot \left( \frac{(z - z_c)_M}{E_M} - \frac{(z - z_c)_P}{E_P} \right)$$

In cavitation tests where Froude similitude is not fulfilled, the net positive suction specific energy or the Thoma number should be adjusted to cover all conditions specified in the contract (variation of tailwater level), and to establish the safety margin between the minimum  $\sigma_{pl}$  and a contractually specified value such as  $\sigma_d$  (see 1.3.3.6.10), taking into account the difference  $\sigma_P - \sigma'_M$  as shown in figure 22.

In some cases, more than one cavitation reference level can be used, for example in the case of a large tubular turbine with horizontal shaft. Then performance characteristics can be measured at a plant Thoma number for example referred to an elevation located 0,2 D below the top of the runner, or referred to the top of the runner, or referred to the top of the hub. Agreement between the parties will be necessary to formulate the procedure to be followed and the subsequent interpretation of results.

Cavitation tests on pump-turbines

For pump-turbines, principally the same Thoma number or cavitation coefficient as defined in 1.3.3.6.6 or 1.3.3.6.7 shall be used for turbine and pump operation.

### 3.1.5.2 Performance tests on impulse turbines

Because of two-phase flow in the turbine housing, the efficiency of impulse turbines (e.g. Pelton type) may be strongly influenced by the Froude number. Therefore, it is recommended, in impulse turbine model tests, to choose a specific hydraulic energy which satisfies the Froude similitude.

### 3.1.6 Other similitude conditions

#### 3.1.6.1 Weber number

Although this standard does not consider any influence of the Weber number (except in annex K), it can be stated that the Weber number becomes important for two-phase flow as it occurs in the housing of impulse turbines. The degree of atomization of droplets, which influences the windage losses and/or the jet disturbance, is dependent on the Weber number.

For model tests of impulse turbines it is usually not possible to respect Froude and Weber similitude simultaneously. Froude similitude is maintained in most cases, because the effects depending on Froude generally dominate over Weber similitude effects.

<sup>1)</sup> When the specific hydraulic energy  $E_M$  of the test is bigger than the one required by the Froude condition, then  $(z - z_c)_M/E_M < (z - z_c)_P/E_P$ , and it follows that  $\sigma'_M > \sigma_P$  for all homologous elevations above the cavitation reference level (more favourable cavitation conditions occur on the model than on the prototype). The opposite occurs for all homologous elevations below the selected cavitation reference level.

### 2.3.1.6.2 Influence of nuclei content on cavitation pattern and performance

According to research work (see [1] and [3]) the visible extent of appearance of cavitation bubbles and the resulting cavitation characteristics can be significantly influenced by the content of nuclei in the water (non visible air or gas bubbles with a radius less than 50  $\mu m$ ).

At present, it is not possible to define the required minimum values for nuclei content and dissolved gas content which are linked in some way, because the impact of influencing parameters such as: type of machine, specific hydraulic energy, etc. has not yet been sufficiently established.

The measurement of nuclei content is described in 2.5.3.2. The appearance of cavitation and the possibility of observing it depend on the type of cavitation, which is correlated with the type of machine. Especially for cavitation tests ( $\sigma$ -variation) with Francis runners of medium or high specific speed, where cavitation usually occurs at the runner outlet, it is important that the water contains sufficient nuclei, which can be activated to grow in zones where the local pressure is equal to the vapour pressure.

Prototype measurements show that normally the number of nuclei is sufficient to produce cavitation in all zones of the runner/impeller, where vapour pressure prevails.

However, in test rigs with closed circuits, the number and the size of nuclei are reduced by degassing of the water occurring during cavitation tests. The result is that, at a defined  $\sigma$ -value (e.g. at  $\sigma$ -plant), an insufficient number of nuclei are activated to grow in the low pressure zones, which reduces the extent of visible cavitation.

Therefore, with respect to cavitation, model water quality is similar to prototype conditions if the nuclei content in the model is sufficient to ensure that cavitation development occurs in all the zones where the local pressure is equal to or less than the vapour pressure. This means that, in this condition, the extent of the zones with visible cavitation and the resulting drop in efficiency due to cavitation influence are no longer affected by different test conditions. This can be checked by varying the number of nuclei injected upstream of the runner/impeller or by increasing the test specific hydraulic energy, which could however violate Froude similitude.

### 2.3.2 Test conditions

#### 2.3.2.1 Determination of test conditions

The test conditions to be chosen for the different types of tests are dependent upon:

- capacity of test installation and its instrumentation;
- size and mechanical design of the model machine;
- guaranteed and/or specified operating range.

The same model shall be used for performance and cavitation tests.

If guarantees or specified data are given for the prototype, the required model test parameters can be calculated from hydraulic similitude, defined in 2.3.1.2 b), applying the formulae in 3.8.2.5. It is essential that the following aspects are taken into account:

- the permitted minimum values of table 4 shall be satisfied;
- the mechanical limitations due to model design shall be checked;

the limitations due to design and operation of the test rig and available instrumentation shall be considered.

models used for comparative tests shall be the same size and tested at approximately the same Reynolds number (see 2.1.3.2)

For performance tests, it is sometimes recommended to choose a test specific hydraulic energy higher than the minimum value to achieve a higher Reynolds number (Froude number impulse turbines), which is closer to that of the prototype, in order to reduce the relative accuracies in measurement.

It is unnecessary to require that cavitation model tests at a specific hydraulic energy be equal to that of the prototype. However, it is generally not desirable to test the model at very low specific hydraulic energies because of the reduced measurement accuracy and the risk of gassing in the low-pressure region.

From the above considerations, the absolute range of values of the following model quantities, the test conditions for each type of test, can be defined:

speed or specific hydraulic energy;  
discharge;  
power and/or torque;  
net positive suction energy (for reaction machines).

#### 2.2 Minimum values for model size and test conditions to be fulfilled

In order to achieve good hydraulic similarity between model and prototype, it is necessary to define minimum values for model size, Reynolds number, and test specific hydraulic energy as given in table 4, in addition to the requirements for geometrical similarity and surface roughness of model and prototype stipulated in 2.1.3.4 and 2.2.

These minimum values shall be satisfied in order to:

ensure the required dimensional accuracy, with normal manufacturing techniques;  
obtain test results with sufficient measurement accuracy, independent of inadmissible test conditions (e.g. due to air or gas separation during cavitation tests);  
reduce scale effects between model and prototype, by testing at appropriate Reynolds and Froude numbers.

The various minima are independent of each other and shall all be satisfied. Normally, models could be as large as practicable, but never less than the values stated.

Table 4 – Minimum values for model size and test parameters

Parameter	Type of machine			
	Radial (Francis)	Diagonal (Mixed-flow)	Axial (Kaplan, bulb)	Impulse (Pelton)
Reynolds number Re (-)	$4 \times 10^5$	$4 \times 10^5$	$4 \times 10^5$	$2 \times 10^5$
Specific hydraulic energy (per stage) E ( $\text{J} \cdot \text{kg}^{-1}$ ) (note 1)	100	50	30 (note 2)	500
Reference diameter D (m)	0,25 (note 3)	0,30	0,30	-----
Bucket width B (m)	-----	-----	-----	0,08
NOTES 1 With respect to the Froude similitude condition, the test specific hydraulic energy for cavitation tests may be chosen so that the resulting Re number is lower than the value given. 2 $E_{\min} = 20 \text{ J} \cdot \text{kg}^{-1}$ if $D \geq 0,4 \text{ m}$ 3 For pumps and pump-turbines with low specific speed, a reference diameter such as $0,20 \text{ m} \leq D \leq 0,25 \text{ m}$ may be allowed if the outer diameter is equal to or greater than 0,5 m.				

#### 2.3.2.3 Stability of test conditions

Fluctuations in the various measured quantities cannot be avoided. Such fluctuations can be of periodic or random nature within a large frequency range. They can be generated by elements of the test rig (e.g. booster pump, throttling devices, control system for low head pressure, etc.) and/or by the model machine (e.g. vortices in the draft tube, rotating stall, etc.). During model tests it is essential that at all operating points, repeatable steady-state operating conditions are achieved, especially within the range of guaranteed operation of the prototype.

##### 2.3.2.3.1 Stability and fluctuations during measurements

Before and during the measurement of a point, the operating stability of the test rig shall be such that repeated measurements of the same operating point are within the agreed random uncertainties of the various measured quantities (e.g. within  $\pm 0,3 \%$  for efficiency close to best efficiency conditions). This also means that drifting effects of discharge, specific hydraulic energy, speed and net positive suction energy shall remain small (e.g. within  $\pm 0,3 \%$ ). Drifting effects usually introduce systematic errors, and shall therefore be eliminated.

Fluctuations during the measurement of a point can be checked by means of the standard deviation of a measured quantity or the derived random uncertainty if the test rig is equipped with a suitable data acquisition system. If the results are affected by fluctuations, it may be necessary to apply linear hydraulic damping (see 3.3.3.4), to adjust the filtering of electric signals (see 3.1.4.3.2), to adjust the test conditions or to apply other means to eliminate these effects. However, such means shall not bias the measured quantity.

##### 2.3.2.3.2 Adjustment of the operating point

When the operating points to be measured are defined by specified dimensionless values (speed factor, discharge factor, Thoma number or other dimensionless terms) corresponding to the contractually specified ones, it is necessary to adjust the test conditions so that they are as close as possible to the specified data. Deviations between measured and specified dimensionless values should not exceed  $\pm 0,5 \%$  for speed, discharge or power coefficient or factor and  $\pm 3 \%$  for the cavitation coefficient or Thoma number.

### 3 Test procedures

#### 3.1 Organization of tests

en planning model tests, the following items covering general aspects of preparation, anization and realization shall be clarified and agreed on by the parties involved.

##### 3.1.1 Specification for model tests

pecification for model tests is the basis for planning and preparing a model acceptance test l for drafting the detailed technical programme of tests (see 2.3.3.3.2). This model test ification is often part of the general technical and/or commercial specification for a whole ject (e.g. supply and manufacture of a turbine or replacement runner/impeller) issued by the chaser or its engineer.

ong other items, the specification for model tests shall define:

object, scope and extent of model tests;  
reference to guaranteed and specified plant data;  
reference to test standards;  
model scale and/or size;  
place(s) where the model(s) or certain components are manufactured;  
place(s) where the model(s) is (are) tested;  
documentation of results (test reports);  
time schedule indicating, at a minimum, start and end dates of work for model testing.

##### 3.1.2 Time schedule

ime schedule should be agreed on, which indicates as a minimum, the different stages, adlines and/or duration for the following items:

submission of model drawings (especially those showing model construction and principal dimensions of model high and low pressure side at the transition to the test rig);  
description of testing equipment (including methods of calibration, calculation and representation of results and expected uncertainties of measurement);  
calibration of instruments;  
check of model geometry;  
preliminary and acceptance (or witnessed) tests and sequence of models to be tested in the case of comparative model tests;  
test reports.

e manufacturer shall always be given sufficient time to manufacture the model, making all cessary dimensional checks and carrying out his own preparatory tests, whether in his own oratory or elsewhere. In case of test equipment defects or model machine defects arising ring preliminary or acceptance tests, a mutual agreement is necessary to modify the time hedule and/or the test programme.

##### 3.1.3 Personnel and responsibilities

is important that the responsible persons of the purchaser and/or his engineer, of the plier and of the independent laboratory if any are designated in ample time before test mmencement. Their responsibilities and authority shall be clarified, so that any problems ising during the preparation for and conducting of tests can be quickly resolved.

Both purchaser and supplier shall be entitled to have authorized representatives present at all contractual tests, inspections and dimensional checks of the model and prototype, in order to verify that they are performed in accordance with both this standard and any prior agreement.

For the carrying out of tests (as defined in 2.3.3.3.1), a chief of tests shall be designated. The chief of tests can be selected from the technical staff of the laboratory where the model is tested or, by special agreement between the parties, an independent expert can act as chief of tests. The chief of tests will assume full responsibility for the correct calibration of instruments, execution of tests and computation of results, including determination of uncertainties of measurement and documentation of results in the final test report. The chief of tests shall consider any remarks or suggestions by any of the officially authorized representatives of the parties attending the tests.

When model tests are conducted in an independent or external laboratory, the supplier can be present during all activities for the test of his model, including the installation and any preparatory tests.

The tests shall be carried out by personnel having experience with the test equipment.

##### 2.3.3.1.4 Design of the model and preparation of the test installation

In order to prepare the model and the testing equipment, the technical specification for model tests (see 2.3.3.1.1) shall provide all relevant details for design and manufacturing of the model machine such as:

- extent of the water passages to be modelled on the high and low pressure sides;
- location of the pressure measuring sections;
- number and location of observation windows;
- provisions for exchange and/or adjustment of model components;
- provisions for special tests (video recording of cavitation pattern, pressure fluctuations, guide vane torque, axial or radial thrust, velocity profiles, etc.);
- test conditions for all types of specified tests;
- adjusting range for geometric parameters (e.g. maximum distributor opening, etc.).

In addition, sufficient data defining the extent and conditions for all the tests shall be given to enable the model to be constructed and prepared according to the state of the art. It is then possible to select the appropriate test facility, and to check the general arrangement of the model in the test rig, modifying or rearranging some of the existing components of the test rig if necessary.

It is recommended that inflow and outflow parts as well as the definitive location of the pressure measuring sections and the number of pressure tapings are agreed upon at an early stage of model design.

##### 2.3.3.1.5 Instrumentation and processing of test data

The person responsible for the selected laboratory or chief of tests shall provide the purchaser, or his engineer, with a description of the standard instrumentation installed on the test rig, including details on the measuring and calibration methods, on the processing of calibration and test data and on documentation of results.

In some laboratories, there are two or more instruments permanently installed for measuring a particular quantity. One shall be selected as the instrument whose measuring signals or indications are to be used in calculating the results, and the other(s) shall be used only for reference and functional control purposes.

netimes the calculation of test results occurs in several steps using more than one computer system. In this case, the evaluation procedure for the quantities concerned shall be defined in detail. It shall be agreed which quantities are processed on-line and immediately sent on records and/or diagrams, and which test results are calculated and documented offline.

### 3.1.6 Dimensional checks

Components which are to be checked before, during or after the acceptance tests shall be identified. The methods to be used for dimensional checks and the approximate extent and number of dimensions to be checked (see 2.2) shall be agreed in sufficient time to enable relevant documents and measuring equipment to be prepared accordingly. If accepted by the parties, it is possible to make spot-checks during the acceptance tests.

### 3.2 Inspections and calibrations

Shortly before the start of the preliminary and/or acceptance tests, the model, the test rig, the instrumentation and the data acquisition and processing system shall be thoroughly inspected by the representatives of the parties and the chief of tests, to ensure that the test results are not affected by any mechanical, structural or other defects of the model or the testing equipment.

Measuring instruments should be calibrated against primary methods (as explained in 3.2.4) prior to the tests and also after completion of tests if one of the parties so desires. Recalibrations during tests may be necessary if serious problems with the standard measuring equipment occur, such as a defect of an instrument or a measuring chain or a significant and systematic deviation of a measuring signal at zero or reference conditions.

Methods to be used, the extent of various calibrations (spot-check or complete calibration) and the procedure shall be agreed on by the parties before beginning the preliminary or acceptance tests. Based on certified documents produced by the responsible of the laboratory or chief of tests, it may be mutually agreed, for certain instruments, that the latest existing calibration data be used without further calibrations or checks.

#### 3.2.1 Inspection of the model machine

Items to be checked and/or recorded are:

identification of model components by means of the corresponding model drawings (especially if it is planned to exchange or modify certain components during testing);

geometric dimensions as listed in 2.2;

characteristic dimensions used for calculation of test results (e.g. areas of high pressure and low pressure measuring sections);

seal clearances and/or blade tip clearances;

individual and average values of guide vane angle or needle openings and/or runner/impeller blade openings;

surface quality, impurities and local faults in the different components;

proper matching at the joints of components;

conformity with reference dimensions on the model drawings.

If necessary, these checks shall be repeated if mechanical faults or defects occur during the tests (see 2.3.3.4), or at the end of witnessed tests, in the presence of the authorized representatives of all parties concerned. These checks are part of the official acceptance test.

#### 2.3.3.2.2 Inspection of the test circuit

As a minimum, the following checks shall be carried out:

- no water leakage or supply shall occur between the model and the discharge measuring section;
- no water leakage shall occur at pressure tapings and measuring pipes (on the low pressure side, no air leakage into the water circuit shall occur if the internal pressure is below ambient pressure);
- flow conditions close to the model inlet and outlet and close to the discharge measuring section shall be regular. The water passages shall have no disturbances and the wetted surfaces shall be of good quality;
- the booster pumps and regulating devices (valves, supply of water and pressurized air, etc.) shall work properly;
- the water quality and temperature shall be stable (see 2.1.2.3).

If necessary, some checks shall be repeated at the end of the acceptance tests, in the presence of all parties concerned.

#### 2.3.3.2.3 Calibration of instruments and check of the data acquisition system

It shall be agreed by the parties concerned:

- to what extent the various instruments shall be calibrated or spot-checked;
- if all instruments require to be spot-checked or calibrated before and after acceptance tests;
- the conditions for the recalibration of an instrument during or after acceptance tests;
- range of calibration and number of calibration or check points for the various instruments;
- the basic data and the procedure for evaluating the systematic uncertainties related to the calibration data and to each measured quantity.

Before and after the acceptance tests, as a minimum, the following checks or measurements shall be made:

- identification of instruments and/or measuring devices used;
- "zero readings", i.e. readings in well defined conditions for the different instruments, to detect if any drifting effects occurred during the tests;
- check of the data acquisition system by repeated measurements in well defined operating conditions. Manual sample calculations shall demonstrate that acquisition, transmission and processing of test data (usually automatic) work properly;
- measurement of mechanical friction torque in bearings and shaft seals which are not built into or connected to a stator of the swinging type (automatically yielding the torque on the runner or impeller), in order to decide if any further corrections should be applied.

The "zero readings" are usually checked during preliminary and acceptance tests. All the other checks and calibrations will be repeated, if necessary, at the end of the acceptance tests in the presence of all parties concerned.

the differences between the two checks or calibrations compared are less than the systematic uncertainty evaluated at the beginning of the tests, the test data are valid and no correction needs to be applied. If, between the two calibrations or checks, differences greater than the anticipated systematic uncertainty occur in several points, the test shall be cancelled or repeated.

In order to ensure the validity of calibration results, it is essential to maintain the influence quantities (such as ambient temperature and humidity, power supply, electromagnetic field, etc.) within a reasonable range during calibration and during tests (see 3.9.2.1.2).

Any of the interested parties may, for declared and substantiated reasons, call for a recalibration of any instrument during the course of a test.

### 3.3.3 Execution of tests

#### 3.3.3.1 Type of tests

Conducting an acceptance test successfully and efficiently requires good preparation by means of adequate preparatory tests. Depending on the results of preliminary and acceptance tests, it is sometimes necessary to perform additional tests.

For easier identification of the status of tests and for improved communication between the parties involved, this standard defines the following types of tests:

##### Preparatory tests<sup>1)</sup>

Often these tests are not specified in detail, but they are essential with respect to the quality of all further tests. They comprise:

- checks and tests to ascertain that model performance and cavitation pattern are not affected by any mechanical defects of model or test rig and measuring equipment;
- a check on the correct operation of the measuring equipment and data acquisition system. Often, it is helpful to perform a systematic variation of the test speed (i.e. a variation of  $E$ ) at constant  $\sigma$  and a variation of NPSE (i.e. a variation of  $\sigma$ ) at constant  $E$ , for at least one operating point.

Use of results:

normally, for internal use of the supplier or the laboratory only.

##### Preliminary tests

These are tests covered by the technical specification (see 2.3.3.1.1) or technical programme (see 2.3.3.3.2), and the extent is mainly dependent on the future use of the results. Therefore, the parties involved have to agree before beginning the tests, whether:

- the results are to be used for information only and have no contractual value. In that case, the preliminary tests are used only to explore the general behaviour or some limits of the model with respect to specified items;
- or whether the results will be used officially and have contractual value. In that case, these results are part of the official test data to be completed or spot-checked during the acceptance tests. For example, the results could be used to establish the efficiency step-up, as explained in 3.8.2.4, and the systematic and random uncertainties as explained in 3.9.2. However, such data shall be confirmed during the acceptance tests.

<sup>1)</sup> If mutually agreed, sufficient time should be allowed to the supplier during this period for the selection of definitive components or any last-minute adjustments, but these final development tests are not included in the scope of this standard.

#### c) Acceptance tests (or witnessed tests)

These tests measure, establish or check all relevant model data which are defined by the technical specification (see 2.3.3.1.1) or technical programme (see 2.3.3.3.2), and which form the basis for comparison with guarantees or other contractually specified data.

Use of results:

all results are of contractual value and shall be summarized in the final test report (see 2.3.3.5).

#### d) Additional tests

These are tests which supplement the results of preliminary and acceptance tests and which may include tests for additional data explained in 1.4.4. Such tests may or may not be witnessed.

Use of results:

these results are also summarized in the final test report (see 2.3.3.5). However, their possible contractual value shall be agreed on.

#### 2.3.3.3.2 Technical programme

A technical programme, referring to the technical specification (see 2.3.3.1.1) and the relevant contractual guarantees and data, shall be established in advance and agreed upon by the parties involved. If not covered by the contractual documents, the programme shall define the purpose and the extent of the various types of tests to be performed during preliminary and/or acceptance tests. To allow efficient progress in testing and documentation, the following shall be specified for each type of test, such as main hydraulic performance tests, cavitation tests, guide vane torque tests, etc.:

- ranges of hydraulic parameters to be varied and corresponding increments, to define the number and distribution of test points;
- test conditions to be maintained constant, i.e. usually the test speed (or specific hydraulic energy) and the Thoma number (tests at  $\sigma_{pi}$  or at higher  $\sigma$ -values);
- number and type of test data to be recorded and the method of recording;
- definitions, formulae and procedures (see 3.8.1 and figure 62) to be used for calculation of model and/or prototype results;
- guidelines for graphical representation of test results.

If necessary, for the acceptance tests, the technical programme can be supplemented, in order to clarify and define, for example:

- extent and sequence of checks, calibrations and tests to be witnessed;
- recording and/or graphical representation of test data to be signed by the parties to the tests;
- number and definition of the test point(s) to be measured for a sample calculation and for calculation of systematic, random and total uncertainties;
- preparation of a daily log and of a final protocol (see 2.3.3.3.9).

#### 2.3.3.3.3 Data to be used for calculation of results

Before the beginning of preliminary and/or acceptance tests, the data and formulae to be used for calculation of model and prototype results shall be checked and agreed on. Such data are:

- areas of high- and low-pressure measuring sections;

geometric and hydraulic references and data of model and prototype;  
 physical constants and properties for model and prototype;  
 model friction torque (if not automatically compensated);  
 calibration data for all relevant instruments;  
 leakage flow-rate through labyrinth seals, if considered (see 2.1.3.4.3);  
 efficiency step-up procedure.

sample calculation shall demonstrate the correct use of these data and explain the calculation procedure.

### 3.3.4 Signing and handling of test records

Complete records of measured model data and corresponding data at zero or reference conditions, as well as notes from inspections and calibrations, readings and observations during the acceptance tests and/or preliminary tests shall be agreed on and signed by the testing parties and by the chief of tests immediately on completion of each phase, and kept as a complete set by each party.

### 3.3.5 Performance tests

It is recommended to determine first the best efficiency point in non-cavitating conditions, i.e.  $\sigma_{piM}$  (for a pump-turbine, in both modes of operation) as the basis for calculation of  $\delta_{rel}$  (see 3.2.2) and efficiency increase  $\Delta\eta_h$ .

At least within the range of guarantee, the performance tests shall be carried out at constant speed and/or at constant test head. For computation of test results (see 3.8), it is preferable to perform the tests at constant speed and water temperature (if possible), so that the resulting Reynolds number is approximately constant. If, due to limitations of the model and/or the test installation, constant test conditions cannot be maintained, 3.8.2.2 explains the further processing required of such performance test results. In the same subclause, some typical graphical presentations of results of performance tests for various types of machines are given (see figures 55 to 61).

Reaction machines: influence of cavitation

Performance tests can be carried out in one of the following two test conditions:

- at plant Thoma number  $\sigma_M = \sigma_{pi}$   
 In this case, especially for machines of higher specific speed, cavitation which can affect efficiency could occur within the range of guaranteed efficiency. This has to be checked by means of  $\sigma$ -variations in the affected zones as explained and illustrated in 2.3.3.3.6.
- at non-cavitating condition, with  $\sigma_M > \sigma_{pi}$   
 This means that the Thoma number  $\sigma_M$  is sufficiently high to avoid any cavitation. As a consequence, the possible influence of cavitation on the performance curves at plant conditions is to be checked by  $\sigma$ -variations as explained in 2.3.3.3.6. If these tests reveal that within the range of guarantee an influence exists, figure 70 (see 3.8.2.3.7) explains the correction procedure for the efficiency curve measured with  $\sigma_M > \sigma_{pi}$ .

Impulse turbines: influence of tailwater level

For impulse turbines, it is recommended to determine the tailwater elevation at which performance is affected. This check is to be done at selected full load operating points, by varying the tailwater level.

### 2.3.3.3.6 Cavitation tests on reaction machines

Cavitation tests, i.e. systematic variations of the Thoma number  $\sigma$ , combined with recording of the cavitation pattern, are performed at selected operating points. The results are usually represented as illustrated in figures 71 and 72. At specified values of  $\sigma$  (e.g. at  $\sigma_{pi}$ ) it can be demonstrated how cavitation influences performance (efficiency, discharge or specific hydraulic energy, power). It is the only way to check the safety margin between the  $\sigma$ -values related to plant conditions and the  $\sigma_d$ -value at which performance is or begins to be affected by cavitation (see figure 70).

At each  $\sigma$ -variation it is important that the chosen geometric model parameters remain constant. It shall be agreed, whether the energy coefficient (or speed factor), or the discharge coefficient (or discharge factor) shall be kept constant.

If the model is equipped with suitable windows or transparent parts, it is possible, at specified values of  $\sigma$ , to observe the cavitation pattern at the runner/impeller and/or in the draft tube (where, for example, the vortex rope at part load operation of Francis turbines becomes visible), by the use of stroboscopic light. It is also possible to observe the cavitation pattern by introducing an endoscope into the model. Usually, this cavitation pattern is recorded by means of manual sketches, photos or video.

The results of cavitation tests may be used to indicate other phenomena associated with cavitation such as noise, vibration and pressure fluctuation.

For the consequences of not respecting the Froude similarity for large low specific hydraulic energy machines, see 2.3.1.5.1 c).

Contractual parties shall agree on the different reference levels and the corresponding  $\sigma_{pi}$  values to be used (see 2.3.1.5.1 and annex M), as well as on the method of how the influence of cavitation on performance, if any, should be considered when transposing the results to prototype conditions (see 3.8.2.4.2).

### 2.3.3.3.7 Runaway tests

The runaway test method depends on the design of the test rig, the instrumentation and the model design. If the test rig is, or can be, equipped with a driving motor to compensate friction torque due to shaft bearings and seals, it is usually possible to maintain  $P_{mM} = 0$ , and thus to establish directly the points of the runaway characteristics. If this procedure is not possible, the runaway conditions can be determined by extrapolation (as an example see figure 76) or by interpolation.

In most cases, the specific hydraulic energy is reduced, so that the highest speed which can be endured by the model and/or the testing facility is not exceeded. However, the minimum runaway speed of the model should not be lower than the speed used for performance testing. The influence of Reynolds and Froude numbers is assumed to be negligible in the range near to runaway.

The runaway tests shall be carried out with a sufficient variation of geometric parameters of the model machine, so that the most unfavourable combination of parameters and all specified conditions are covered. For multijet impulse turbines (Pelton turbines), the maximum steady-state runaway speed shall be measured taking into account the most unfavourable combination of operating nozzles.

Subclause 3.8.3.1 explains how the model runaway characteristics are determined for different types of machines and figures 74 to 76 give some examples of graphical representation of the runaway speed factor  $n_{EDR}$ .

reaction machines, the influence of cavitation on model runaway data is to be checked (see 3.2). The relevant  $\sigma_{PI}$ -value shall first be agreed on; it shall relate to the most unfavourable conditions which can occur during runaway (often at maximum specific hydraulic energy). There are then two possible methods for checking the influence of cavitation:

perform the model runaway tests at a sufficiently high Thoma number, and then check at selected, critical operating points the influence of cavitation by means of  $\sigma$ -variations, i.e. establish curves  $n_{ED,R}(\sigma)$  and  $Q_{ED,R}(\sigma)$  for each of these points;  
carry out the model runaway tests at  $\sigma_M = \sigma_{PI}$  and at  $\sigma_M > \sigma_{PI}$ .

### 3.3.8 Tests to check additional data

procedures applied for tests, such as:

pressure fluctuations;  
guide vane torque;  
four-quadrant performance characteristics;  
axial/radial thrust;  
etc.

described in clause 4 which details the relevant aspects of these additional tests.

### 3.3.9 Daily log and final protocol on acceptance tests

daily log shall summarize, for each day:

names of the persons participating in the tests;  
activities such as checks, calibrations, test series, discussions;  
agreements, decisions and unresolved issues with respect to test results;  
modifications of the technical programme and/or test programme.

At the end of the acceptance tests, a final protocol shall be established covering at least:

purpose of acceptance tests;

location and date of tests;

names of persons participating;

identification of the model and/or the model components;

comments and/or conclusions on:

- inspection of test rig, instrumentation and installation of the model;
- calibration of instruments;
- data acquisition system (sample calculation);
- check of model geometry;

discussion of results and comparison with guaranteed and/or specified data, covering at least:

- performance tests;
- cavitation tests;
- runaway tests;

conclusions regarding whether:

- guarantees and specifications have been met;
  - test results are complete with respect to the technical programme and technical specification for the model tests;
- agreements on:
- additional tests (if any);
  - documentation of test results;
  - shipment or storage of the model.

### 2.3.3.4 Faults and repetition of tests

#### 2.3.3.4.1 Types of faults and consequences

During the acceptance tests, faults in the model, test rig, instrumentation or data processing may arise, such as:

a) mechanical faults in the model:

- bearing or seals of the model fail and effect a change of mechanical friction losses. Replacement bearings and/or seals need to be fitted, but the mechanical friction losses may have changed;
- running clearances and/or throttling conditions in piping for leakage flow-rate may have changed, effecting changes in hydraulic performance;
- guide vanes and/or runner/impeller blades become misaligned affecting performance and/or cavitation pattern;
- mechanical defect on runner/impeller or at other model components occurs.

b) faults in the test rig or instrumentation:

- unusual variations of speed, specific hydraulic energy or discharge are introduced due to faults in the auxiliary control systems of the test rig or due to malfunctioning of components;
- additional leakage due to an open valve or a defect in the measuring leads is detected;
- excessive shift of instrument indications at zero conditions before and after a series of tests is detected.

c) faults in data processing

- malfunctioning of the data acquisition system may produce faulty test results;
- faulty test results are produced due to incorrect reference or calibration data.

The correction of such faults shall be closely supervised by the chief of tests and all parties concerned.

In comparative tests, particular care shall be taken to ensure that none of the parties is advantaged from the results obtained up to that point. The tests shall be completed in the manner they began and without modification of the hydraulic design.

After correction of the fault, several preparatory tests and/or preliminary tests should be made to ensure that the model is behaving exactly as it was before the faults occurred. If its performance is proven to have changed, then by mutual agreement, the previous series of tests shall either:

be allowed to stand, and no further tests be deemed necessary;  
or be declared invalid and the whole series of tests repeated.

### 3.4.2 Procedure for repetition of tests

y. of the parties shall have the right to require interruption and/or repetition of the tests, provided the chief of tests deems valid the reasons put forward, for example:

unsatisfactory agreement between calibrations before and after tests;  
test rig, instrumentation or data processing malfunction;  
mechanical faults in the model;  
non-compliance, to a significant degree, with this standard, except as otherwise agreed beforehand.

such a situation, the other party(ies) and/or the chief of tests may also demand a repetition of the tests. It is recommended that the subject of repeated tests, repeated calibrations and the responsibility for the associated costs be subject to written agreement beforehand.

no agreement can be reached on how to conduct such a repetition of tests or who is responsible for the additional costs, the matter shall be referred to an independent arbitrator acceptable to all parties.

### 3.3.5 Final test report

After completion of all tests according to the technical specification for model tests (see 3.3.1.1) and the technical programme (see 2.3.3.3.2), a final test report shall be prepared according to the rules set out in this standard and signed by the chief of tests. The parties shall agree whether a draft of the whole report or only selected chapters have to be approved before distributing the final version.

The final report shall cover primarily the following items:

- object and purpose of tests, with reference to technical specification of model tests including relevant guarantees and other contractual data;
- records of all agreements, and other essential documents pertinent to the tests;
- personnel taking part in the tests;
- description of the model machine together with drawings showing, as a minimum, the main section of the model and its general arrangement in the test rig;
- description of the test rig and the measuring equipment, including calibration methods and data processing;
- calculation of model test results and transposition to contractual model and/or prototype conditions (including consideration of scale effects, if any);
- calibration data and inspection reports;
- test procedures for the different types of tests;
- log covering activities related to the specified tests and the sequence of different tests;
- relevant test records and data sheets from measurements and observations of the various tests, together with the test results graphically represented;
- calculation of uncertainties of measurement with reference to the calibration data, results and further observations;

- 12) discussion and interpretation of test results and comparison with guaranteed and other contractual data;
- 13) conclusions as to whether or not the guaranteed and contractual requirements have been met, and the tests are complete with respect to the technical specification.

## 2.4 Introduction to the methods of measurement

It is recognized that no physical quantity can be measured without error. Consequently, the result of any measurement is worthless if not accompanied with the associated uncertainty estimated at a given confidence level. General prescriptions on analysis and combination of uncertainties are given in 3.9.

The quantities to be measured during a model test to verify the main hydraulic performance guarantees defined in 1.4.2 require a high level of accuracy. For this reason, the prescriptions given in clause 3 of this standard are mandatory in order that the test may be deemed to be in accordance with this standard. Subclause 2.4.1 gives prescriptions on how to calculate the quantities (power, efficiency) which are derived from the basic quantities (discharge, specific hydraulic energy, shaft torque, speed of rotation). Hydraulic quantities such as NPSE and  $\sigma$  related to the influence of cavitation on the hydraulic performance are determined from the same physical measurements, and thus with the same accuracy, as those used for the above basic quantities.

Additional quantities are determined mainly for guidance, even if some of them may be of contractual interest (see clause 4).

### 2.4.1 Measurements related to the main hydraulic performance guarantees

#### 2.4.1.1 Hydraulic efficiency

The purpose of a model acceptance test on a hydraulic machine in accordance with this standard is to compare the achieved hydraulic performance, expressed either as the measured model performance or transposed to prototype performance, with guarantees given by the supplier.

Since there is no correlation between the mechanical losses (power dissipated in the guide bearings, thrust bearings and shaft seals) of the model and those of the prototype, the comparison shall be based on the mechanical power of runner/impeller  $P_m$  (see 1.3.3.8.3) and hydraulic efficiency  $\eta_h$  (see 1.3.3.9.1) and not the mechanical power of the machine  $P$  (see 1.3.3.8.2) and efficiency  $\eta$  (see 1.3.3.9.3).

Hydraulic efficiency is calculated from the mechanical power  $P_m$  transmitted through the coupling of the runner/impeller and the shaft and the hydraulic power  $P_h$  exchanged with the water. It is given by:

$$\eta_h = \frac{P_m}{P_h} \text{ for a turbine,}$$

and

$$\eta_h = \frac{P_h}{P_m} \text{ for a pump.}$$

It shall be noted that according to these definitions the disc friction losses and leakage losses (volumetric losses) are considered in this standard as hydraulic losses, and therefore no correction is made.

the principle of the method involves the measurement of discharge  $Q$ , specific hydraulic energy  $E$ , torque  $T$  and rotational speed  $n$ .

the direct determination of hydraulic efficiency by the thermodynamic method is not recommended for model acceptance tests.

### 1.2 Hydraulic power

the determination of hydraulic power requires the knowledge of the specific hydraulic energy of machine and of the mass flow rate through the high pressure reference section of the del. The formula is:

$$P_h = E (p, Q)_1$$

the transfer of water to or from the system between the reference section and the discharge measuring section shall be taken into account. Where the volume flow rate is measured, the value obtained shall be associated with the value of water density in the conditions of pressure and temperature prevailing in the discharge measuring section.

Subclause 2.5 explains how to determine the values of physical quantities such as the local acceleration due to gravity, the water density, etc. either by direct measurement or from internationally recognized formulae or tables. Methods of discharge measurement are described in 3.2. Methods of specific hydraulic energy determination, from pressure measurement in accordance with 3.3 (or possibly from water level measurement in accordance with 3.4), are described in 3.5.

### 1.3 Mechanical power

the calculation of the mechanical power from the measurement of electrical power at the motor/generator terminals and from the efficiency of the latter is not recommended for model acceptance tests. Thus the determination of mechanical power at the runner/impeller requires knowledge of the torque supplied by/applied to the runner/impeller and of the rotational speed:

$$P_m = 2 \pi n T_m$$

Methods of torque measurement are described in 3.6. Methods of rotational speed measurement are described in 3.7.

### 1.1.4 Computation of efficiency

From the definitions given in the previous subclauses, the hydraulic efficiency of a model in the operating conditions prevailing during a point may be calculated by:

$$\eta_h = \frac{2 \pi n T_m}{E(p, Q)_1} \text{ for a turbine,}$$

and

$$\eta_h = \frac{E(p, Q)_1}{2 \pi n T_m} \text{ for a pump.}$$

When the guarantees are referred to the prototype performances, the hydraulic efficiency and mechanical power of runner/impeller of the prototype shall be determined from the corresponding quantities of the model by applying a scale-up formula, as explained in 3.8.2.4. The mechanical losses of the prototype shall then be taken into account to determine the mechanical power of the machine  $P$  (power delivered by the turbine shaft or to the pump shaft) and the total efficiency of the hydraulic machine  $\eta = \eta_h \cdot \eta_m$ , more simply called "efficiency" in this standard (see 1.3.3.9.3).

### 2.4.2 Measurements related to additional data

In addition to the verification of the main hydraulic performance guarantees, model tests may be used to determine some additional data (see clause 4). This implies the measurement of the stationary and/or fluctuating components of various hydraulic or mechanical quantities.

### 2.4.3 Acquisition and processing of data

Whatever the quantity to be measured, particular care shall be given to the method of averaging a fluctuating signal to obtain the true mean value of the physical quantity and to the analysis of this signal to characterize the frequency and amplitude of the fluctuations. Subclauses 3.1 and 4.2 give guidance on the requirements of the system of measurement and on data processing for obtaining average and fluctuating quantities respectively.

## 2.5 Physical properties

### 2.5.1 General

This subclause defines the main physical properties needed to characterize the hydraulic behaviour of hydraulic machines. The terms and definitions of most of these quantities are listed in 1.3.3.3 together with their symbols and units.

The formulae which can be used in data processing to calculate these quantities are listed in the following subclauses. For convenience, tables of numerical values derived from these formulae are given in annex B.

### 2.5.2 Acceleration due to gravity

Acceleration due to gravity  $g$  (see 1.3.3.3.1) is given as a function of latitude and altitude:

$$g = 9,7803 (1 + 0,0053 \sin^2 \varphi) - 3 \cdot 10^{-6} \cdot z$$

where

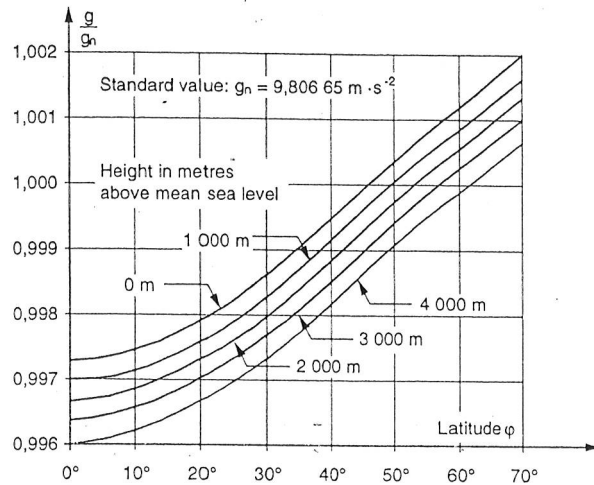
$\varphi$  is the latitude in degrees, and

$z$  is the altitude in metres.

The computed values of  $g$  are given in table B.1 and are represented in figure 23.

The international standard value of  $g$  is  $9,806 65 \text{ m} \cdot \text{s}^{-2}$ .

If measured values of  $g$  are available, they shall be used. The local value of  $g$  can be measured for example by a pendulum or free fall (in vacuum).

Figure 23 – Acceleration due to gravity  $g$  ( $\text{m} \cdot \text{s}^{-2}$ )

### 3 Physical properties of water

#### 3.1 Density of water

##### 3.1.1 Application of the density of water

testing hydraulic machines, the density of water  $\rho$  (see 1.3.3.3.3) shall be known in order to:

determine the specific hydraulic energy of machine E from pressure measurements (see 1.3.3.6.2);

determine the mass flow rate ( $\rho Q$ ) needed for the calculation of the hydraulic power (see 1.3.3.8.1);

d, if necessary, to:

calculate the pressure from measurements by using a water column manometer (see 3.3.4.2);

determine the discharge when the weighing method is used for the measurement itself or for the calibration (see 3.2.2.1 and 3.2.2.2).

##### 3.1.2 Density of actual water

ie water used for model testing in the laboratory contains slight quantities of dissolved substances, depending on the local hydrological conditions. Therefore its actual density  $\rho_{wa}$  is higher than that of distilled water  $\rho_{wd}$  (see 2.5.3.1.3). However, the value of  $\rho_{wa}$  in the model test equipment generally differs by less than 0,05 % from the value of distilled water  $\rho_{wd}$ .

For calculation of the hydraulic efficiency, this deviation is negligible if the determination of the specific hydraulic energy of the machine E is predominantly obtained by pressure measurement (see annex D). Therefore, in most cases, it is sufficient and suitable to apply the values for distilled water.

However, if it is necessary to determine the density  $\rho_{wa}$  of the water actually used, several methods can be applied:

- an indirect method using a calibrated pressure gauge connected to a static free water level, as described in 3.3.5.2;
- direct methods such as a precision hydrometer (e.g. a pycnometer, or so called "density bottle") or a buoyancy method.

It may be assumed that the ratio of the actual and distilled water densities is constant whatever the pressure and temperature. So, if the density of the actual water has been measured at certain conditions c of pressure and temperature ( $\rho_{wa,c}$ ), its value for any other condition can be calculated by:

$$\rho_{wa} = \frac{\rho_{wa,c}}{\rho_{wd,c}} \cdot \rho_{wd}$$

where  $\rho_{wd}$  and  $\rho_{wd,c}$  are calculated according to 2.5.3.1.3.

##### 2.5.3.1.3 Density of distilled water

The formula for the density  $\rho_{wd}$  of distilled water as a function of temperature and pressure is derived by Herbst and Roegenen [4] from the empirical state equation of the free enthalpy of distilled water. In determining the coefficients below, all the test results of Kell and Whalley [5] and of Kell, McLaurin and Whalley [6] were used.

$$\rho_{wd} = 10^2 \left[ \sum_{i=0}^3 \sum_{j=0}^3 R_{ij} \cdot \alpha^i \cdot \beta^{(j-1)} \right]^{-1}$$

where

$$\beta = \frac{1}{p^*} (p_{abs} + 200 \cdot 10^5) \quad (p^* = 10^5 \text{ Pa})$$

$$\alpha = \frac{1}{\theta^*} (\theta - \theta_1) \quad (\theta^* = 1 \text{ } ^\circ\text{C})$$

From 0 °C to 20 °C:  $\theta_1 = 0 \text{ } ^\circ\text{C}$       From 20 °C to 50 °C:  $\theta_1 = 20 \text{ } ^\circ\text{C}$

The formula is valid in the used pressure range from  $p_{abs} = 0$  to  $150 \cdot 10^5 \text{ Pa}$

Table 5 furnishes the coefficients  $R_{ij}$  ( $\text{m}^3 \cdot \text{kg}^{-1}$ ).

Table 5 – Coefficients of the Herbst and Roeger formula

R(i,j) in the temperature range 0,0 °C to 20,0 °C			
j = 0	j = 1	j = 2	j = 3
$0,4466741557 \cdot 10^{-4}$	$-0,5594500697 \cdot 10^{-4}$	$0,3402591955 \cdot 10^{-5}$	$-0,4136345187 \cdot 10^{-7}$
$0,1010693802$	$-0,1513709263 \cdot 10^{-4}$	$0,1063798744 \cdot 10^{-5}$	$-0,8146078995 \cdot 10^{-8}$
$-0,5398392119 \cdot 10^{-5}$	$0,4672756685 \cdot 10^{-7}$	$-0,1194765361 \cdot 10^{-8}$	$0,1366322053 \cdot 10^{-10}$
$0,7780118121 \cdot 10^{-9}$	$-0,1619391322 \cdot 10^{-10}$	$0,5883547485 \cdot 10^{-12}$	$-0,8754014287 \cdot 10^{-14}$

R(i,j) in the temperature range 20,0 °C to 50,0 °C			
j = 0	j = 1	j = 2	j = 3
$-0,4410355650 \cdot 10^{-4}$	$0,3052252898 \cdot 10^{-4}$	$0,9207848427 \cdot 10^{-6}$	$-0,2590431198 \cdot 10^{-7}$
$0,1011269892$	$0,1763956234 \cdot 10^{-4}$	$0,5750340044 \cdot 10^{-6}$	$-0,1923769978 \cdot 10^{-8}$
$-0,4832441163 \cdot 10^{-5}$	$0,1533281704 \cdot 10^{-7}$	$-0,3749721294 \cdot 10^{-9}$	$0,1322804180 \cdot 10^{-11}$
$0,6194433327 \cdot 10^{-9}$	$-0,3164540431 \cdot 10^{-11}$	$0,6311389123 \cdot 10^{-13}$	$0,2469249342 \cdot 10^{-15}$

lead of the formulae of Herbst and Roeger [4], the formulae of Borel and Lan [7] or of ar, Gallagher and Kell [8] can also be used for calculation by computer.

these authors have taken the experimental values [5, 6] as their basis. The values of these differences are within the same range of accuracy ( $\pm 0,01\%$ ) in the range of temperature and pressure as mentioned above.

numerical application, the simpler empirical equation of Weber [9], somewhat transformed, may be used. The values calculated for temperatures up to  $35^\circ\text{C}$  and pressures up to  $1 \cdot 10^5 \text{ Pa}$  are within the same range of accuracy as mentioned above:

$v$  is the specific volume in  $\text{m}^3 \cdot \text{kg}^{-1}$ :

$$v = 1/p = v_0 [(1 - A \cdot p) + 8 \cdot 10^{-6} \cdot (\theta - B + C \cdot p)^2 - 6 \cdot 10^{-8} \cdot (\theta - B + C \cdot p)^3];$$

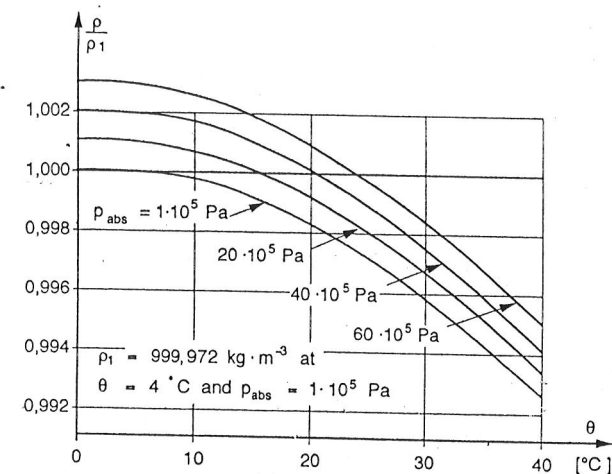
h  $v_0 = 1 \cdot 10^{-3} \text{ m}^3 \cdot \text{kg}^{-1}$

$$A = 4,6699 \cdot 10^{-10} \quad (p = p_{\text{abs}} \text{ in Pa})$$

$$B = 4,0 \quad (\theta = \text{temperature in } ^\circ\text{C})$$

$$C = 2,1318913 \cdot 10^{-7}$$

values for distilled water on the basis of the formula of Herbst and Roeger [4] are given in table B.2 and are represented in figure 24.

Figure 24 – Density of distilled water  $\rho_{wd}$  ( $\text{kg} \cdot \text{m}^{-3}$ )

### 2.5.3.2 Condition of water during test

#### 2.5.3.2.1 Definition of nuclei and gas content in water

As stated in 2.1.2.3 and 2.3.1.6.2, to determine the influence of cavitation on the performance of the machine it is useful to know, in addition to pressure and temperature, other conditions of the water passing through the machine. These other conditions are:

- **nuclei content** (see 2.1.2.3) in terms of number of nuclei per unit volume of water. The nuclei content corresponds approximately to the undissolved gas (air) content in terms of volume per unit volume of water;
- **dissolved gas content** in terms of volume per unit volume of water.

Possible extreme conditions for water are:

- completely degassed water (water with no nuclei and no gas content);
- completely saturated water (water saturated with dissolved gas, however with low content of nuclei);
- high nuclei content of water due to an artificial injection, independently of the content of dissolved gas.

It is currently not possible to specify in advance a value for the required nuclei content, which depends on model scale, test specific hydraulic energy and other factors.

For a discussion of the influence of water conditions (nuclei content, gas content) in model testing, see 2.3.1.6.2 and references [1] and [3].

### 3.2.2 Determination of nuclei and gas (air) content in water

#### 3.2.2.1 Nuclei content in water

A determination of the nuclei content of water requires the measurement of the number and the critical pressure of nuclei.

A special cavitation nuclei counter is described in [1] and [3]. In this counter, the flow is accelerated through a restricted section to promote the explosive growth of nuclei.

The injection of nuclei can be performed by the injectors described in [1] and [3]. These injectors are based on the rapid expansion of saturated water through an orifice.

#### 3.2.2.2 Gas content (air content) in water

Water normally contains gases in dissolved or undissolved form. These gases may be air or other substances such as carbon dioxide (CO<sub>2</sub>).

##### Dissolved gas content

The maximum possible amount of dissolved gases depends on the pressure and temperature of the water and the actual gas content shall be measured. Two basic methods of measurement can be applied<sup>1)</sup>:

- measurement of dissolved oxygen content using an electrical analyzer based on the oxygen diffusion through a PTFE membrane (e.g. Beckman apparatus [10]);
- physical separation: Van Slyke method [11]. This method allows the extraction of the totality of the air content, whether in dissolved or occluded form, by cascading the sampling under vacuum in a packed column. The method is relatively rapid, but necessitates working on small volume samplings.

##### Undissolved gas content

A gas completely dissolved on the high pressure side of a hydraulic machine may become free while moving from the high pressure side to the low pressure side of the circuit, thus changing the behaviour of the machine. Therefore, the gas content not only for dissolved but also for undissolved gases should be determined. Such a method using an extraction vessel is described in [13].

[12] a comparison of the Van Slyke, Merl and Brand [13] apparatus and a dissolved oxygen meter is made, including measurement of dissolved and undissolved gases.

### 5.3.3 Kinematic viscosity

The kinematic viscosity  $\nu$  (see 1.3.3.3.6) of water depends on its temperature  $\theta$  and absolute pressure  $p_{abs}$  and is derived from the basic physical property dynamic viscosity  $\mu$  using  $\nu = \mu/\rho$ .

Formula for  $\mu$  is given in [14].

However, for practical reasons in hydraulic machinery, an approximate value of  $\nu$  can be computed using the following formula:

$$\nu = e^{-16,921 + 396,13/(107,41 + \theta)}$$

<sup>1)</sup> The Winkler method, using iodometry, may also be used. It is accurate, but its application is difficult.

Using this equation, the average deviation from the standard values given in [15] is  $\pm 0,05\%$ , the maximum deviation is  $\pm 0,09\%$ .

The influence of pressure is negligible. The deviation for  $p = 10 \cdot 10^5$  Pa against a reference pressure of  $p = 10^5$  Pa is about  $-0,05\%$ .

Values for  $\nu$  are given in table B.3.

### 2.5.3.4 Vapour pressure

The vapour pressure  $p_{va}$  (see 1.3.3.3.4) of water between the water temperatures of  $\theta = 0^\circ\text{C}$  and  $\theta = 40^\circ\text{C}$  can be calculated using the following empirical formula:

$$p_{va} = 10^{(2,7862 + 0,0312\theta - 0,000104\theta^2)}$$

The resulting error is less than  $\pm 7$  Pa.

Numerical values of  $p_{va}$  are given in table B.4, see [8].

Attention shall be paid to dissolved chemical substances in water which may influence the vapour pressure.

### 2.5.4 Physical conditions of atmosphere

#### 2.5.4.1 Density of dry air

The density of air  $\rho_a$  (see 1.3.3.3.3) as a function of  $p_{abs}$  and temperature of air  $\theta$  can be calculated using the following formula according to ISO 2533:

$$\rho_a = (p_{abs} \cdot 3,4837 \cdot 10^{-3}) / (273,15 + \theta)$$

Values of  $\rho_a$  are given in table B.5.

The influence of humidity on the density of air is negligible for the determination of E.

#### 2.5.4.2 Ambient pressure

Normally, the ambient pressure  $p_{amb}$  (see 1.3.3.5.2) is the barometric pressure measured in the laboratory by a barometer. For conversion of test results to the conditions of prototype at site (e.g. determination of NPSE or  $\sigma$  of the site) the ambient pressure shall be calculated using the standard atmosphere defined in ISO 2533.

Assuming a linear change of temperature with elevation equal to  $-6,5 \cdot 10^{-3}$  K/m, the ambient pressure may be calculated by the following approximate formula derived from ISO 2533:

$$p_{amb} = 101\,325 \left( 1 - 2,2558 \cdot 10^{-5} \cdot z \right)^{5,255}$$

where  $z$  is the elevation, in metres.

The resulting error is less than  $\pm 15$  Pa.

Values for  $p_{amb}$  from ISO 2533 are given in table B.6.

## 5 Density of mercury

The density of mercury  $\rho_{Hg}$  (see 1.3.3.3.3) used in liquid manometers is calculated for pure mercury by the following equation with  $p_o = 101\,325$  Pa (standard ambient pressure at sea level):

$$\rho_{Hg} = (13\,595 - 2,46 \theta) \left[ 1 + 3,85 \cdot 10^{-11} (p - p_o) \right]$$

Values of  $\rho_{Hg}$  are given in table B.7, see [16].

Mercury used in practical applications may be contaminated by dissolved metal or by other materials. To ensure valid measurements the mercury shall be pure and clean.

## 3 Main hydraulic performances: methods of measurement and results

### 3.1 Data acquisition and data processing

#### 3.1.1 Introduction and definitions

Data acquisition and data processing involve the conversion of measured signals into appropriate engineering units through a measuring chain of several components such as transducers, multiplexers, signal converters or conditioners, data storage equipment and computers. The final output is a presentation of parameters as meaningful performance data.

The measurands are fluctuating quantities. However, their average values are of main interest for the determination of the main hydraulic performances of a model.

#### Definitions:

##### measurand

quantity subjected to measurement

##### transducer

measuring device, which provides an output quantity with a given relationship to the input quantity

##### transducer with digitized output

measuring device with built-in electronics to give a digitized output (e.g. serial port RS 232)

##### multiplexer (MUX)

device for switching two or more signals in order to share the same analog-to-digital converter, frequency counter or cabling facilities

##### analog-to-digital converter (A/D converter)

device that translates continuous analog signals into discrete digital signals

##### counter

device that measures frequency, time period or number of pulses

##### voltage-to-frequency converter (V/F converter)

device that translates with a given relationship, voltage levels into frequency

##### aliasing

when sampling analog signals with a sampling rate less than twice that of the frequency of the highest-frequency signal or noise component ("Nyquist rate"), the sampling process will produce spurious low-frequency signals (aliases) that cannot be distinguished from the original signal

##### computer interface

communication port that enables the computer to control and communicate with other compatible devices

#### 3.1.2 General requirements

The output from the data acquisition and data processing system shall be a true reflection of the measurand.

Documented calibration procedures shall exist for all instruments in use. Maintained records of all measurement standards and measuring equipment used to establish compliance to specified requirements shall also exist.

Where applicable, it should be made possible via parallel connections to witness *in situ* the calibration of all instruments in the measuring chain by a primary method to verify that the complete data acquisition system represents the measurand within the specified limits. This usually means that the same signal path, hardware and software configuration shall be used during both calibration and performance testing.

During a performance test, the averages of each of the measured quantities shall be obtained by measurements performed during the same time interval.

A possible check of the complete measuring chain would be to have parallel instrumentation. It is also preferable to have the capability of comparing the results from the data acquisition system and the reference instrument(s) even under running conditions of the machinery being tested.

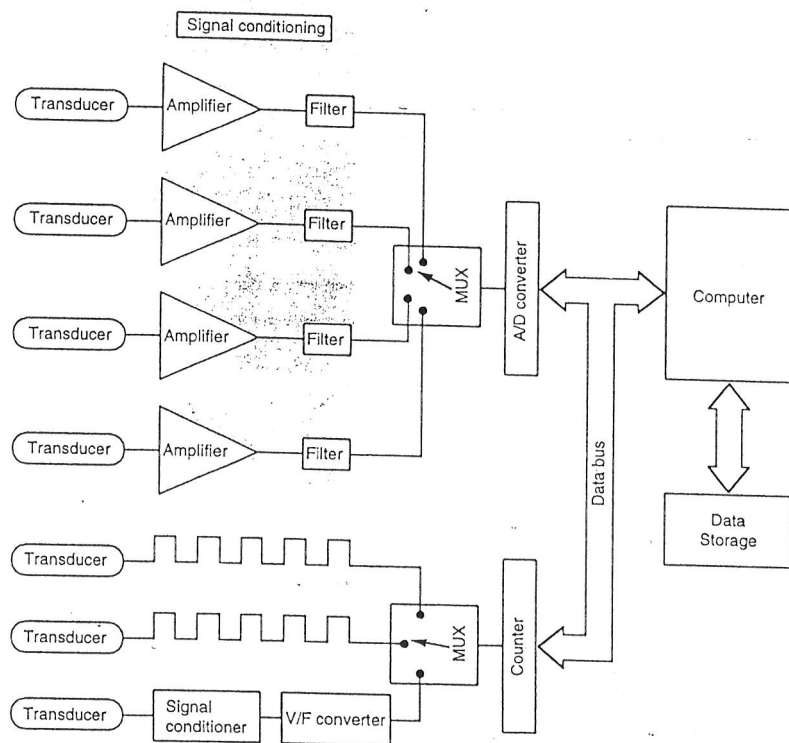


Figure 25 – Time multiplexing data acquisition system

### 3.1.3 Data acquisition

The data acquisition system may be arranged in different ways (including manual methods) depending on the hardware available and the chosen averaging method.

Possible arrangements and examples of different data acquisition systems are given. Usually a combination of different systems is used.

#### 3.1.3.1 Time multiplexing system

In a time multiplexing system (figure 25), the measurands are measured via multiplexers that scan the channels sequentially a number of times during a given time period.

The calculated average value of the measurand is taken for further processing.

#### 3.1.3.2 Parallel measuring system

In a parallel operated system (figure 26), the measurands are measured by a computer collecting the data directly from each channel. This arrangement makes possible high speed data logging and simultaneous sampling of all the channels (see 3.1.4.4).

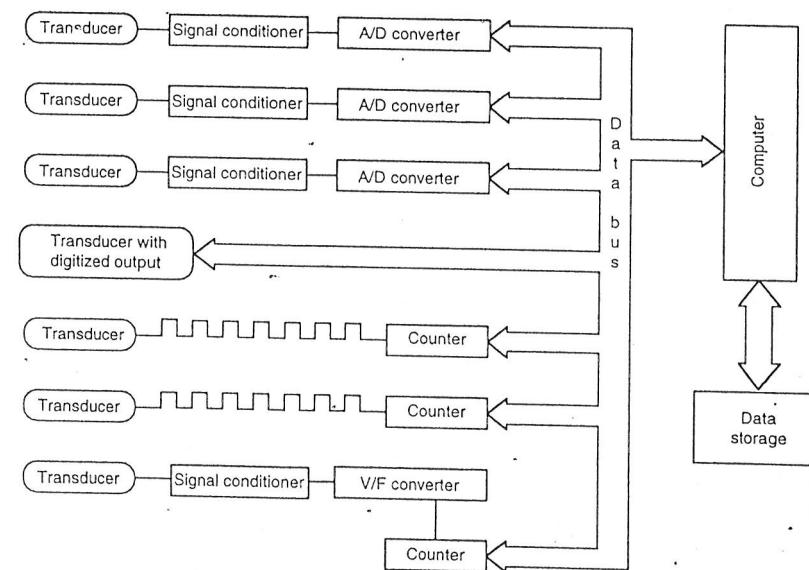


Figure 26 – Bus operated data acquisition system

#### 1.4 Component requirements

The components in the measuring chain shall be able to manage the frequency range of interest.

Components transferring information about the measurand to the transducer, for example pressure piping, can cause spurious effects and cause errors in the measurements.

For all the components in the measuring chain, note that temperature variations, in their environment, can cause errors in the measurements outside the specified limits.

Properties such as linearity and hysteresis shall be documented during calibration.

##### 1.4.1 Transducer

Transducers used for the measurement of performance parameters should operate in a stable temperature environment. They should be located where they are not influenced by temperature variations, for example from direct sunlight, heating panels, ventilation channels, etc.

The dynamic behaviour of the measurands shall be known, as the transducers shall only be used in the frequency domain they are designed for.

Precautions should be taken when using transducers with special inherent damping property or adjustable response time, and transducers with extremely high deflection of the sensing element. Such transducers can cause erroneous measurements in both averaging and oscillating measurements.

##### 1.4.2 Cables and termination

The signal path between transducers and amplifier shall be designed in such a way that external influences on the signals (e.g. from power lines or temperature variations) are minimized. Proper shielding and grounding shall be observed. Connectors and terminations shall have stable, reliable mechanical and electrical properties.

Even if all the above precautions have been taken, additionally be aware of spurious influences from the power network on the measurement results.

##### 1.4.3 Signal conditioning

The output from transducers with analog output are often amplified and filtered in a signal conditioning unit.

###### 1.4.3.1 Amplifier

To exploit the resolution of the A/D converter, the output range of the amplifier shall match the range of the converter.

The amplifier shall be located as close as possible to the transducer in order to minimize the influence of noise pick-up in the cabling.

###### 3.1.4.3.2 Filter

When choosing filters, special attention should be paid to properties such as:

- a.c. signals: cut-off frequency, attenuation (order) and time delay;
- d.c. signals: offset, temperature drift and linearity.

In analyses where simultaneous measurement of two or more measurands is important, be aware of delays in the conditioning and data acquisition systems. Filters cause delays (phase shift) that are a function of the filter type and the cut-off frequency (figure 27).

The cut-off frequency of a low-pass filter shall be a maximum of half the sampling frequency in order to avoid aliasing effects. This is illustrated in figure 28. In practice, however, a cut-off frequency of one-third or less of the sampling rate is used.

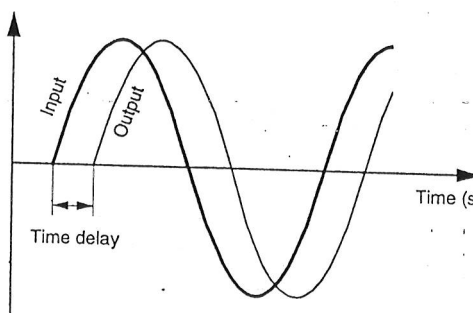
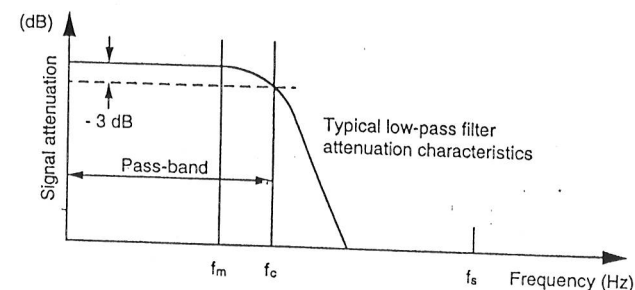


Figure 27 – Time delay



$f_m$  is the maximum frequency component of interest;  
 $f_c$  is the cut-off frequency of low-pass filter;  
 $f_s$  is the sampling rate.  
 To obtain desired frequency content:  $f_c > f_m$ .  
 To avoid aliasing in the pass-band:  $f_s \geq 2 f_c$ .

Figure 28 – Filtering and sampling frequencies

#### 1.4.4 Multiplexer

The effective switching rate for the multiplexer shall be compared to the requirements for each measurand. Because the A/D converter is sampling several channels sequentially, the sampling rate for each channel is reduced in proportion to the number of channels.

The switching system is mostly either of a relay or a solid state switching type. Relay switching is usually more accurate than the solid state switching, but has a lower switching rate. When switching between different voltage levels, be aware of interference effects between neighbouring channels. Generally, these errors increase with the switching rate.

#### 1.4.5 Analog-to-digital converter

Before the continuous analog signal can be read by the computer, the signals must be converted into digital numbers.

Important parameters for analog-to-digital converters are the conversion time, resolution, accuracy, input range, temperature drift and linearity.

The resolution of an A/D converter is defined as the number of bits the converter uses to describe the analog signal. A 3-bit converter divides the range into  $2^3 - 1 = 7$  divisions.

For performance tests, a minimum requirement would be a 14-bit resolution. For dynamic measurements, a lower resolution can be accepted.

To obtain simultaneous measurements during A/D conversion, one A/D converter per channel and a simultaneous sample-and-hold equipment can be used.

#### 1.4.6 Computer

The controller in the data acquisition system is the computer. It shall have the following functions: to configure and synchronize the data logger, handle data transfer, communicate with peripheral equipment, perform calculations and present results.

The computer interface should have a selectable data transfer rate (baud rate in bits/s) enabling it to communicate with and control different devices on the bus.

#### 1.4.7 Data processing

Typical software tasks are:

- control of the data acquisition system;
- calculation of calibration coefficients;
- conversion of electrical values into engineering units;
- calculation of average values and other statistics;
- calculation of data;
- evaluation of random uncertainty;
- presentation of results;
- data storage.

The raw data for each parameter in an acceptance performance test shall be available after the evaluation of a test point in order to perform a manual calculation and verify the computer code.

If possible, essential performance data should be continuously displayed during the test to give an overview of model performance together with the hydraulic system to which it is connected.

The number of samples and the sampling rate shall reflect the characteristics of the complete measuring chain to give:

- an accurate mean value for performance measurements;
- a satisfactory determination of the necessary characteristics of oscillating measurements.

#### 3.1.5 Check of the data acquisition system

Each measuring chain shall have a complete schematic diagram showing its main components. This will help the parties to decide where checks should be made when particular problems occur, or when oscillating signals need to be more closely investigated. Figure 29 shows some typical measurement chains with suggested test and checkpoints.

##### 3.1.5.1 Transducer with analog output

In figure 29, point 1 is a test point for determining the dynamic behaviour of the measurand.

Proper operation of the signal conditioning system can be confirmed by correlating signals at input point A to test point 3.

Proper amplifier operation can be confirmed by correlating signals at input point A to test point 2.

Proper filter operation can be confirmed by correlating signals at input point B to test point 3.

To check the proper operation of the multiplexer and A/D converter, a reference signal can be applied to point C, and compared with the output at point 5.

##### 3.1.5.2 Transducer with frequency or scaled pulse output

The signal quality shall be controlled at point 4 to ensure proper triggering of the counter. A reference signal can be applied at D to check the timebase of the counter.

##### 3.1.5.3 Transducer with digitized output

The transducer and a measurement chain of this kind can best be checked during calibration.

##### 3.1.5.4 Check for bias effects

To check that the signal conditioning system does not give any bias effects, the output signal from the system may be correlated with the input signal. The latter could be a reference signal from a separate electrical source. The checkpoints are indicated in figure 29 at points A and 3.

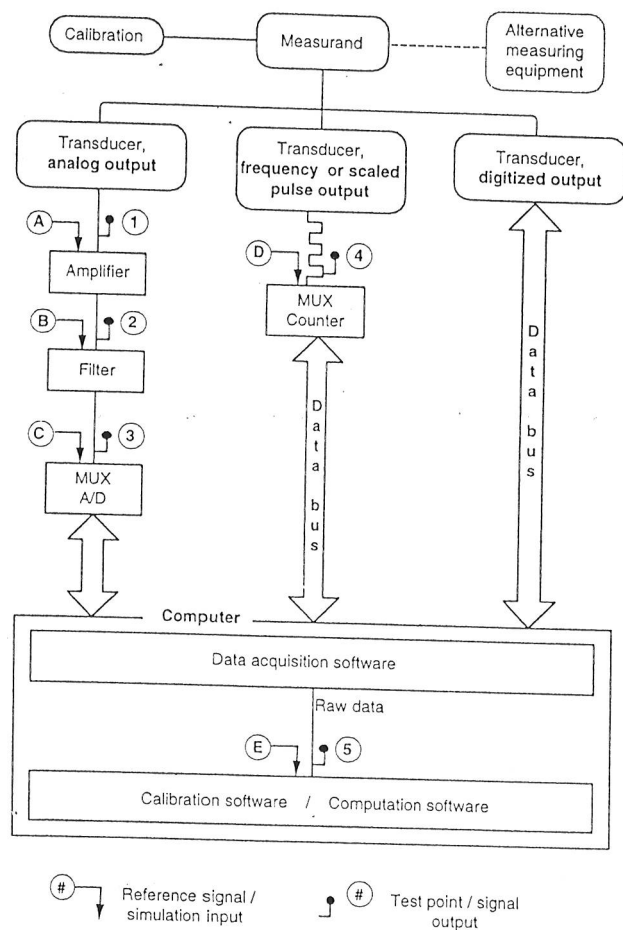


Figure 29 – Different measurement chains and their recommended checkpoints

### 3.1.5.5 Software

The software code can be verified by an alternative computation using the raw data read at control point 5, and comparing it with the result from the computer.

The performance algorithm can be verified by entering numerical values at E giving a known performance result.

It should be documented that the algorithms used for the calibration of a measuring chain are equivalent to those used in the performance computation.

## 3.2 Discharge measurement

### 3.2.1 General

As far as possible, there should be no loss or gain of water between the machine and the discharge measuring device. Nevertheless, if such auxiliary discharges exist, they shall be measured independently.

#### 3.2.1.1 Choice of the method of measurement

The methods which may be used for measuring the discharge during a model acceptance test can be classified into primary and secondary methods.

##### 3.2.1.1.1 Primary methods

Primary methods are those which need only measurements of fundamental quantities: length, mass and time. In the field of application of this standard, the primary methods which may be used are:

- the weighing method;
- the volumetric method;
- the moving screen method.

These methods are the most accurate. For this reason, and notwithstanding some inherent disadvantages (cumbersome equipment, duration of measurement, etc.), any model test facility shall necessarily include the possibility of using one of these methods; nevertheless, for convenience of use, it is generally supplemented by a secondary method.

##### 3.2.1.1.2 Secondary methods

Many other methods, founded on various principles and thus considered as secondary methods, may be used for discharge measurements in model tests. Although some of them are standardized, the high accuracy required for the purpose of this standard makes it mandatory to calibrate the measuring equipment *in situ* under the prevailing test conditions by one of the above primary methods. Consequently, and since repeatability is the most important quality required from the secondary method measuring device, it is not necessary for it to comply with all the requirements of the relevant standards.

The arrangements necessary to carry out such a calibration periodically, without dismantling or modifying the measuring line, shall be provided at the design stage of the test facility.

The main secondary methods of discharge measurement are:

velocity-area method by means of current-meters or Pitot tubes and tracer methods are very seldom used for model tests, and will not be mentioned in the following subclauses;

thin-plate weirs and differential pressure devices (orifice plates, nozzles and Venturi tubes), even when designed, installed and used in accordance with the relevant ISO standards, do not achieve the accuracy required for model tests, when using standardized discharge coefficients, therefore periodic calibration *in situ* is mandatory;

various types of flow meters, such as turbine, electromagnetic, acoustic or vortex flow meters; they are particularly convenient to use for they allow quick measurements, their output signal can easily be introduced into a data acquisition system and most of them generate little disturbance in the flow pattern. For the time being, the effect of installation conditions on their response is not established with sufficient accuracy for model tests. Thus, their calibration *in situ* is mandatory and their repeatability over the whole range of flow conditions to be encountered shall be checked regularly.

## 2.1.2 Accuracy of measurement

### 2.1.2.1 Reference to ISO standards

method of measurement is described in detail in the following subclauses only when no standardized procedure exists elsewhere. Whenever possible, reference has been made to existing standards, especially to those published by ISO, which are particularly suited to the precise requirements of this standard.

### 2.1.2.2 Evaluation of uncertainty

The numerical values of systematic uncertainty indicated in the following clauses are to be used only as guidance. They are valid only:

- with the best conditions for measurement;
- if all requirements specified in this standard and in the relevant standards are satisfied; and
- if the testing and analysis are carried out by qualified and experienced personnel.

If these conditions are not satisfied, there may be an unpredictable increase in both the systematic and random errors of the discharge measurement.

In each particular case, the actual values of systematic and random uncertainties shall be evaluated by the user, taking into account the whole measuring system and the operating conditions of the test facility.

The method for combining the random and systematic uncertainties associated with the individual sources of error is explained in 3.9.2.2.4. The final result is then expressed as the uncertainty at a confidence level of approximately 95 %.

### 2.1.2.3 Steadiness of the flow

Whatever method is used, a discharge measurement for a model acceptance test is valid only if the flow is steady or nearly steady during each point.

In most situations, the primary methods require a rather long time of measurement and produce only a mean value of the discharge during this time. Thus it is possible to ascertain a variation of the flow occurring between two runs, but not the possible fluctuations (see 2.3.2.3).

Most secondary methods quoted in 3.2.1.1.2. produce quasi-instantaneous readings which have to be averaged to obtain the mean value of the discharge during the point and which can be treated graphically and statistically to assess the nature and the extent of the fluctuations of the flow (see 3.1 and 4.2). This is another reason why a test facility should have access to a primary and a secondary method.

## 3.2.2 Primary methods

### 3.2.2.1 Weighing method

#### 3.2.2.1.1 Principle of the method

ISO 4185 gives all necessary requirements concerning the measuring apparatus, the procedure, the method for calculating the discharge and the uncertainties associated with the measurement. Although ISO 4185 specifies two alternative methods, the "static" and the "dynamic" method, only the static weighing methods, which consists of diverting the flow to the weighing tank for a measured time and then weighing the diverted quantity, is recommended for the purpose of this standard.

The weighing method, which gives only the average discharge value during the time taken to collect a suitable quantity of water, may be considered the most accurate method of discharge measurement.

As stated in ISO 4185, the calibration of the weighing device shall be periodically checked at least every two years for a mechanical weigh-beam and every year for a load cell. These intervals may be extended if the calibration history shows stable results.

#### 3.2.2.1.2 Uncertainty of measurement

The weighing method is affected by errors relating to weighing, measuring of filling time, determination of density, taking into account the temperature of the fluid and motion of the diverter. Furthermore, a buoyancy correction must be made to the readings of the weighing machine to account for the difference between the upthrust exerted by the atmosphere on the liquid being weighed and on the reference mass used during the calibration of the weighing device.

If the installation is carefully constructed, maintained and used, a systematic uncertainty on the discharge measurement (at a confidence level of 95 %) within  $\pm 0,1$  % to  $\pm 0,2$  % should be achieved.

### 3.2.2.2 Volumetric method

#### 3.2.2.2.1 Principle of the method

ISO 8316 gives all necessary requirements concerning the measuring apparatus, the procedure, the method for calculating the discharge and the uncertainties associated with the measurements.

Although ISO 8316 specifies two alternative methods, the "static" and the "dynamic" methods, only the static gauging method is recommended in this standard.

The volumetric method is approximately of the same accuracy as the weighing method and similarly supplies only the average discharge value during the time taken to collect a suitable quantity of water.

As stated in ISO 8316, the calibration of the volumetric tank shall be periodically checked; at least every five years for concrete tanks and every three years for metallic tanks. These intervals may be extended if the calibration history shows stable results.

### 2.2.2.2 Uncertainty of measurement

The volumetric method is affected by errors relating to the calibration of the reservoir, the measurement of levels, the measurement of filling time and the motion of the diverter. The water tightness of the reservoir shall be checked and a leakage correction applied if necessary.

If the installation is carefully constructed, maintained and operated, a systematic uncertainty (at confidence level of 95 %) within  $\pm 0,1$  % to  $\pm 0,2$  % can be achieved.

### 2.2.3 Moving screen method

#### 2.2.3.1 Principle of the method

The principle of the method is, to a certain extent, similar to the volumetric method, for it is based on the determination of the volume of water displaced in a channel between the cross-sections A and B, by means of a screen moving with the water (see figure 30). The discharge is calculated by the following formula:

$$V = b \cdot d \cdot L$$

$$Q = \frac{V}{t} = b \cdot d \cdot \frac{L}{t} = b \cdot d \cdot v$$

where

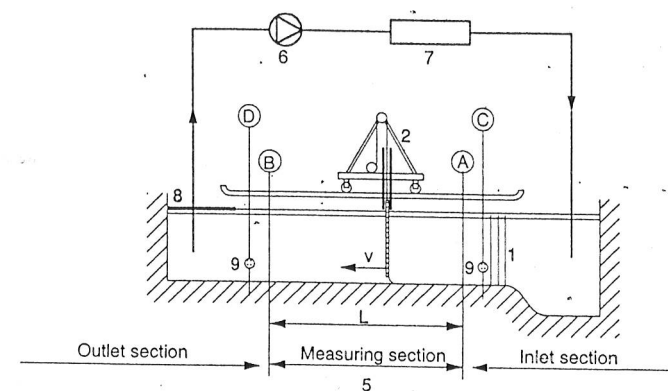
- $V$  is the displaced volume of water between cross-sections A and B;
- $L$  is the distance between the cross-sections A and B (length of measuring section);
- $b$  is the mean width of the channel within the measuring section;
- $d$  is the mean depth of water in the channel within the measuring section;
- $t$  is the travel time of the screen between cross-sections A and B;
- $Q$  is the mean discharge during travel time  $t$ ;
- $v$  is the mean flow velocity within the measuring section of the channel.

#### 2.2.3.2 Measuring equipment

##### 2.2.3.2.1 Channel

The measuring channel shall be a straight horizontal section, generally rectangular, precisely calibrated over the entire path of the screen travel. The width and depth of the channel shall be such that, for the range of discharge to be measured, the velocity lies within 0,05 m/s to 1 m/s.

The water supply of the channel shall ensure a regular velocity distribution, free of swirl, symmetry and excessive turbulence. This may be achieved by means of straightening devices (perforated plates, honeycomb, etc.).



- 1 Straightening devices
- 2 Moving screen and carriage
- 3 Measurement of water level
- 4 Measuring wells
- 5 Measurement of travel time
- 6 Booster pump of test circuit
- 7 Flowmeter of the test rig to be calibrated
- 8 Plate cover to reduce the downstream free water surface
- 9 Perforated plate, flush with the wall

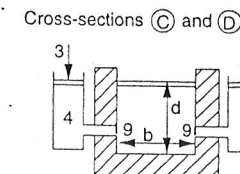


Figure 30 – Moving screen method

The total length of the channel includes:

- an inlet section, where the screen is introduced in the water and reaches uniform motion;
- a measuring section, the length of which is very accurately determined;
- an outlet section, where the screen is extracted from the flow.

The cross-sectional area of the channel corresponding to a given water level can be determined by geometric measurements. All the geometric dimensions involved shall be periodically checked, recommended every five years. Dimensional changes due to thermal expansion and strain due to the weight of the water may need to be taken into account in extreme conditions.

##### 3.2.2.3.2.2 Screen

The screen is generally suspended from a carriage rolling on rails installed along the length of the channel or supported by fluidic guide-blocks. The use of a floating screen should preferably be avoided.

The screen is often constructed of a light rigid material mounted on a lightly built frame. The carriage and screen assembly shall be as light as possible and friction shall be reduced to a minimum or compensated for by means of a driving motor such that the screen velocity will rapidly equal the mean water velocity and will move smoothly even at the lowest velocity.

It is essential that the introduction of the screen into the channel shall disturb the flow as little as possible and not initiate ripples or waves resulting in serious errors. One possible way to ensure this is to accelerate the screen carriage by means of an electric drive unit in order to give it approximately the same speed as the water velocity before the screen is lowered into the water.

The clearance between the screen and the walls and bottom shall be as small as possible in order to minimize the leakage. It is good practice to fit flexible lip seals to the screen provided that their friction is negligible or is compensated by a driving motor.

#### 3.2.3.2.3 Measurement of travel time

Screen travel time shall be measured between two fixed points installed at the beginning and end of the measuring section. When passing these points, the screen actuates an electronic timer through electro-mechanical, optical or magnetic switches.

#### 3.2.3.2.4 Measurement of water level

The level shall be measured before, during and after the travel time of the screen by means of measuring wells located in the walls on each side upstream and downstream of the measuring section. They shall be fitted with point or hook gauges or high accuracy pressure transducers or measuring apparatus, see 3.4).

It is essential that the level remains constant (e.g. within 0,5 mm) between the front and rear of the screen. This confirms that the moving screen velocity is equal to the water velocity.

In order to obtain high accuracy it is important to reduce slow mass oscillations (e.g. from adjustment of discharge) in the calibration channel. In order to observe such oscillations the free water surface downstream of the measuring section shall be reduced as far as possible. Mass oscillations may then be observed as variation of the water level, which may thus be used to indicate stable conditions.

#### 3.2.3.2.5 Controls before and during the run

Before starting a run, it is essential to check that the indication of the water level is constant in order to ensure that no oscillations occur within the channel.

Uniform velocity of the screen is essential to avoid ripples and waves which might substantially increase the uncertainty of measurement. This can be checked by means of a few supplementary switches evenly distributed along the measuring reach in order to determine intermediate travel times.

It is also important that any leakages from one side of the screen to the other are as small as possible. This can be checked by injecting a dye liquid near the wall and bottom seal.

Nevertheless, slight disturbances in the front and the rear of the screen or very small leakages, especially in the vicinity of the free surface, are often observed and in no way indicate faulty operation of the apparatus.

The time interval between two consecutive runs shall be of adequate duration to dampen the perturbation in the channel caused by the previous run.

#### 3.2.2.3.3 Uncertainty of measurement

If the installation is carefully constructed, maintained and used, and if the above requirements are satisfied, a systematic uncertainty (at the 95. % confidence level) on the discharge measurement within  $\pm 0,2$  % to  $\pm 0,3$  % can be achieved.

#### 3.2.3 Secondary methods

##### 3.2.3.1 General requirements

Various types of flowmeter may be used by agreement under the following conditions:

- the device chosen shall be of the best quality available, particularly with respect to its repeatability and its sensitivity to influence quantities (ambient temperature, frequency and voltage of the power supply, etc.);
- the flowmeter and the associated measuring system shall be calibrated by a primary method in the actual operating conditions (see 2.3.3.2.3 and 3.2.3.8);
- the repeatability of the measurement shall be checked over the whole range of discharge to be measured.

Although their application is not mandatory, the relevant standards and manufacturer's instructions give useful advice concerning the best installation and measurement conditions.

The types of flowmeter most often used are described in 3.2.3.2 to 3.2.3.7.

##### 3.2.3.2 Weirs

Only rectangular or triangular sharp-edged thin-plate weirs may be used within the scope of this standard.

For the design of the weir, its installation and the conditions for measuring the head over the weir, ISO 1438-1 should be referred to; however, the standardized discharge coefficients will not achieve the required accuracy (see 3.2.1.1.2). In addition, weirs are very sensitive to any change in the distribution of approach velocity and in the condition of the plate (roughness of the upstream face, cleanliness and sharpness of the edge, etc.).

The weir is commonly located on the low pressure side of the machine, and care shall be taken to ensure that smooth flow (free from eddies, surface disturbances or significant amounts of entrained air) exists in the approach channel.

When the weir is located on the outlet side of the machine being tested, it shall be far enough from the machine or the discharge conduit outlet to enable the water to release its air bubbles before reaching the weir. Stilling screens and baffles shall be used when necessary to give a uniform velocity distribution over the whole cross-section. Disturbed surface or undercurrents, or asymmetry of any kind, shall be corrected by suitable screens.

##### 3.2.3.3 Differential pressure devices

Orifice plates, nozzles or Venturi tubes may be used for discharge measurement in model test facilities, particularly operating on closed circuit without a free water surface.

For the design of the differential pressure device, including its pressure tapings, its installation and operating conditions, refer to ISO 5167-1; however the standardized discharge coefficients will not achieve the accuracy required in this standard (see 3.2.1.1.2). Other types of differential pressure devices than those described in ISO 5167-1 may also be used.

Differential pressure devices offer high reliability, but are very sensitive to the flow pattern and create a high pressure loss, particularly orifice plates and nozzles.

The differential pressure generated by the device shall be measured in accordance with 3.3.4.

The connecting pipes between the primary device and the pressure gauge shall conform with ISO 2186.

Precautions should be taken to avoid cavitation.

### 2.3.4 Turbine flowmeters

Turbine flowmeters, which generally include a flow straightener, require a minimum upstream and downstream straight length and generate only very slight disturbance of the flow, but create a somewhat high pressure loss. The output signal, which is a frequency measurement, is simple to measure without loss of accuracy. Care shall be taken to maintain the bearings in good condition and to maintain the blades of the turbine clean. The calibration shall be checked at least after each maintenance.

Since cavitation on the runner blades can occur in low pressure conditions, calibration shall be checked at the lowest test pressure (see 3.2.3.8).

### 2.3.5 Electromagnetic flowmeters

Electromagnetic flowmeters are the subject of ISO 6817 and ISO 9104.

The main advantages of electromagnetic flowmeters are that they generate neither disturbance of the flow, nor pressure loss, and are not very sensitive to wear. They produce an instantaneous reading of discharge and thus are particularly convenient for observing discharge fluctuations. Care shall be taken to detect any drift in the electronic circuitry output signal in the surface condition of the electrodes. The calibration shall be checked at least after each maintenance.

### 2.3.6 Acoustic flowmeters

Several methods of acoustic discharge measurement exist. Currently available knowledge is such that the method preferred for the purpose of this standard is that based on the measurement of the transit time of acoustic pulses travelling upstream or downstream, preferably including several parallel paths.

The data acquisition and processing system shall demonstrate that the equipment is operating correctly (separate measurement of the average velocity along each individual path, verification of the speed of sound, checking of the proportion of lost pulses, etc.).

More details on this method are given in IEC 60041.

Other kinds of acoustic flowmeters, based, for instance, on the measurement of the refraction of an acoustic beam by fluid velocity, or on the cross-correlation of acoustic signals emitted in two cross-sections, may also be used.

Acoustic flowmeters have the advantage of not introducing any flow disturbance or pressure loss, but are somewhat sensitive to the velocity distribution and to the presence of gas bubbles and acoustic noise. Their sensitivity to turbulence and limited sampling of local instantaneous velocities do not allow the use of successive readings to assess the level of discharge fluctuations.

### 3.2.3.7 Vortex flowmeters

The principle of vortex flowmeters is based on measuring the frequency of vortex-shedding generated by a bluff body inserted in the flow, the frequency of which is proportional to the mean velocity in a given range of Reynolds numbers.

Although many devices of this type are available, experience with this method of discharge measurement is still limited and the method shall only be used with caution. For instance, any vibration of the pipe is liable to alter the measured frequency and shall thus be avoided.

Due to the risk of cavitation on the bluff body of the vortex flowmeter, the calibration shall be checked at the lowest test pressure (see 3.2.3.8).

### 3.2.3.8 Calibration procedure

As stated above, any device used for discharge measurement by a secondary method shall be calibrated against one of the primary methods described in 3.2.2. The calibration shall be made without dismantling the flowmeter from the test circuit or modifying the flow conditions at the inlet of the flowmeter.

Calibration shall include the whole of the flowmeter and the associated measuring system: for instance an orifice plate, the connecting pipes, the pressure transducer, its power supply and the data acquisition system.

Calibration normally should be carried out in the actual operating conditions (pressure, temperature, water quality, etc.) prevailing during the tests. Should the pressure encountered during the tests be lower than the minimum pressure attainable in the open circuit used for calibration, it shall then be demonstrated that the flowmeter calibration is not affected by cavitation at that reduced pressure. This may be achieved by using two secondary flowmeters in series, one of which is not sensitive to cavitation effects. It is not permitted to make a discharge measurement with a flowmeter affected by cavitation, even if calibrated in the same operating conditions, as the phenomena involved are not sufficiently reproducible.

Any calibration shall include sufficient measuring points evenly distributed over the whole range of discharge to be measured during tests, to allow an accurate evaluation of their scattering.

In most cases, the result of a calibration can be written, at least in the range of use, as  $Q = CR^\alpha$ , where

$R$  is the output signal delivered by the secondary flowmeter;

$\alpha$  is an exponent which is known by theoretical considerations ( $\alpha = 1$  when  $R$  is the frequency of a turbine meter,  $\alpha = 1/2$  when  $R$  is the differential pressure of a Venturi tube,  $\alpha = 3/2$  when  $R$  is the head over a rectangular weir, etc.);

$C$  is a discharge coefficient which may be constant or variable over the range of the meter.

It is thus possible to plot the discharge coefficient versus the discharge indicated by the primary method or preferably versus the corresponding non-dimensional coefficient appropriate to the type of flowmeter (Reynolds number for flowmeters in closed conduit, Froude number for weirs).

In any case, the best fitted curve (often a straight line) through the measured points should be determined by a regression technique such as the least squares method. Guidance for deriving this calibration curve and evaluating the associated uncertainty may be found in ISO 7066 (see also annex H).

The secondary flowmeter should normally be calibrated before and after the test (see 3.3.1.5). If a significant difference appears between both calibrations<sup>1)</sup>, the flowmeter and the associated measuring system shall be carefully inspected to find the reason for this deviation and the test may possibly be rejected. A historical record of the flowmeter calibration should be available for inspection and analysis. If no systematic trends occur, an average of all obtained values may be a better approximation of the true value than the mean of the two values obtained before and after the test.

### 3 Pressure measurement

#### 3.1 General

This clause deals only with the measurement of the time-averaged value of the pressure, whereas the measurement of pressure fluctuations is described in 4.3. Pressure measurements in hydraulic machinery are made in order to determine:

- quantities of the hydraulic performance such as
  - specific hydraulic energy  $E$  (see 3.5.2 and 3.5.3) and
  - net positive suction specific energy NPSE (see 3.5.4);

gauge pressures or differential pressures at special locations of the water passage in the model for various purposes: for example to measure the discharge utilizing differential pressure devices (see 3.2.3.3) or to obtain information on

- local pressure;
- pressure distribution;
- index testing (values to be converted to site conditions).

The pressure  $p$  is measured as single gauge pressure or differential pressure at steady-state conditions.

#### 3.2 Choice of pressure-measuring section

Special attention shall be paid to the location of the measuring sections; normally they are entical to the reference sections. There should be minimum disturbance of the flow. The high pressure and low pressure reference sections 1 and 2, specified by the contract, should normally fulfil these conditions. However, under exceptional circumstances where the velocity distribution of the reference section is considerably distorted this section should be replaced, if possible, by other measuring sections as close as possible to the reference section and offering better flow conditions.

The plane of the measuring section should preferably be normal to the average direction of flow. Its cross-sectional area, which is required for computing the mean water velocity, shall be readily measurable.

The measuring section should preferably be arranged in a straight conduit section but could be tightly convergent or divergent.

<sup>1)</sup> It may be agreed that the relative deviation  $2(Q_1 - Q_2) / (Q_1 + Q_2)$  shall be less than a permissible value specified prior to the test (for instance 0,1 %),  $Q_1$  and  $Q_2$  being the readings of the secondary flowmeter delivered before and after the test for the same discharge given by the primary method.

### 3.3.3 Pressure taps and connecting lines

#### 3.3.3.1 Number and location of pressure taps

Generally, for any form of section at least two pairs of opposed pressure taps shall be used (four pressure taps). In the case of circular sections the four pressure taps shall be arranged on two diameters at right angles to each other. The taps should neither be located at or near the highest point of the measuring section in order to avoid air pockets, nor near the lowest point because of the risk of dirt obstructing the taps.

In the case of non-circular sections (in most cases rectangular sections) the taps should not be located near the corners. If taps are arranged at the top or bottom of a section, special care has to be taken to avoid disturbances due to air or dirt.

If the flow conditions are disturbed or asymmetric, more than four pressure taps shall be used.

Individual mean pressure measurements at the same measuring section shall not differ from one another by more than 0,5 % of the specific hydraulic energy of the machine or, for low head machines, by more than 20 % of the specific kinetic energy calculated from the mean velocity in the measuring section (see 3.5.2.4), both referring to operation close to the best efficiency point.

If this requirement is not fulfilled, mutual agreement should be reached either

- to select another location; or
- to make an evaluation of the specific kinetic energy distribution in the measuring section according to 3.5.2.4; or
- to accept this deviation, and add arithmetically an additional uncertainty to the measurement uncertainty in the specific hydraulic energy  $E$  (see 3.5.2.5 and J.2.3).

### 1.3.2 Design of pressure taps

Pressure taps shall be located in inserts of non-corroding material. Figure 31 shows typical inserts which shall be installed flush with the wall of the conduit.

The cylindrical bore of the pressure tap shall be 2 mm to 4 mm in diameter and have a minimum length  $\ell$  of at least twice the diameter. It shall be perpendicular to the conduit wall and free of all burrs or irregularities which could cause local disturbances. The edges of the openings shall be sharp or rounded with a radius  $r \leq d/4$  smoothly joining the flow passage. The purpose of this rounding is to eliminate possible burrs.

The surface of the conduit shall be smooth and not be curved in the flow direction in the vicinity of the bore for at least 100 mm upstream and downstream.

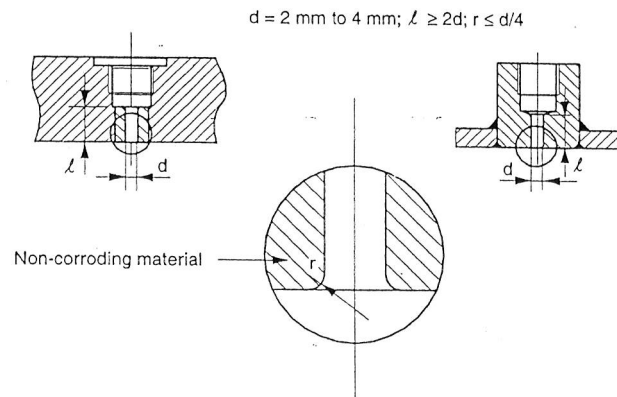


Figure 31 – Examples of pressure taps

### 3.3.3.3 Gauge piping

Pressure taps may be manifolded (figure 32), but each tap shall be separately valved so that it can be read individually. The diameter of the connecting piping shall be at least twice that of the tap and not less than 6 mm. The diameter of the manifold (or of the ring manifold, figure 32b) shall be at least three times the diameter of the tap. Connection pipes should, if possible, be of equal length, slope upward to the gauge or manometer with no intermediate high spots where air may be trapped. Valves with a gas-collecting chamber shall be provided at all high points for flushing out air. Transparent plastic piping, available for a wide pressure range, is recommended as it is useful in disclosing the presence of air bubbles. However, in the case of pressure fluctuations, the damping effect existing in plastic pipes shall be considered (see 3.3.3.4). No leaks shall be permitted in the gauge connections.

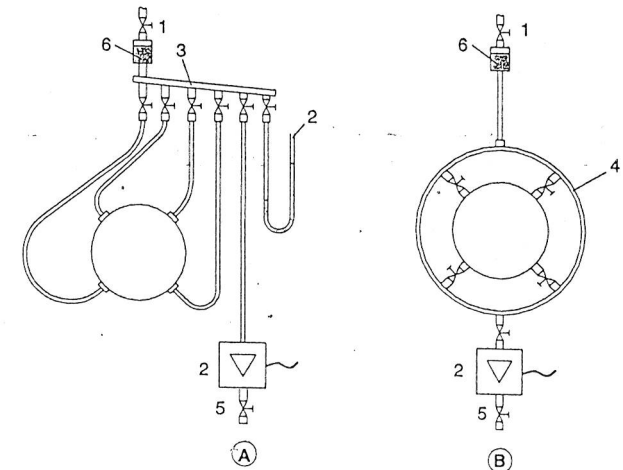


Figure 32a – Separate connecting pipe to manifold

Figure 32b – Ring manifold

- 1 Vent
- 2 Pressure measuring instrument
- 3 Manifold
- 4 Ring manifold
- 5 Drain
- 6 Gas-collecting chamber

Figure 32 – Types of pressure manifolds

### 3.3.4 Damping devices

Whenever possible, all measurements shall be made under steady-state conditions and ensure fluctuations eliminated at their source. In particular, no fluctuations requiring a damping arrangement for a manometer shall occur in the range of normal operation.

certain ranges of operation (low values of  $Q$  and  $\sigma$ , etc.), fluctuations cannot be avoided. In order to obtain correct readings on a pressure measuring instrument under such conditions, a suitable damping device may be installed, provided the flow through it is laminar and equal in distance in both directions, thus ensuring a linear viscous resistance. This may be secured using a capillary tube of about 1 mm bore and suitable length or a specially designed valve. Damping device can also be obtained by using long plastic tubes. Additional damping may be obtained from an air or surge chamber connected to the pressure line ahead of the gauge. The use of an orifice plate is not recommended because it may introduce error due to non-linear damping. A valved bypass around any throttling device shall be provided and kept open except the short time during which readings are taken. Bending or pinching the connecting pipes or inserting any non-symmetrical throttling device (e.g. a valve) is not permitted.

## 3.4 Apparatus for pressure measurement

### 3.4.1 Types of apparatus

Apparatus for pressure measurements fall into two classifications:

**primary methods** (or instruments), such as liquid column manometers (see 3.3.4.2), dead weight manometers (see 3.3.4.3) and pressure weighbeams (see 3.3.4.4); these methods use only measurements of fundamental quantities (length, mass) and thus do not need any calibration;

**secondary methods** (or instruments), such as pressure transducers (see 3.3.4.5) and other apparatus such as spring gauges (see 3.3.4.6), which need to be calibrated against a primary method used as a standard.

The choice of the measuring apparatus shall take into account the requirements of an automatic data acquisition system. Often a combination of primary and secondary methods is applied.

The physical principles and typical examples of possible experimental set-ups are described in the following subclauses for various instruments.

### 3.3.4.2 Liquid column manometers (primary method)

Liquid column manometers are used to measure low pressures or small pressure differences (up to about  $5 \times 10^5$  Pa, when mercury is used as the manometer liquid). Mostly water or mercury column manometers are used (see figures 33a, 33b and 33c). In some cases other liquids of known density may be used.

The pressure measured with a liquid column manometer is determined by the following basic relation:

$$p = \rho \cdot g \cdot h$$

where

$h$  is the height of the liquid column;

$\rho$  is the density of the liquid used in the manometer and taken for the temperature of this liquid.

The tube of a water column manometer shall have a minimum inside diameter of 12 mm in the measuring range to minimize capillary effects. For mercury manometers, this diameter shall be at least 8 mm.

Common types of liquid manometers for gauge pressure or differential pressure are:

- a) single-limb manometer (standpipe)
  - mercury pot with standpipe (figure 33a)

If the manometer is calibrated or corrected for the change in level  $h_1$  in the pot, only the height  $h_2$  in the single limb need be read.

- water column (standpipe) (figure 33b)
- b) U-tube
  - normal U-tube (figure 33c)

The heights of the liquid columns in the two legs shall be read simultaneously, which can be achieved by optical reading. Whatever combination of liquid is used, the correct densities of both manometric liquids shall be used.

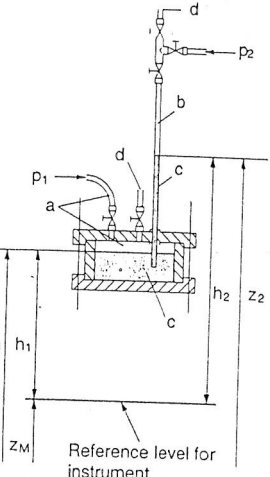
Manometer	Gauge pressure $p_2 = p_{amb}$ $p = p_{abs} - p_{amb}$	Differential pressure $p_2 \neq p_{amb}$ $\Delta p = p_1 - p_2$
Figure 33a - Pot with standpipe 	$p_M = \text{pressure at the reference level of instrument}$  $p_M = g [\rho_{Hg} (h_2 - h_1) + \rho h_1]$ $h_1 = z_1 - z_M$ $h_2 = z_2 - z_M$  $a = \text{water}$ $b = \text{air}$ $c = \text{mercury}$ $d = \text{vent}$	$\Delta p = g (\rho_{Hg} - \rho) (h_2 - h_1)$ $\Delta p = g (\rho_{Hg} - \rho) (z_2 - z_1)$  $a = \text{water}$ $b = \text{water}$ $c = \text{mercury}$ $d = \text{vent}$

Figure 33 – Liquid column manometer (example of experimental setup)  
(values of  $\rho$ ,  $\rho_{Hg}$  and  $\rho_a$  are given in annex B) (continued)

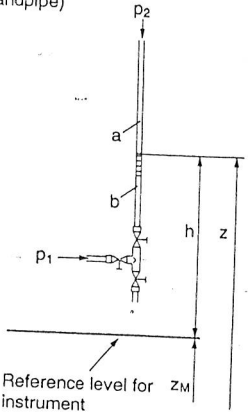
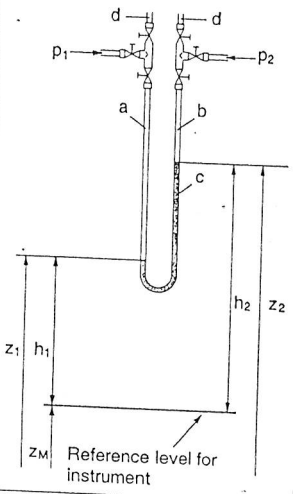
Manometer	Gauge pressure $p_2 = p_{amb}$ $p = p_{abs} - p_{amb}$	Differential pressure $p_2 \neq p_{amb}$ $\Delta p = p_1 - p_2$
Figure 33b - Water column (standpipe) 	$p_M = g \rho h$ $h = z - z_M$  $a = \text{air}$ $b = \text{water}$	Not applicable
Figure 33c - U - tube 	$p_M = \text{pressure at the reference level of instrument}$  $p_M = g [\rho_{Hg} (h_2 - h_1) + \rho h_1]$ $h_1 = z_1 - z_M$ $h_2 = z_2 - z_M$  $a = \text{water}$ $b = \text{air}$ $c = \text{mercury}$ $d = \text{vent}$	$\Delta p = g (\rho_{Hg} - \rho) (h_2 - h_1)$ $\Delta p = g (\rho_{Hg} - \rho) (z_2 - z_1)$  $a = \text{water}$ $b = \text{water}$ $c = \text{mercury}$ $d = \text{vent}$

Figure 33 (concluded)

### 3.3.4.3 Dead weight manometers (primary method)

Dead weight manometers (also called piston manometers) may be of the simple or differential type. Their application range depends on the effective piston area  $A_e$  and on the sensitivity of the mechanical piston system related to the pressure to be measured. For low pressures or low pressure differences, large effective areas  $A_e$  are used (e.g.  $A_e \approx 0,0005 \text{ m}^2$  for pressures down to about  $3 \times 10^4 \text{ Pa}$ ) and vice versa (e.g.  $A_e \approx 0,0001 \text{ m}^2$  for pressures  $> 2 \times 10^5 \text{ Pa}$ ).

The effective piston diameter  $d_e$  may be determined as the arithmetic mean value of the piston diameter  $d_p$  and bore diameter  $d_b$ :  $d_e = (d_b + d_p)/2$ .

This apparatus may be used for pressure calculation without further calibration if:

$$(d_b - d_p)/(d_b + d_p) \leq 0,001.$$

The pressure  $p$  measured at the lower end of the piston of a dead weight manometer loaded with the mass  $m$  is:

$$p = (gm)/A_e = (4gm)/(\pi d_e^2)$$

Dead weight manometers shall fulfil the following main conditions:

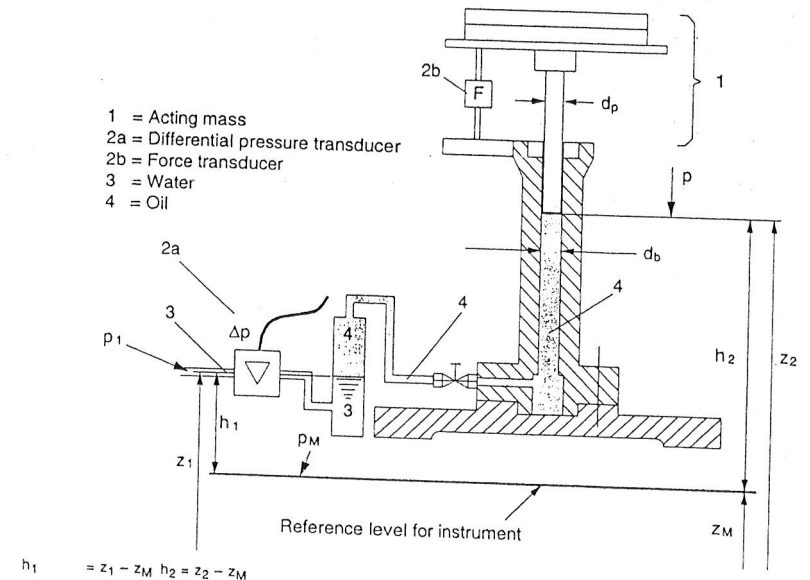
- the effective piston diameter  $d_e$  shall be determined within a relative uncertainty  $f_{de} < 5 \times 10^{-4}$ ;
- the friction between piston and bore shall be eliminated by rotating the piston slowly ( $0,25 \text{ s}^{-1} \leq n \leq 2 \text{ s}^{-1}$ ), and the cylinder shall be filled with a suitable fluid, usually by oil of low viscosity ( $\nu \approx 10^{-5} \text{ m}^2 \text{ s}^{-1}$ );
- the axis of the piston shall be vertical. All the acting masses (weights, piston, weight plate etc.) shall be calibrated.

When using a data acquisition system, it is recommended to use a set-up combining a dead weight manometer with a pressure or force transducer (see figure 34).

The correction curve for these set-ups shall be determined either by checking them against a calibrated dead weight manometer without compensating devices or by loading the weight plate at constant pressure with additional small weights of calibrated appropriate mass, so that the indicator of the compensator indicates zero.

Dead weight manometers of the above type connected to transducers or load cells are preferred for use with automatic data acquisition.

The sensitivity of a dead weight manometer in good condition is less than 0,002 kg, i.e. less than  $(0,02/A_e) \text{ Pa}$  (e.g.  $A_e = 0,0002 \text{ m}^2$ , sensitivity: 100 Pa).



$$h_1 = z_1 - z_M \quad h_2 = z_2 - z_M$$

$$p = (4mg)/(\pi d_e^2)$$

$$d_e = (d_b + d_p)/2$$

Case a: compensation by differential pressure transducer

$$p_M = p_1 + \rho g h_1 = p + \rho_{oil} g (h_2 - h_1) + \rho g h_1 + \Delta p$$

Case b: compensation by force transducer

$$p_M = p_1 + \rho g h_1 = p + \rho_{oil} g (h_2 - h_1) + \rho g h_1 + (4F)/(\pi d_e^2)$$

Figure 34 – Dead weight manometer with compensation by pressure or force transducer (example of experimental set-up)

### 3.3.4.4 Pressure weighbeam (primary method)

An extension of the dead weight manometer is the pressure weighbeam which comprises a weighbeam mounted on frictionless pivots, and bearing on one or more weight manometers or a differential type of weight manometer. The force exerted by the piston of the weight

manometer is balanced by a jockey weight moving along the weighbeam (figure 35). The operation of the weighbeam and jockey weight may be by hand or by an automatic servobalance system. The pressure weighbeam is in principle a primary method but in some cases needs to be calibrated.

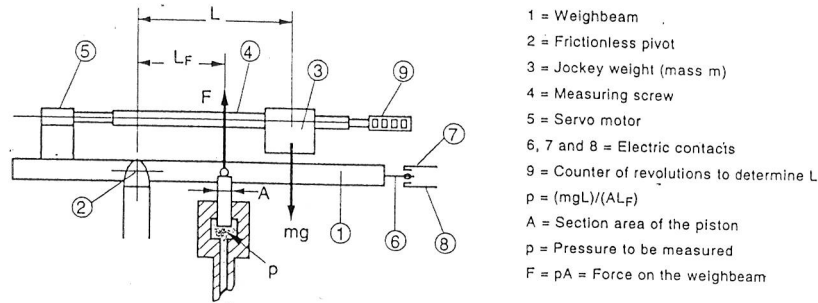


Figure 35 – Pressure weighbeam (example of experimental set-up)

### 3.3.4.5 Pressure transducers (secondary method)

Pressure transducers are electromechanical devices in which mechanical effects produced by pressure are converted into electrical signals.

Although pressure transducers are also used for measuring pressure fluctuations, this subclause deals only with static pressure measurements in steady state conditions, in order to obtain the mean value.

Depending on the pressure to be measured, the appropriate range for the pressure transducer shall be selected.

Some advantages in using pressure transducers are:

- easy integration into electronic data acquisition systems;
- they usually require negligible fluid flow through pressure taps thus providing rapid and accurate response;
- average values of fluctuating pressure or pressure differences, as well as records of transient phenomena, are easily obtained using readily available electronic equipment.

The pressure transducers should have the following characteristics:

- sufficient calibration stability;
- high repeatability, negligible hysteresis;
- low zero shift and low temperature sensitivity;
- no influence by bias effect when charged by pressure.

Operation with and without filters on the electronic equipment should be conducted to ascertain the absence of bias when filters are operating.

The complete pressure transducer system shall be calibrated under the test pressure conditions. The accuracy of a transducer will mainly be determined by the accuracy of the calibration. The calibration shall be carried out using a primary method, for example a dead weight manometer, which allows checking of the measurements of the transducer system at any time during the test.

To reduce the systematic uncertainty, it is also recommended to install two similar transducer systems in parallel and to take simultaneous readings during the test. The transducer systems are to be checked before and after the tests and if the two systems show readings that differ more than their systematic uncertainty, a comparison with a primary method shall be effected.

### 3.3.4.6 Other apparatus such as a spring pressure gauge (secondary method)

This type of gauge uses the mechanical deflection of a loop of tubing (plan or spiral) or of a diaphragm to indicate pressure. Depending on the pressure to be measured, the corresponding range for a spring pressure gauge shall be selected. It may be used by mutual agreement provided the gauge is of suitable accuracy, is used within its optimum measuring range (usually between -60 % and -100 % of full scale) and is suitably calibrated against a primary method before and after the test.

## 3.3.5 Calibration of pressure measurement apparatus

### 3.3.5.1 General procedure of calibration

As already mentioned, the pressure measured with secondary methods (spring gauges or transducers) shall be checked or calibrated. This can be done by comparison against primary methods (see 3.3.4.2 and 3.3.4.3) or by comparison with the static pressure obtained by a free water level as described in 3.3.5.2, or with an authorized standard.

It might also be useful to check the influence of the measuring and data acquisition system by means of a dynamic calibration, utilizing a pressure fluctuation generator of variable frequency and known average value, to ensure that no bias exists to affect the average value of the static pressure measurement.

### 3.3.5.2 Comparison of gauge pressures with a well defined static pressure obtained from free water level

Before and after the acceptance test and, if necessary, during the test, the readings of the pressure gauge  $p_M$  may be compared with the static pressure for zero discharge, obtained from a free water level taking into account the buoyancy of water in air:

$$p = (p - p_a) \cdot g \cdot \Delta z$$

## 3.3.6 Vacuum measurements

### 3.3.6.1 General requirements

For vacuum measurements, 3.3.2 to 3.3.4 also apply, except as indicated in 3.3.6.2.

### 3.3.6.2 Gauge piping for vacuum measurements

The gauge piping shall either be completely filled with water or, if air is used, shall be transparent to permit observation of the water level, if present. Such pipes, when filled with water, shall be flushed carefully and frequently between runs to remove any air coming out of solution or entering through the pressure tap and to maintain the water in the gauge piping at the same temperature as in the conduit. All piping and connections shall be airtight (free from leaks). Flexible pipes may be used as gauge pipes only if they are sufficiently rigid to avoid distortion or collapse by ambient pressure. Transparent plastic tubing is very convenient for observing air bubbles.

### 3.3.7 Uncertainty in pressure measurements

Estimations for the absolute systematic uncertainties  $e_p$  (at 95 % confidence level) that could be expected<sup>1)</sup>:

- liquid column manometers
  - mercury / water  $\pm 50 \text{ Pa to } \pm 300 \text{ Pa}$
  - water / air  $\pm 10 \text{ Pa to } \pm 50 \text{ Pa}$
- dead weight manometers  $\pm (1 \text{ to } 3) \times 10^{-3} p$
- pressure weighbeams  $\pm (2 \text{ to } 5) \times 10^{-3} p$
- spring pressure gauges  $\pm (3 \text{ to } 10) \cdot 10^{-3} p_{\max}^2)$
- pressure transducers  $\pm (1 \text{ to } 5) \cdot 10^{-3} p_{\max}^2)$

### 3.4 Free water level measurement<sup>3)</sup>

#### 3.4.1 General

In general, the determination of the specific hydraulic energy of the model machine should be based on pressure measurement within the water passages in accordance with 3.5.1.2.

In test stands with free and stable water levels, the specific hydraulic energy can be determined on the basis of measurements of the free water levels (see 3.5.3.3).

The measurement of free water levels is also necessary for some methods of discharge measurements (see, for example, 3.2.2.2, 3.2.2.3 and 3.2.3.2).

#### 3.4.2 Choice of water level measuring sections

The measuring section for the determination of a free water level shall be chosen to satisfy the following requirements:

- a) if no special similarity requirements are imposed, the model shall be arranged so that the flow is steady and free of disturbances. Especially, the free water surfaces at the measuring sections shall be stable. Sufficient submergence should therefore be provided;
- b) the area used to determine the mean water velocity shall be accurately defined and readily measurable.

#### 3.4.3 Number of measuring points in a measuring section

Measurement of free water levels shall be obtained where possible for at least two points in every measuring section or in each passage of a multiple passage measuring section and the average of the readings taken as the free water level.

<sup>1)</sup> These values are valid for stable pressure conditions. It should be noted that pressure fluctuations at a pump high pressure side can be important and more or less unsymmetrical, so that when they are not correctly damped (see 3.3.3.4), the uncertainties may be increased.

<sup>2)</sup>  $p_{\max}$  is the full-scale reading of the instrument.

<sup>3)</sup> See also ISO 4373.

### 3.4.4 Measuring apparatus

Commonly, a free water level is measured from a reference level  $z_M$  of the instrument, determined by means of a high precision instrument in relation to other reference levels.

The free water level is generally not measured directly in the section but in a stilling well connected to the measuring section as shown in figure 36.

#### 3.4.4.1 Point or hook gauge

Point or hook gauges (see figure 37) may be used to determine the level of calm water, preferably in stilling wells or directly in the flow if the free level is particularly undisturbed. In place of the normal visual indication of contact with the water, electrical, optical or other indicators may be used, provided they are calibrated against the direct visual method.

#### 3.4.4.2 Float gauge

Float gauges may be used where the water level varies a great deal. The float diameter shall be at least 150 mm. The minimum dimension of a stilling well shall be 200 mm. Gauges shall be sensitive within 1 mm when manually displaced from the true reading (resolution of  $\pm 0,001 \text{ m}$ ).

#### 3.4.4.3 Pressure measuring device

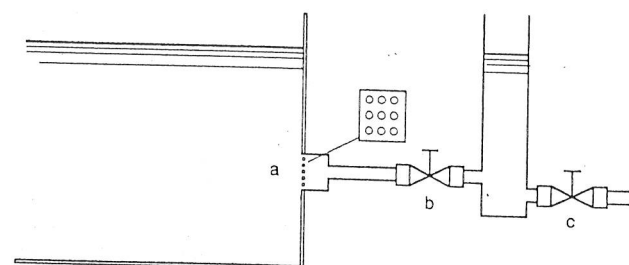
Immersible pressure transducers or any other pressure measuring device, including liquid manometers (standpipe) may be used (see 3.3) to determine the free water level. The pressure indication shall be checked with no water flowing.

#### 3.4.4.4 Bubbler with compressed air

The free water level may also be determined by means of the pressure inside a tube filled with compressed air, the so-called gas purge "bubbler" technique (for detailed information see IEC 60041).

#### 3.4.4.5 Other methods

Other methods may be used, for example ultrasonic devices and capacitive methods, as long as they meet the required accuracy (see 3.4.5).



$$A_p \geq 0,05 A_c$$

- a Perforated plate, flush with the wall  
 b Disconnecting valve  
 c Flushing valve  
 $A_p$  Total cross-sectional area of perforation  
 $A_c$  Cross-sectional area of the well

Figure 36 – Stilling well

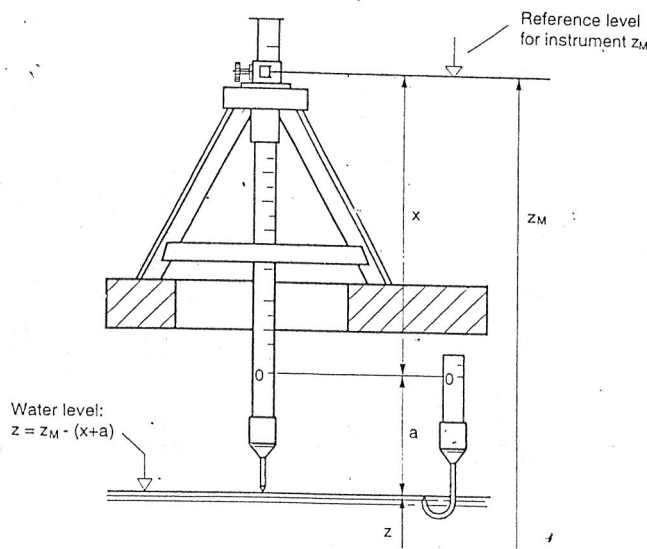


Figure 37 – Point and hook gauges

### 3.4.5 Uncertainty in free water level measurement

Estimations for the absolute systematic uncertainties  $e_z$  (at 95 % confidence level) that could be expected in the case of calm water conditions and velocity smaller than or equal to 1,0 m/s (the lower value referring to a velocity close to zero):

- point or hook gauges  $\pm 0,001 \text{ m to } \pm 0,003 \text{ m}$
- float gauges  $\pm 0,001 \text{ m to } \pm 0,003 \text{ m}$
- immersible pressure transducers  $\pm (0,5 \text{ to } 5) \times 10^{-3} z_{\max}^1)$
- bubbler with compressed air  $\pm 0,001 \text{ m to } \pm 0,003 \text{ m}$
- ultrasonic device  $\pm 0,002 \text{ m to } \pm 0,010 \text{ m}$

In the case of very turbulent flow and  $v > 1,0 \text{ m/s}$ , for example near the outlet of a turbine draft tube, the uncertainties may be considerably higher.

## 3.5 Determination of E and NPSE

### 3.5.1 General

#### 3.5.1.1 Object

The specific hydraulic energy E of the machine shall be determined in any test on a hydraulic model machine and the net positive suction specific energy NPSE determined when required. The quantities for the determination of E and NPSE are measured at steady-state conditions as an average over time. The formulae for their evaluation are given in 1.3.3.6.2 and 1.3.3.6.5 respectively.

Annex C provides the derivation of the formula for E.

#### 3.5.1.2 Method of determination

To determine the specific hydraulic energy acting on the model machine, it is necessary to evaluate the specific energy of water in the high pressure and low pressure reference sections. For the net positive suction specific energy, the specific energy of water is evaluated in the low pressure reference section with reference to a specified level. Whenever possible, the absolute pressure, the mean velocity and the elevation should be directly determined in the reference sections, in particular at the low pressure side where the pressure shall be measured within the draft tube. In some cases, due to special model test equipment, it can be mutually agreed to choose a measuring section located as near as possible to the corresponding reference section or even to replace pressure measurements by free water level measurements. The measurement of the pressure is described in 3.3, whereas the measurement of free water level, although seldom used for model tests, is described in 3.4.

#### 3.5.1.3 Steady-state conditions and number of readings

Readings required to determine the specific hydraulic energy shall be taken at regular intervals and when steady-state conditions prevail as defined in 2.3.2.3.1. The number of readings and the intervals between them shall provide for a sufficiently good approximation of the mean value, taking into account the performance of the data acquisition system (see 2.3.2.3 and 3.1).

<sup>1)</sup>  $z_{\max}$  is the full scale reading of the instrument.

## 3.5.2 Determination of the specific hydraulic energy $E$

### 3.5.2.1 Measuring sections

#### 3.5.2.1.1 General

The basic conditions to achieve an accurate determination of the specific hydraulic energy are described in 3.5.1.2. Requirements for the choice of a pressure measuring section are given in 3.3.2.

#### 3.5.2.1.2 Shifted measuring sections

Model acceptance tests will generally be conducted with measurements at the reference sections of the machine which are specified in the contract. Only in exceptional cases may the measuring sections be different from the reference sections. This may become necessary if low disturbances occur at the reference section, caused by the machine or by the inflow conditions; such a shifting shall be agreed by the parties. In such cases, the components influencing the flow pattern may also be modeled, if contractually agreed.

#### Examples

For pumps, the high pressure measuring section should be moved if the pressure and velocity distributions are such that the calculation of specific hydraulic energy from the mean values would result in significant errors. A measuring section located some conduit diameters from the pump will generally increase the reliability of the measurement.

For turbines, a butterfly valve close to the high pressure reference section may necessitate relocating the measuring section since it is difficult to assess the effect of the valve on the measurement.

#### 3.5.2.1.3 Specific hydraulic energy correction for shifted measuring sections

When the measuring section is not the reference section, the loss of specific hydraulic energy between the measuring section and the reference section shall be taken into account, due consideration being given to the flow direction and distribution and the relative position of the two sections. Evaluation of this loss may be based on theoretical knowledge and/or practical experience.

Before a decision is made to use a different measuring section, due consideration shall be given to the uncertainty introduced by the loss calculation compared to that arising from unsatisfactory measuring conditions at the reference section.

### 3.5.2.2 Reference levels

#### 3.5.2.2.1 Reference datum

All elevations shall be referred to a reference datum such as a reference level of the test rig or the reference level of the machine (see 1.3.3.7.6). An example of main elevations and heights is shown in figure 38.

#### 3.5.2.2.2 Difference of elevations

It is only important to establish accurate differences of elevations. The most important difference of elevations for model tests is the difference between reference level of machine  $z_r$  and reference level of pressure measuring instrument  $z_M$ :  $Z_{rM} = z_r - z_M$ . If the reference level of all the pressure measuring instruments is the same and if it is taken as reference datum, then  $Z_{rM} = z_r$  (see figure 38).

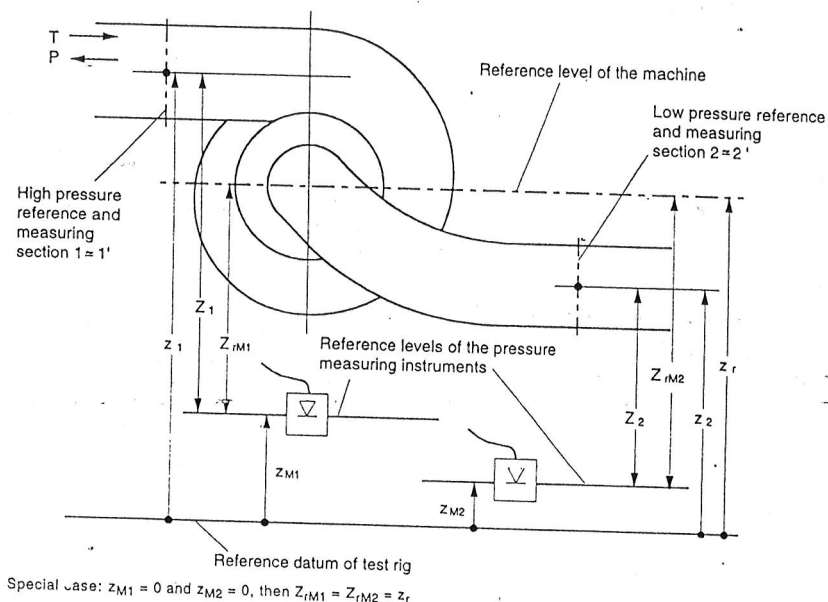


Figure 38 – Example showing main elevations, heights and reference levels of the test rig and model machine

### 3.5.2.3 Water density (see 2.5.3)

From the definition of specific hydraulic energy of the machine in 1.3.3.6.2 the mean water density  $\bar{\rho}$  shall be calculated as the mean of densities at the two reference sections. As the temperature difference between inlet and outlet of the machine is small, the temperature of the water at the low pressure reference section may be used for calculating the densities involved in the evaluation of  $\bar{\rho}$ .

The values of distilled water density (see 2.5.3.1.3 and table B.2) can normally be used as water density  $\rho_w$  for the determination of  $E$  or  $H = E/g$  because:

- the value of the density for the actual water  $\rho_{wa}$  in the model test equipment differs rather little from the value of the density for distilled water  $\rho_{wd}$ : in general the deviation is smaller than 0,05 % (see 2.5.3.1.2);
- the hydraulic power  $P_h = E (\rho Q)_1$ , (see 1.3.3.8.1), as the main hydraulic quantity for the determination of the efficiency, depends only to second order accuracy on density, if the specific hydraulic energy of the model machine is predominantly obtained by pressure measurements (see simplified formulae in 3.5.3.2.1 and 3.5.3.2.2 and the explanation in annex D).

In special cases, it may be necessary to determine the density  $\rho_{wa}$  of actual water used (see 2.5.3.1.2).

## 2.4 Specific kinetic energy

convention the specific kinetic energy term in a reference section is determined from the mean velocity of the water perpendicular to that section and is taken as  $e_c = v^2 / 2$ .

The mean velocity  $v$  is the actual discharge passing through the reference section divided by the area of the same reference section<sup>1)</sup>. This area shall be measured when model similarity is required. The same convention is applied when the measuring section differs from the reference section within the limits of the machine.

## 2.5 Uncertainty in the determination of specific hydraulic energy E

The determination of E shall be adapted for each method and arrangement according to the principles described in 3.5.3.

In 3.2.3 an example for the determination of the relative systematic uncertainty  $f_E$  is shown corresponding to figure 39).

In order to account for the effect of non-uniformity of the pressure distribution in the measuring sections (see 3.3.3.1), an additional uncertainty  $f_{\Delta E}$  is added arithmetically to the total relative uncertainty  $f_E$ :  $f_{E, \text{corr.}} = f_E + f_{\Delta E}$

## 3 Simplified formulae for E

### 3.1 General

As indicated in annex C, the general formula given in 1.3.3.6.2 is a convenient approximation of the exact value of the specific hydraulic energy of the machine.

Further simplifications are possible in each specific case and approximations may be introduced, for example when the water compressibility or the difference in ambient pressure between sections 1 and 2 is negligible.

For the local velocity  $v_l$  in the streamline of a fluid, the specific kinetic energy is  $e_{c,l} = v_l^2 / 2$ . The mean value of the specific kinetic energy of the flow passing a cross-section A (with the mean axial velocity  $v$ ) can be expressed as  $e_c = \alpha v^2 / 2$ , the kinetic energy coefficient  $\alpha$  being defined (see ISO 4006) by:

$$\alpha = \frac{\int_A v_l^3 \cdot dA}{v^3 A}, \quad v_{zl} \text{ being the meridional component of } v_l.$$

The coefficient  $\alpha$  would be equal to 1 for a uniform velocity distribution (rectangular velocity profile) and is always greater than 1 in industrial flow.

In testing hydraulic machines, the actual flow configuration in a measuring section shows a non-uniform velocity distribution arising from the layout of the plant and the operation of the machine. It is usually assumed that the flow configuration in the model and in the prototype is approximately the same. However, it is impracticable and time-consuming to determine  $\alpha$  during model tests from a detailed measurement of the velocity distribution. Therefore, it is conventionally agreed to assume  $\alpha = 1$  and thus  $e_c = v^2 / 2$ .

Although the difference between the conventional and actual values of the specific kinetic energy can, for low-head machines, reach 1 % to 2 % of the specific hydraulic energy of the machine, it is agreed to disregard this difference when evaluating the uncertainty in the measurements (see for example the calculation of the uncertainty in E in clause J.2, where the uncertainty in the specific kinetic energy only accounts for uncertainties in the determination of the discharge Q and area A).

It can be assumed that the acceleration due to gravity and the ambient pressure are constant throughout the test rig:

$$\bar{g} = g_1 = g_2 = g \quad \text{and} \quad p_{\text{amb}1} = p_{\text{amb}2} = p_{\text{amb.}}$$

The simplified formulae established in this subclause are typical for the described measuring installations. Only the most common installations are reviewed. A simplified formula shall not be used for a different installation without carefully examining its adequacy.

### 3.5.3.2 Determination of E from pressure measurement (see 3.3)

#### 3.5.3.2.1 Measurement of differential pressure

Figure 39 shows schematically the measuring installations for the determination of specific hydraulic energy of the machine whenever a differential pressure measuring instrument is used. This solution is especially suitable for low model test heads where instruments of sufficient accuracy are available.

#### 3.5.3.2.2 Separate measurement of pressure

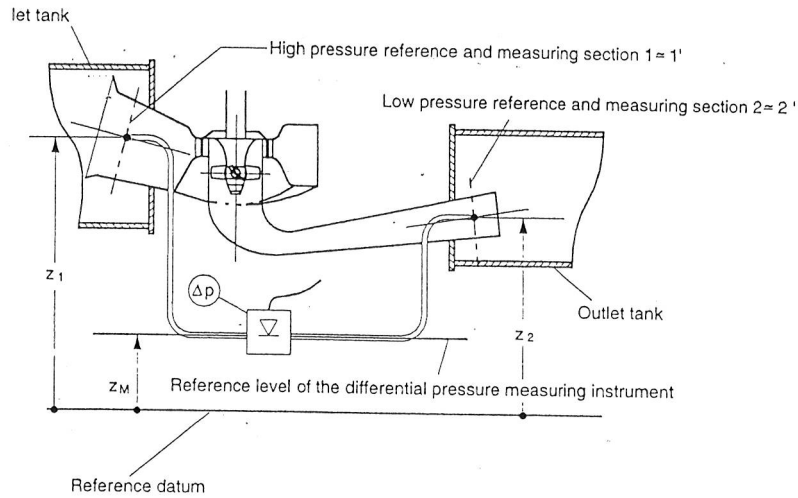
##### a) Reaction machines

The pressures are measured separately in each section. For pressure differences less than about 400 000 Pa (about 40 m of water column), the compressibility of water can be neglected.

If the pressure measuring instrument provides absolute pressure measurements (e.g. pressure transducers), the ambient pressure does not need to be considered.

If the pressure measuring instrument provides gauge pressure measurements (e.g. spring-pressure gauge or liquid column manometer), it shall be verified whether the difference in the ambient pressure on the instruments shall be included (see figure 40 [influence negligible] and figure 41 [influence taken into account]).

Further simplifications may be introduced by setting the pressure measuring instruments at the same reference level. This is generally easy to achieve (see figure 40, last simplification).



$$E = gH = (p_{abs1} - p_{abs2}) / \bar{\rho} + (v_1^2 - v_2^2) / 2 + g(z_1 - z_2)$$

Using a differential pressure measurement, the following is obtained:

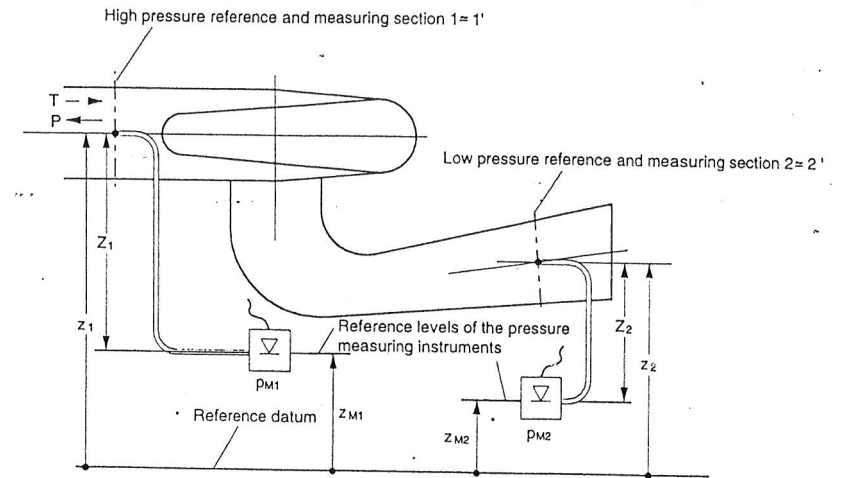
$$(p_{abs1} - p_{abs2}) / \bar{\rho} = \Delta p / \bar{\rho} + g[(z_2 - z_M) \cdot \rho_2 / \bar{\rho} - (z_1 - z_M) \cdot \rho_1 / \bar{\rho}]$$

When applied to low model test heads ( $\Delta p \leq 400\,000$  Pa, i.e.  $H \leq 40$  m), the compressibility of water is negligible and it is assumed that  $\bar{\rho} = \rho_1 = \rho_2$ .

Therefore the simplified formula is:

$$E = \Delta p / \rho_2 + (v_1^2 - v_2^2) / 2$$

Figure 39 – Determination of specific hydraulic energy through differential pressure measuring instrument



$$E = gH = (p_{abs1} - p_{abs2}) / \bar{\rho} + (v_1^2 - v_2^2) / 2 + g(z_1 - z_2)$$

Gauge manometers are applied at points 1 and 2. The difference in ambient pressure between  $z_{M1}$  and  $z_{M2}$  is negligible, because  $(z_{M1} - z_{M2})$  is small compared to  $H$ ; therefore:

$$p_{ambM1} = p_{ambM2} = p_{amb}$$

$$p_{abs1} = p_{M1} + \rho_1 g(z_{M1} - z_1) + p_{amb}$$

$$p_{abs2} = p_{M2} + \rho_2 g(z_{M2} - z_2) + p_{amb}$$

If the compressibility of water can be neglected, then  $\rho_1 = \rho_2 = \bar{\rho}$

hence  $(p_{abs1} - p_{abs2}) / \bar{\rho} = (p_{M1} - p_{M2}) / \bar{\rho} + g(z_{M1} - z_1 - z_{M2} + z_2)$ ,

therefore, the simplified formula is:

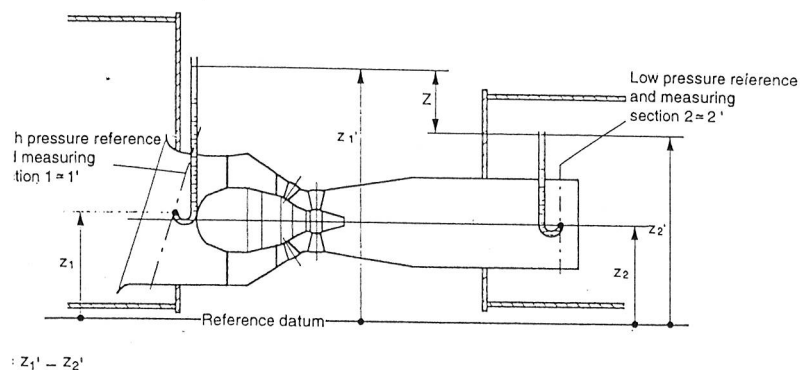
$$E = gH = (p_{M1} - p_{M2}) / \bar{\rho} + (v_1^2 - v_2^2) / 2 + g(z_{M1} - z_{M2})$$

Further simplification:

If the pressure measuring instruments are on the same elevation,  $z_{M1} = z_{M2}$ , then

$$E = gH = (p_{M1} - p_{M2}) / \bar{\rho} + (v_1^2 - v_2^2) / 2$$

Figure 40 – Determination of specific hydraulic energy of the machine through separate measurement of gauge pressures



$$E = gH = (p_{abs1} - p_{abs2}) / \rho + (v_1^2 - v_2^2) / 2 + g(z_1 - z_2)$$

When column manometers are applied at sections 1 and 2:

the compressibility of water is negligible, because the difference of pressure between sections 1 and 2 is small.

Therefore:  $\rho_1 = \rho_2 = \bar{\rho} = \rho$

Hence:  $p_{abs1} = \rho \cdot g(z_1 - z_1') + p_{amb1}$

$p_{abs2} = \rho \cdot g(z_2 - z_2') + p_{amb2}$

$p_{amb1} - p_{amb2} = -\rho_a \cdot g(z_1' - z_2')$

The simplified formula is

$$E = g(z_1 - z_2') \left(1 - \rho_a / \rho\right) + (v_1^2 - v_2^2) / 2$$

$$= g \cdot Z \left(1 - \rho_a / \rho\right) + (v_1^2 - v_2^2) / 2$$

Figure 41 – Determination of specific hydraulic energy of the machine through separate measurement of pressures by water column manometers

## b) Pelton turbines (impulse turbines)

For Pelton turbines, when the housing is under atmospheric pressure, only the measurement of the pressure  $p_1$  at the high pressure reference section is required. Thus further simplifications can be introduced if the general formula is applied to Pelton turbines (see figures 42 and 43).

By convention,  $v_2$  is taken as zero, elevation  $z_2$  of the low pressure reference section is the mean elevation of all contact points of the jet axis with the Pelton jet circle and the pressure inside the housing is assumed equal to the ambient pressure, provided the housing is not pressurized and is supplied with sufficient air.

If the housing is pressurized, the ambient pressure in the housing shall be measured and accounted for when determining  $E$  ( $p_{amb2} \neq p_{amb1}$ ).

### 3.5.3.3 Determination of $E$ from water level measurements

Whenever possible, water level measurements (see 3.4) should be avoided for model acceptance tests. Nevertheless, if it is necessary or it is agreed to determine  $E$  by measurements of free water levels, especially at the low pressure side, the methods described in 3.4 shall be applied.

The requirements for the flow condition in the surrounding area of the measuring sections are described in 3.4.2.

Figure 44, referring to a low head machine, shows the evaluation of the specific hydraulic energy from measurements of the water levels. The low pressure measuring section 2' shall be as close as possible to the draft tube outlet. For such measurement the water level should be measured directly above 2'. To evaluate the mean velocity, the walls of the draft tube are assumed to extend out to section 2', delineating the fictional area of the section.

### 3.5.4 Determination of the net positive suction specific energy NPSE

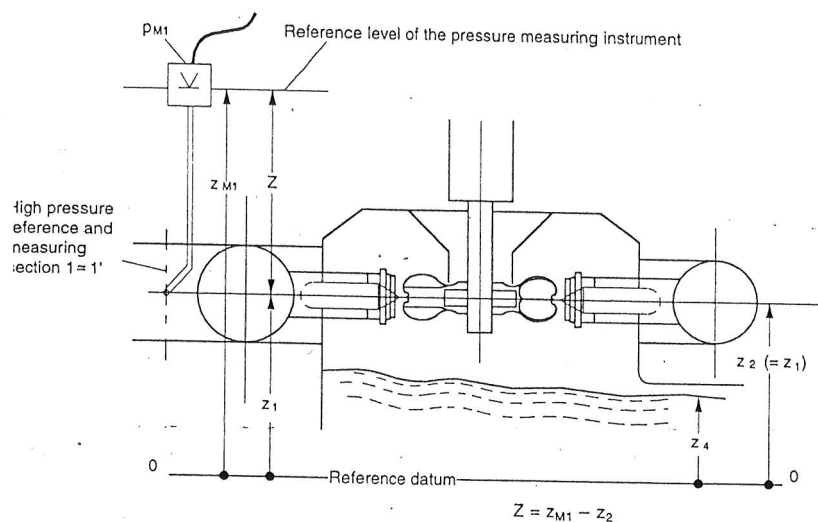
#### 3.5.4.1 Definition

The net positive suction specific energy NPSE is referred to the low pressure side of the machine. Its definition and the general formula for its determination are given in 1.3.3.6.5.

Measurement may be affected by practical circumstances, in the same way as the specific hydraulic energy  $E$  of the machine. Subclause 3.5.2 shall also be considered for the determination of the net positive suction specific energy.

#### 3.5.4.2 Simplified formulae

As long as the pressure can be measured in the low pressure reference section, the general formula is directly applicable and valid for both operating modes, pump and turbine. In figure 45, three cases for the determination of NPSE are described.



is conventionally assumed that the low pressure reference section is the equatorial plane of the runner at elevation  $z_2$ . For non-pressurized housing, the pressure inside the housing is conventionally assumed to be equal to the ambient pressure.

$$E = gH = (p_{abs1} - p_{abs2}) / \rho + (v_1^2 - v_2^2) / 2 + g(z_1 - z_2)$$

The difference in ambient pressure between  $z_{M1}$  and  $z_2$  is neglected because  $Z$  is small compared to  $H$ .

Therefore:

$$p_{ambM1} = p_{amb2} = p_{amb}$$

Further it is assumed

$$Z \cdot \rho_1 / \rho = Z$$

Hence:

$$p_{abs1} = p_{M1} + Z \cdot \rho_1 \cdot g + p_{amb}$$

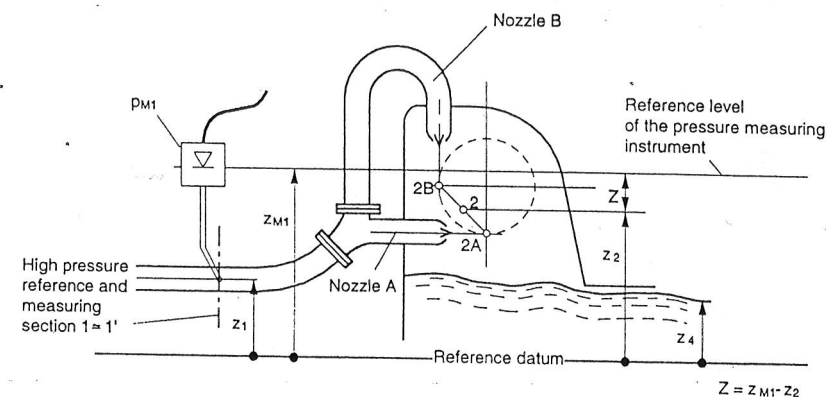
where  $p_{M1}$  is the gauge pressure measured at  $z_{M1}$

$$p_{abs2} = p_{amb}$$

As  $z_1 = z_2$  and assuming  $v_2 = 0$ , the simplified formula is:

$$E = p_{M1} / \rho + g \cdot (z_{M1} - z_2) + v_1^2 / 2 = p_{M1} / \rho + g \cdot Z + v_1^2 / 2$$

Figure 42 – Pelton turbines with vertical axis.  
Determination of specific hydraulic energy of the machine



NOTE – In the case of multiple nozzles, the elevation  $z_2$  of the low pressure reference section is defined as the average of the elevations of the points of contact (2A and 2B in the sketch).

Case of non-pressurized housing: the pressure inside the housing is conventionally assumed as equal to the ambient pressure.

$$E = p_{M1} / \rho + g \cdot (z_{M1} - z_2) + v_1^2 / 2 = p_{M1} / \rho + g \cdot Z + v_1^2 / 2$$

The difference in ambient pressure between  $z_{M1}$  and  $z_2$  is neglected because  $Z$  is small compared to  $H$ .

Therefore:

$$p_{ambM1} = p_{amb2} = p_{amb}$$

Further it is assumed:

$$Z \cdot \rho_1 / \rho = Z$$

Hence:

$$p_{abs1} = p_{M1} + (z_{M1} - z_1) \rho_1 g + p_{amb}$$

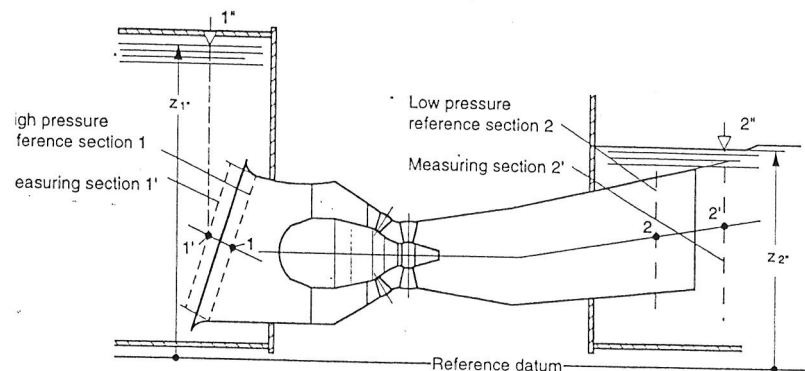
where  $p_{M1}$  is the gauge pressure measured at  $z_{M1}$

$$p_{abs2} = p_{amb}$$

Assuming  $v_2 = 0$ , the simplified formula is:

$$E = p_{M1} / \rho + g \cdot (z_{M1} - z_2) + v_1^2 / 2 = p_{M1} / \rho + g \cdot Z + v_1^2 / 2$$

Figure 43 – Pelton turbines with horizontal axis.  
Determination of specific hydraulic energy of the machine



$$E = gH = (p_{abs1} - p_{abs2}) / \bar{\rho} + (v_1^2 - v_2^2) / 2 + g(z_1 - z_2)$$

Sections 1' and 2' are chosen as measuring sections.

$$E = gH = (p_{abs1'} - p_{abs2'}) / \bar{\rho} + (v_1'^2 - v_2'^2) / 2 + g(z_1' - z_2') \pm E_{L1'-1} \pm E_{L2'-2'}$$

Losses  $E_{L1'-1}$  between 1' and 1 and  $E_{L2'-2'}$  between 2 and 2' are subtracted for a turbine and added for a pump with the situation described in the sketch above<sup>1)</sup>.

The compressibility of water is neglected because the difference of pressure between 1' and 2' is small.

Therefore

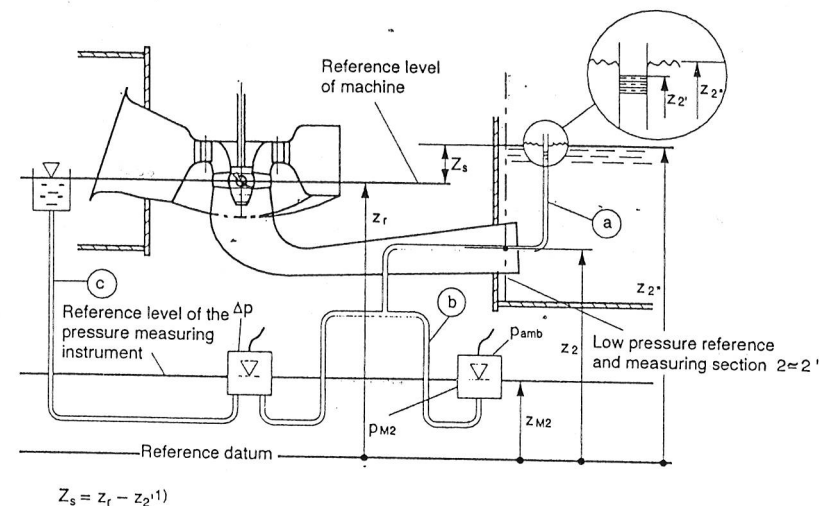
$$p_1 = p_2' = \bar{p} = \rho$$

The simplified formula becomes (see figure 41):

$$E = g \cdot (z_1' - z_2') (1 - \rho_a / \rho) + (v_1'^2 - v_2'^2) / 2 \pm E_{L1'-1} \pm E_{L2'-2'}$$

Figure 44 – Low-head machines. Determination of specific hydraulic energy of the machine using water levels

<sup>1)</sup> It is difficult to establish methods of calculation of energy losses  $E_{L1'-1}$  and  $E_{L2'-2'}$ , particularly in non-symmetrical or swirling flow (high values of the kinetic energy coefficient  $\alpha$ ), which would enable in this standard to give some guidance generally valid. Particularly when the intake and outlet of the unit are not fully modelled, the evaluation method of these losses is to be agreed upon before the tests.



$$Z_s = z_r - z_2'^{1)}$$

$$NPSE = g \cdot NPSH = (p_{abs2} - p_{va}) / \rho_2 + v_2^2 / 2 - g(z_r - z_2)$$

Case a) Liquid (water column) manometer at point 2:

$$p_{abs2} = \rho_2 \cdot g(z_2' - z_2) + p_{amb}$$

The simplified formula is:

$$\begin{aligned} NPSE &= (p_{amb} - p_{va}) / \rho_2 + v_2^2 / 2 - g(z_r - z_2') \\ &= (p_{amb} - p_{va}) / \rho_2 + v_2^2 / 2 - g \cdot Z_s \end{aligned}$$

Case b) Pressure gauge at level  $z_{M2}$ , measuring at point 2:

$$p_{abs2} = p_{M2} + g \cdot \rho_2 \cdot (z_{M2} - z_2) + p_{amb}$$

The simplified formula is:

$$NPSE = (p_{M2} + p_{amb} - p_{va}) / \rho_2 + v_2^2 / 2 - g(z_r - z_{M2})$$

Case c) Differential manometer connected with a pot situated at the reference level of the machine:

The simplified formula is:  $NPSE = (\Delta p + p_{amb} - p_{va}) / \rho_2 + v_2^2 / 2$

Figure 45 – Determination of net positive suction energy NPSE and net positive suction head NPSH

<sup>1)</sup>  $Z_s$  is positive when the level  $z_2'$  is lower than the reference level of machine  $z_r$ , and vice versa.

## Shaft torque measurement

### 1 General

a calculation of mechanical power of the runner/impeller  $P_m$  requires the determination of torque applied to the runner/impeller  $T_m$ :

$$P_m = 2 \cdot \pi \cdot n \cdot T_m$$

$$T_m = T \pm T_{Lm} \begin{cases} + & \text{for turbine rotational direction} \\ - & \text{for pump rotational direction} \end{cases}$$

$n$  is the friction torque due to seal and bearing arrangement.

ncipally, two different measuring systems can be applied for torque measurement:

those of the type "swinging frame", where  $T_{Lm}$  is a so-called "inner torque", i.e.  $T_{Lm}$  is taken into account by the system itself (in the following, described as "bearing of rotating parts in balance", see for instance figures 46 and 47).

those where  $T$  and  $T_{Lm}$  are measured separately (in the following, described as "bearing of rotating parts not in balance", see for instance figure 49).

e shaft torque  $T$  of runner/impeller may be absorbed or generated by:

an electrical machine, usually a motor/generator with variable speed,

absorbed by different types of brakes:

eddy-current brake,

hydraulic brake,

mechanical brake.

## 6.2 Methods of torque measurement

### 6.2.1 Primary method

the primary method, the torque  $T$  is determined by the force  $F$  applied to a lever arm multiplied by the radius  $r$  at which it is applied:  $T = F \cdot r$

he actual force applied to balance the swinging frame may be measured by:

weighing masses on a lever system (calibrated weights and calibrated lever arm). This is in principle the basic primary method

one of the following methods, which can be calibrated *in situ* by the basic primary method a):

- force transducer,
- manometer (via a rotating piston),
- mechanical balance.

o increase the accuracy in determining the total force, it is recommended to counterbalance a part of the force acting on the arm by means of calibrated weights.

### 3.6.2.2 Secondary method

A torquemeter may be used provided its accuracy is acceptable to all parties and it is calibrated by the primary method. A torquemeter comprises a length of shafting whose torsional strain, when rotating, is converted to an electrical output quantity by optical, electrical or other means. The design and the arrangement of this type of torquemeter shall be such that the measurement is not influenced by speed, temperature, axial thrust or radial thrust.

### 3.6.3 Methods of absorbing/generating power

#### 3.6.3.1 Motor/generator with variable speed

This method comprises a machine for absorbing and generating power electrically, suitably mounted so that the mechanical torque can be measured. This device can be used for both turbine and pump models.

#### 3.6.3.2 Eddy-current brake

The operation of this electromagnetic brake is restricted to absorbing power.

#### 3.6.3.3 Hydraulic brake

This brake absorbs power hydrodynamically. It is unsuitable for use at low speeds as its power absorption varies with  $n^3$ .

#### 3.6.3.4 Mechanical brake

This brake absorbs power by friction. It has the advantage that high torques can be applied at low speeds, even down to zero rotational speed. The torque applied shall be steady and the mechanical system shall be vibration free.

### 3.6.4 Layout of arrangement

#### 3.6.4.1 General

Figures 46 to 54 show practical arrangements comprising primary and secondary methods of torque measurement. All arrangements shown can be adapted for either a horizontal axis or a vertical axis test stand.

Figures 46 and 47 illustrate the principle of the balance arrangement. The torque acting on the runner/impeller is measured at the torque arm of the swinging frame.

If the swinging frame, as shown in figure 48, is formed by two separate frames, the torques acting on each frame shall be measured and added algebraically.

Figure 49 shows an arrangement not fully in balance, therefore the losses due to bearing and seal shall be measured separately.

Figure 50 shows an arrangement with the model shaft through a draft tube elbow. Normally, such an arrangement is not fully in balance and losses have to be accounted for.

Special arrangements are necessary for testing multistage pumps or pump-turbines as shown in figure 51. Particular attention is to be paid to mechanical losses  $P_{Lm}$  which shall be accurately known and accounted for over the whole range of speed and pressure occurring during the test.

Figure 52 illustrates an arrangement using a torquemeter. Figures 53 and 54 show variations with an additional guide bearing which may be balanced or not.

omenclature for figures 46 to 54

- rotating part
- swinging frame
- stationary part
- bearing of rotating part in balance
- mechanical seal in balance
- low friction bearing of the swinging frame
- labyrinth seal, membrane
- bearing of rotating part not in balance
- mechanical seal of rotating part not in balance
- torquemeter
- axial thrust bearing
- — — reference section for torque measurement

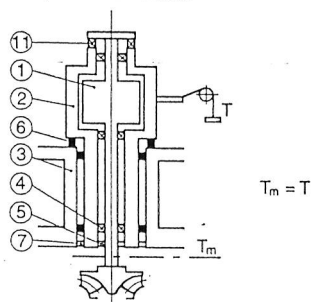


Figure 46 – Balance arrangement

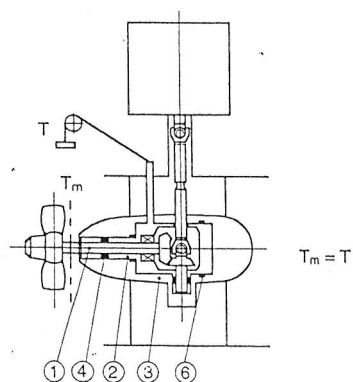


Figure 47 – Balance arrangement with gear

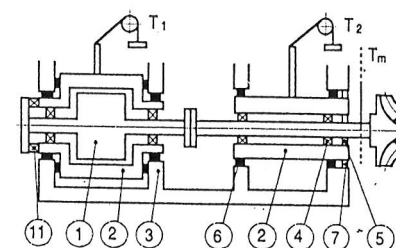


Figure 48 – Balance arrangement with two separate frames

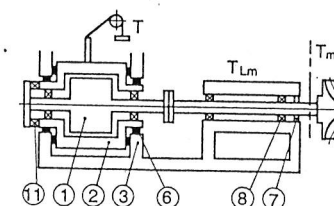


Figure 49 – Arrangement with machine bearings and seals not in balance

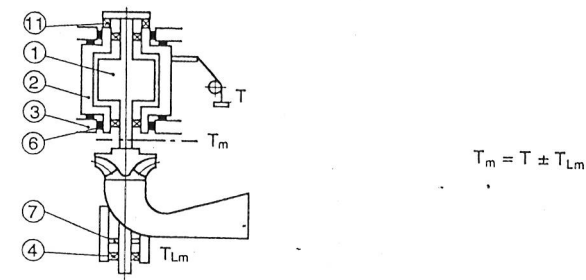
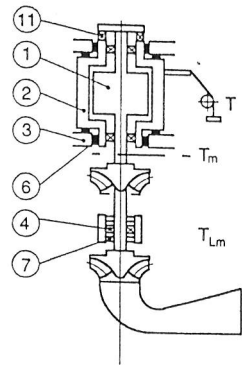
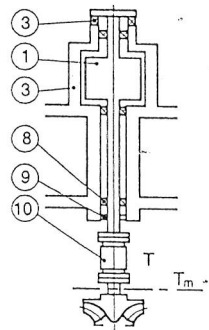


Figure 50 – Arrangement with lower bearing and seal not in balance



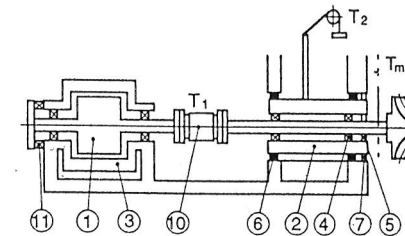
$$T_m = T \pm T_{Lm}$$

Figure 51 – Arrangement with intermediate bearing and seal not in balance



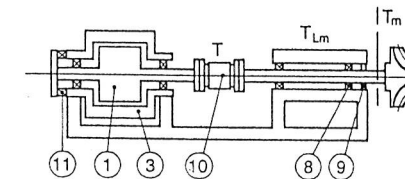
$$T_m = T$$

Figure 52 – Arrangement using a torquemeter



$$T_m = T_1 \pm T_2$$

Figure 53 – Arrangement using a torquemeter with machine bearings and seals in balance



$$T_m = T \pm T_{Lm}$$

Figure 54 – Arrangement using a torquemeter with machine bearings and seals not in balance

### 3.6.4.2 Suspension of swinging frame

To meet the requirements regarding uncertainty of measurement over the measured range, special low friction bearings are necessary for suspending the swinging frame, i.e. oil or water hydrostatic bearings. The swinging frame should be perfectly balanced, otherwise it is necessary to limit the rotational movement.

### 3.6.4.3 Windage losses

Whatever speed of the motor/generator, there shall be no torque reaction caused by windage or by a blower; if there is, this shall be taken into account.

### 3.6.4.4 Cooling fluid connections

The torque measuring device shall be designed in such a way that the cooling fluid enters and leaves without introducing errors due to tangential velocity components. Flexible pipes (if used) shall impose no measurable tangential restraint, especially when under pressure. Dash-pots (if used) shall be shown to impose equal resistance to motion in either direction. Furthermore, the shaft glands retaining the liquid shall either impose no sensible frictional torque or be provided with a torque measurement device.

#### 3.4.5 Seals

sealing between swinging and fixed parts is made by means of friction or membrane seals, these shall be calibrated.

#### 3.4.6 Electrical leads

Electrical connections shall impose no measurable tangential restraint. Braided flexible copper leads or mercury pots are suitable for this purpose.

#### 3.5 Checking of system

The checks described below are recommended to verify the correct operation of the whole torque measuring arrangement; nevertheless, the measuring device shall be calibrated.

##### 3.5.1 Sensitivity test

The sensitivity of a testing arrangement indicates the lowest torque difference which can be measured through the system. The sensitivity strongly depends on the layout and capacity of the arrangement. Reduced sensitivity indicates to incorrect functioning.

Depending on the layout and capacity of the arrangement used, the sensitivity shall be in a range of 0,05 N·m to 0,5 N·m whereby the low value is valid for  $T_{m,max} < 500$  N·m.

##### 3.5.2 Speed test

This test is carried out with a dismantled runner/impeller or a disconnected shaft. The system functions correctly if the mechanical torque  $T_m$  remains zero for the whole range of speeds.

##### 3.5.3 Counterbalancing

During this check the applied torque/force, or part of it, is counterbalanced by means of certified masses. The system functions correctly if the display is reduced according to the counterbalancing mass.

#### 3.6 Calibration

##### 3.6.1 Primary method

During calibration the following quantities shall be measured:

- length of brake lever;
- force on brake lever;
- tare weight of the brake lever if necessary.

The force acting on the brake lever shall be applied by means of certified masses in the direction of both increasing and decreasing loads. Metal tapes and frictionless pulleys shall be used for applying the torque balancing weights.

##### 3.6.2 Secondary method

When using this method, a calibration of the arrangement against a primary method shall be carried out.

#### 3.6.3 Friction torque $T_{Lm}$

If part of bearing/sealing arrangement is not included in the swinging frame, the relevant total friction torque  $T_{Lm}$  shall be determined by an appropriate test taking into account the dependency on speed and shaft seal pressure.

#### 3.6.7 Uncertainty in torque measurement

The expected relative systematic uncertainties (at a confidence level of 95 %) are set out below.

##### 3.6.7.1 Uncertainty in the shaft torque measurement by primary method

###### 3.6.7.1.1 Length of lever arm $r$

The length of lever arm  $r$  should be measured within:

$$f_{r,s} = \pm 0,05 \% \text{ to } 0,1 \%$$

###### 3.6.7.1.2 Force $F$

The force  $F$  acting on the lever arm should be measured within:

$$f_{F,s} = \pm 0,05 \% \text{ to } 0,1 \%$$

##### 3.6.7.2 Uncertainty in the shaft torque measurement by secondary method

The systematic uncertainty in the shaft torque strongly depends on the arrangement used. The expected uncertainty should be within:

$$f_{T,s} = \pm 0,15 \% \text{ to } 0,25 \%$$

##### 3.6.7.3 Uncertainty in the measurement of the friction torque $T_{Lm}$

Where the bearing/seal arrangement is not included in the swinging frame system, the friction torque  $T_{Lm}$  should be measured within:

$$f_{T_{Lm},s} = \pm 0,02 \% \text{ to } 0,05 \%, \text{ of } T_{m,max}$$

##### 3.6.7.4 Systematic uncertainty in the runner/impeller torque measurement

Using the above uncertainties (see 3.6.7.1 to 3.6.7.3) the relative systematic uncertainty in the runner/impeller torque can be calculated as shown below:

- a) for the primary method with  $T_{Lm}$ , measured in the common swinging frame (see figures 46 and 47):

$$f_{Tm,s} = \sqrt{(f_{r,s}^2 + f_{F,s}^2)}$$

- b) for the secondary method (see figure 52):

$$f_{Tm,s} = f_{T,s}, \text{ defined in 3.6.7.2}$$

for the primary method with  $T_{Lm}$ , not measured with swinging frame (see figures 49, 50 and 51):

The absolute systematic uncertainty is:

$$e_{Tm} = \sqrt{T^2 \cdot f_{T,s}^2 + T_{Lm}^2 \cdot f_{Lm,s}^2} = \sqrt{T^2 (f_{r,s}^2 + f_{F,s}^2) + T_{Lm}^2 \cdot f_{Lm,s}^2}$$

then the relative systematic uncertainty is:

$$f_{Tm} = \frac{e_{Tm}}{T_m}$$

for the secondary method with  $T_{Lm}$  not measured with a swinging frame (see figure 54) the absolute systematic uncertainty is:

$$e_{Tm} = \sqrt{T^2 \cdot f_{T,s}^2 + T_{Lm}^2 \cdot f_{Lm,s}^2}$$

then the relative systematic uncertainty is:

$$f_{Tm} = \frac{e_{Tm}}{T_m}$$

## Rotational speed measurement

### 1 General

termination of the mechanical power of the runner/impeller requires knowledge of the rotational speed of the runner/impeller shaft.

### 2 Methods of speed measurement

The rotational speed of the turbine/pump model may be measured by one of the following methods:

counting of pulses generated by the model shaft, using an electronic counter and timebase. The pulse generator may be electrical or optical;

electrical frequency meter connected with a generator directly driven by the model shaft;

electrical high-precision tachometer comprising a stable permanent magnet directly driven by the model shaft.

### 3 Checking

Usually, the speed measurement device is not truly calibrated, but checked

either by comparison with another speed measurement device;

or by checking separately the counting of pulses and the accuracy of the time base.

In case of malfunction, possible errors are:

missing pulses;

change of time base.

### 3.7.4 Uncertainty of measurement

Using the aforementioned instrumentation, systematic uncertainty is expected to be within

$$f_{n,s} = \pm 0,01 \% \text{ to } 0,05 \%$$

## 3.8 Computation of test results

### 3.8.1 General

The main hydraulic performance guarantees verifiable by model test are (see 1.4.2): power, discharge and/or specific hydraulic energy, efficiency, steady-state runaway speed and/or discharge.

The model test results shall be transformed into quantities directly comparable with the data specified or guaranteed in the contract. The procedures to calculate these quantities are described below, and summarized as a flow chart in figure 62. The procedures shall be agreed between the parties prior to the beginning of the tests.

Subclause 3.8.2 deals with the computation of mechanical power of runner/impeller, discharge and/or specific hydraulic energy, and hydraulic efficiency in the guarantee range and includes the influence of cavitation (see 3.8.2.3.7 and 3.8.2.4.2).

Subclause 3.8.3 deals with the computation of steady-state runaway speed and discharge, and includes the influence of cavitation (see 3.8.3.2).

Subclauses 3.8.2.5 and 3.8.3.4 provide the formulae to be used.

Annex E provides an abstract of the test and calculation procedure.

For the hydraulic performance test of a machine, table 6 shows:

- the geometric parameters;
- the independent hydraulic variables;
- the dependent hydraulic variables.

Examples of performance diagrams for a Francis turbine, a Kaplan turbine, a radial pump, a double-regulated (axial) pump and a Pelton turbine are given respectively in figures 55 to 60. In the case of a single-regulated turbine, two examples of hill diagrams are given using either discharge and speed factors (see figure 55) or discharge and energy coefficients (see figure 56). An example of a four quadrant diagram for a single-regulated (radial) pump-turbine is shown in figure 61.

Hydraulic efficiencies measured on two geometrically similar reaction machines at any hydraulically similar operating points (see 2.3.1.2) of the guaranteed efficiency range are generally different because of the different values of test Reynolds number, which affects hydraulic efficiency (and consequently the mechanical power of runner/impeller), as explained in annex F.

Therefore, even for comparison with the guarantees given on the model, all values of hydraulic efficiency computed during the tests on a given model shall be referred to a constant Reynolds number, usually stated in the contract, by using the scale effect formula (see 1.4.1.4 and 3.8.2.2). The relevant symbols become  $\eta_{HM}$  and  $P_{ED}$  or  $P_{ND}$ .

here the model tests can be performed at the Reynolds number specified in the contract, no scale effect formula is applied.

Table 6 – Variables defining the operating point of a machine

	MACHINE		
	Single-regulated	Double-regulated	Non-regulated
Geometrical parameter	$\alpha$ or $\beta$ or $s$	$\alpha$ and $\beta$	—
Independent hydraulic variables	$E_{nD}, Q_{nD}, \sigma_{nD}$ or $n_{ED}, Q_{ED}, \sigma$	$E_{nD}, Q_{nD}, \sigma_{nD}$ or $n_{ED}, Q_{ED}, \sigma$	$E_{nD}$ or $Q_{nD}, \sigma_{nD}$ or $n_{ED}$ or $Q_{ED}, \sigma$
Dependent hydraulic variables	$\eta_h$ $P_{nD}$ or $P_{ED}$	$\eta_h$ $P_{nD}$ or $P_{ED}$	$\eta_h$ $Q_{nD}$ or $E_{nD}, P_{nD}$ or $Q_{ED}$ or $n_{ED}, P_{ED}$

For runaway tests  $\eta_h = 0$  and  $P_{nD} = P_{ED} = 0$ :

- for single-regulated machines, only one of the quantities  $E_{nD}, Q_{nD}$  (or  $n_{ED}, Q_{ED}$ ) is an independent variable;
- for non-regulated machines, there is only one runaway point (neglecting the influence of cavitation).

The prototype usually has a well defined Reynolds number  $Re_p$ . The hydraulic efficiency measured on a reaction machine model shall be transformed into the prototype hydraulic efficiency taking into account the scale effect due to the Reynolds number.

Scale effect due to the Reynolds number is assumed for  $n, Q, E$  and the relevant dimensionless terms unless otherwise agreed (see 3.8.2.5.1): therefore  $n_{EDM} = n_{EDP}$  and  $Q_{EDM} = Q_{EDP}$  (or  $E_{nDM} = E_{nDP}$  and  $Q_{nDM} = Q_{nDP}$ ).

With multistage machines, if the model is tested with a reduced number of stages (see 1.3.4.2), the method of calculation of model data, taking into account the effect of reduced stages (labyrinth leakage and power loss) and the transformation of these to prototype conditions shall be agreed.

For impulse turbines (Pelton), no scale effect in efficiency is taken into account, unless otherwise specified in the contract (see 1.4.1.4a) and 3.8.2.2b)).

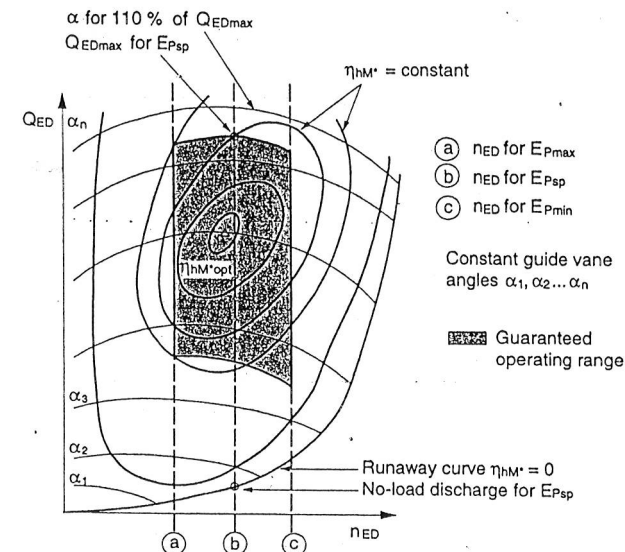


Figure 55 – Single-regulated (Francis) model turbine: performance hill diagram (discharge factor versus speed factor)

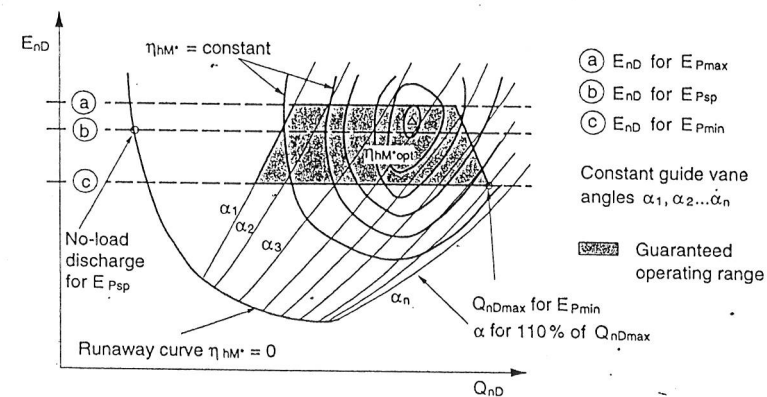


Figure 56 – Single-regulated (Francis) model turbine: performance hill diagram (energy coefficient versus discharge coefficient)

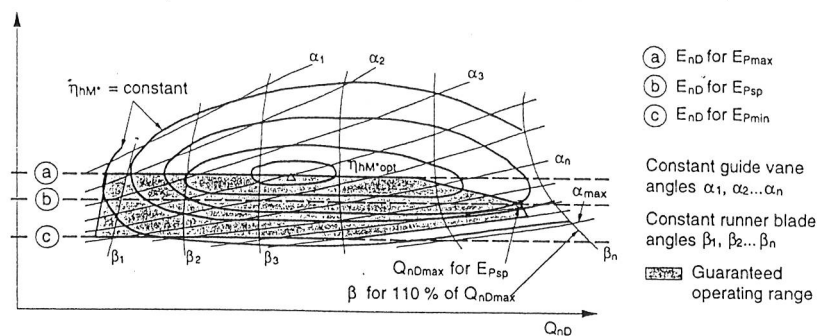


Figure 57 – Double-regulated (Kaplan) model turbine: performance hill diagram

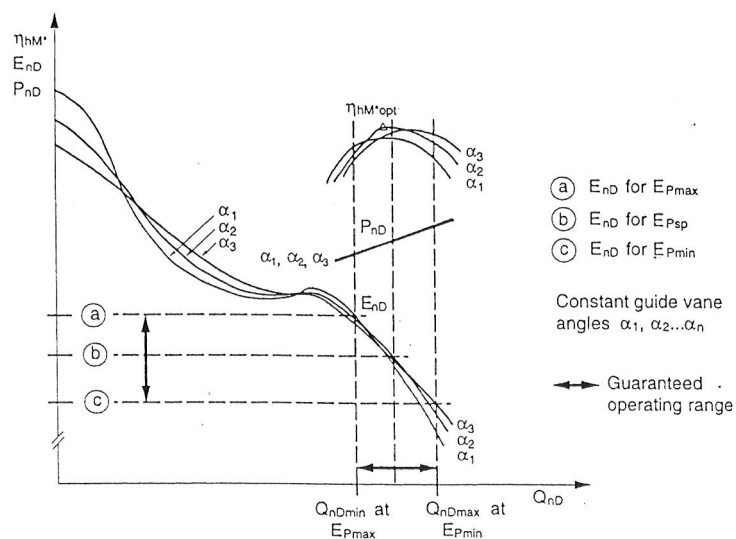


Figure 58 – Single-regulated (radial) model pump: performance diagram

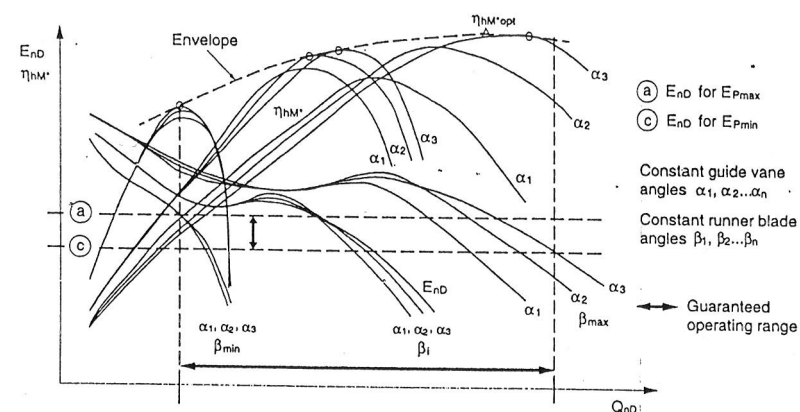


Figure 59 – Double-regulated model pump: performance diagram

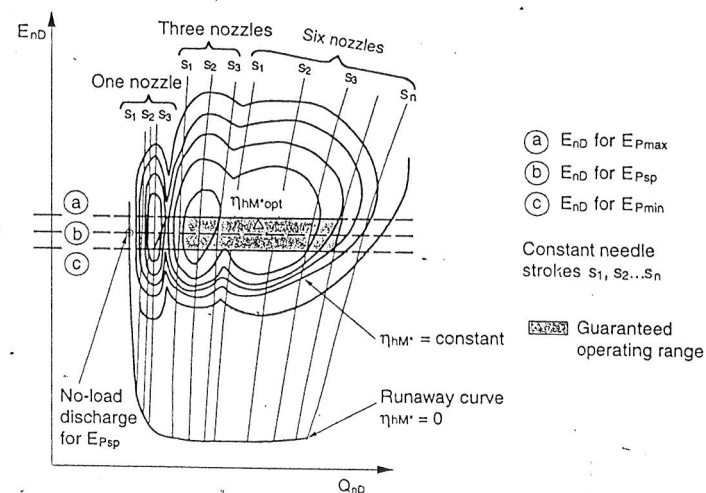


Figure 60 – Pelton model turbine: performance hill diagram (example for a six-nozzle machine)

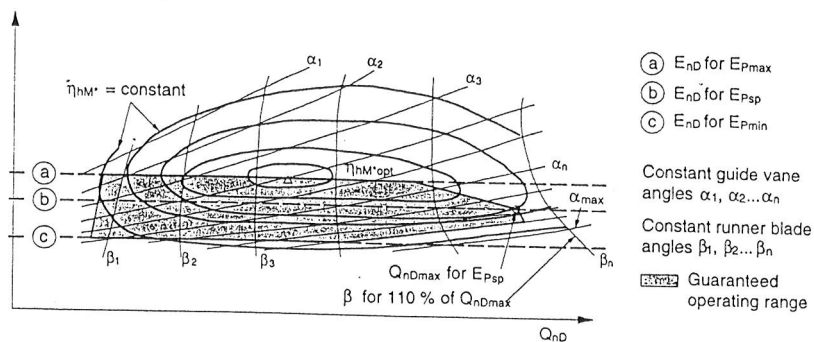


Figure 57 – Double-regulated (Kaplan) model turbine: performance hill diagram

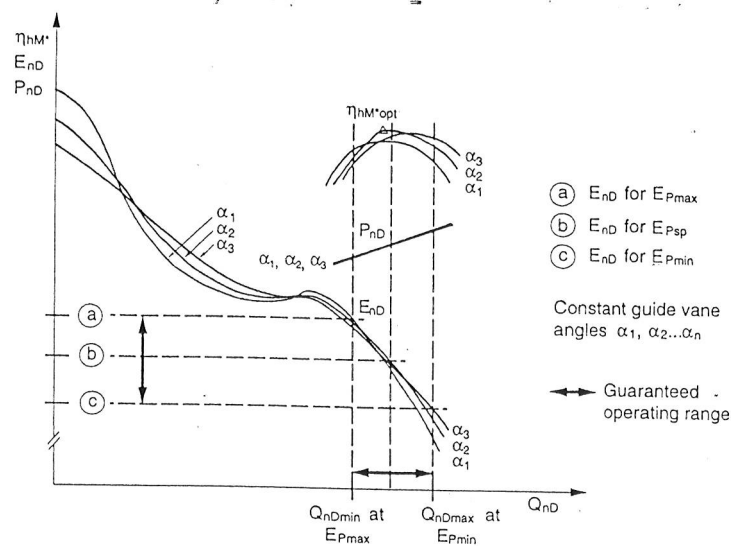


Figure 58 – Single-regulated (radial) model pump: performance diagram

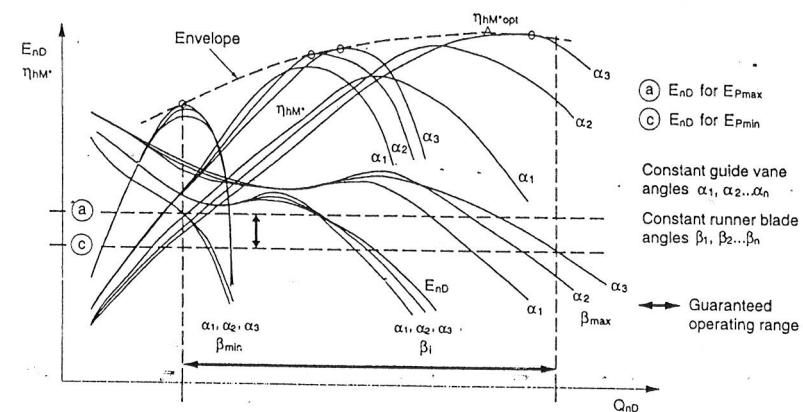


Figure 59 – Double-regulated model pump: performance diagram

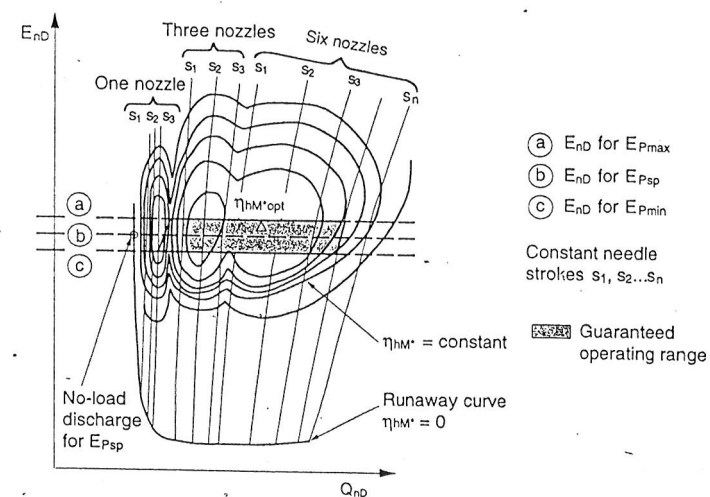


Figure 60 – Pelton model turbine: performance hill diagram (example for a six-nozzle machine)

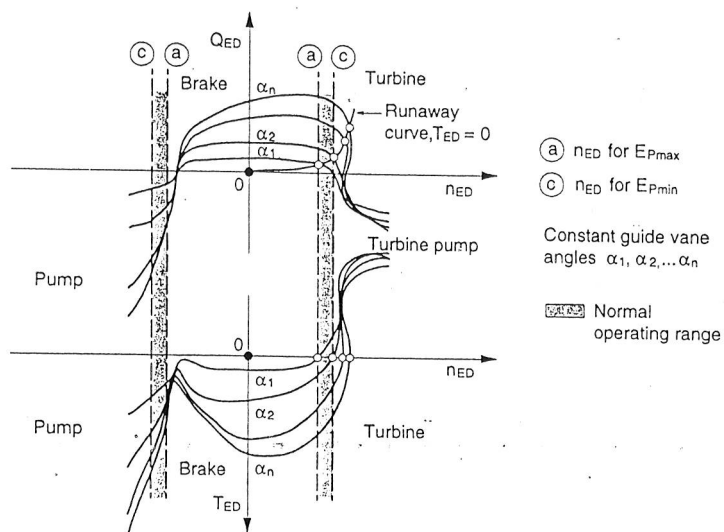


Figure 61 – Radial model pump-turbine: general four quadrant diagram

## 2 Computation of power, discharge and efficiency in the guarantee range

### 2.1 Computation of the model performance at a point

each point a set of one or more readings and/or recordings of the physical quantities used to determine the hydraulic performance of the model (see 2.4) is made.

average values of  $E_M$ ,  $Q_{1M}$ ,  $n_M$ ,  $P_{mM}$  and  $NPSE_M$  are then computed (see 3.1); the values shown in 2.4.1.4 enable the hydraulic efficiency  $\eta_{hM}$  of the model to be calculated.  
Reynolds number  $Re_M$  is computed by the formula in 1.3.3.11.1.

### 2.2 Computation of model performance referred to a constant $Re_{M^*}$

#### Reaction machines

Normally, model tests are carried out at constant Reynolds number  $Re_{M^*}$ . If the guarantees are on the model at a specified Reynolds number  $Re_{MSP}$ , it is good practice to choose  $Re_{M^*} = Re_{MSP}$ . If the model test cannot be carried out at constant Reynolds number, the hydraulic efficiency calculated for each point with a different Reynolds number  $Re_M$  shall be scaled to  $M^*$  (see figures 62 and 63).

The following formula<sup>1)</sup> is applied:

$$(\Delta\eta_h)_{M \rightarrow M^*} = \delta_{ref} \left[ \left( \frac{Re_{ref}}{Re_M} \right)^{0.16} - \left( \frac{Re_{ref}}{Re_{M^*}} \right)^{0.16} \right]$$

where

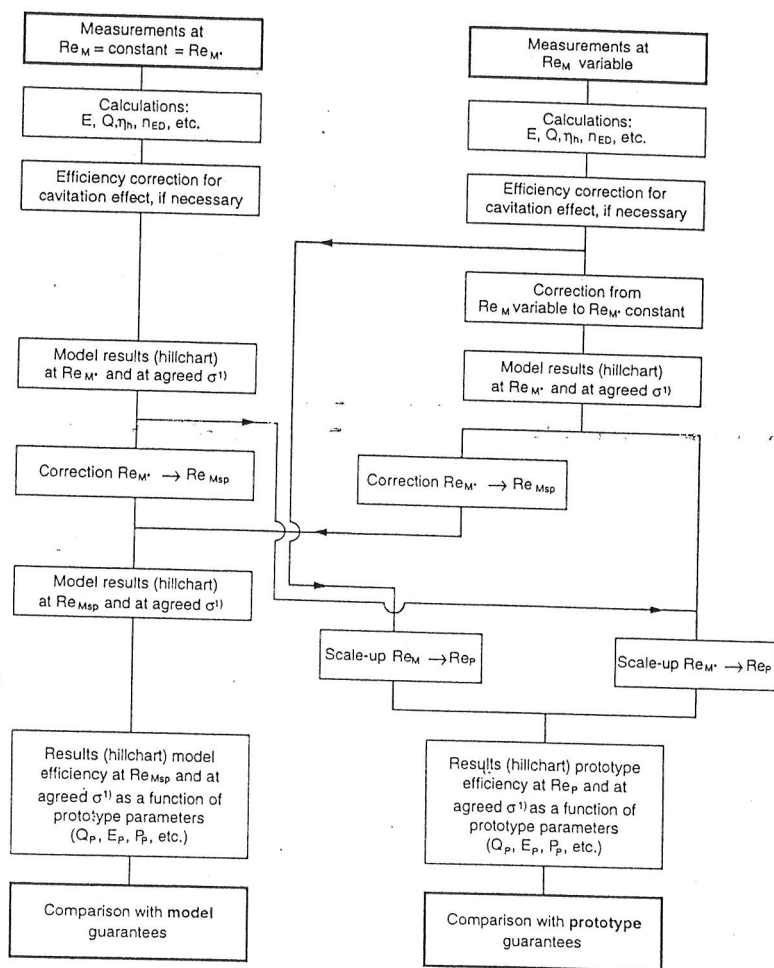
$$\delta_{ref} = \frac{1 - \eta_{hoptM}}{\left( \frac{Re_{ref}}{Re_{optM}} \right)^{0.16} + \frac{1 - V_{ref}}{V_{ref}}} \text{ and } Re_{ref} = 7 \cdot 10^6$$

- $Re_{optM}$  is the Reynolds number at which the optimum hydraulic efficiency  $\eta_{hopt}$  in each operating mode of the model is measured (see 3.8.2.2.1);
- the value of  $V'_{ref}$  is taken from 3.8.2.2.2.

#### b) Impulse turbines

Experience of different manufacturers has shown scale effects on impulse (Pelton) turbines to be primarily influenced by Froude, Reynolds and Weber numbers. A procedure for taking these effects into account is proposed in annex K and may be used by mutual agreement.

<sup>1)</sup> This formula is a particular form of the general scale formula given in annex F.



<sup>1)</sup> Generally, the agreed value of  $\sigma$  is equal to  $\sigma_{pl}$

Figure 62 – Reaction machines: procedure for calculating test results in view of comparison with guarantees

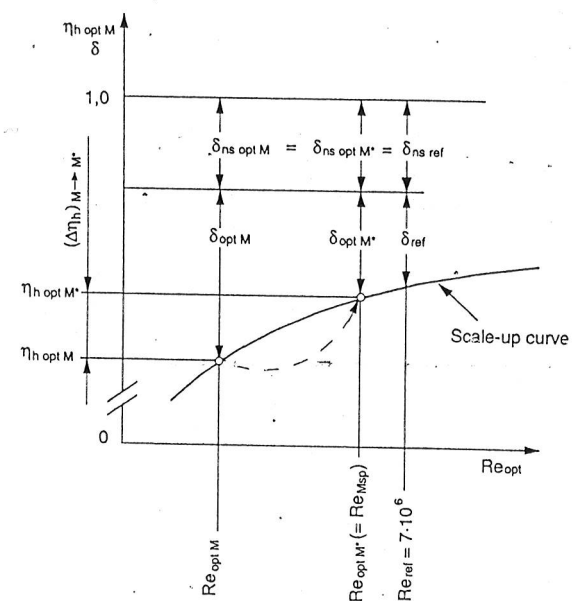


Figure 63 – Scale-up curve for best efficiency point

### 3.8.2.2.1 Determination of the efficiency scale-up

A series of tests performed according to 2.3.3.3.5 enables the optimum value of the hydraulic efficiency of the model  $\eta_{h \text{ opt } M}$  and the corresponding Reynolds number  $Re_{\text{opt } M}$  at non-cavitating conditions to be determined.

Using these values in the equations given in 3.8.2.2.2,  $\delta_{\text{ref}}$  and  $(\Delta \eta_h)_{M \rightarrow M^*}$  may then be calculated (see figure 63 and annex F).

In the case of a pump-turbine, this procedure shall be followed separately for both turbine and pump operation.

In the case of axial or diagonal machines having fixed runner blade angles and/or fixed guide vane angles (see table 7),  $\eta_{h \text{ opt } M}$  is the optimum efficiency of the model tested with the same openings as the prototype.

Table 7 –  $V_{ref}$  values

Type of reaction machine <sup>1)</sup>	$V_{ref}$
<b>turbines</b>	
axial turbine (Francis)	0,7
axial or diagonal turbine (Kaplan, tubular <sup>2)</sup> and Deriaz) with adjustable runner blades and adjustable or fixed guide vanes	0,8
axial or diagonal turbine with fixed runner blades (propeller turbine)	0,7
<b>storage pumps</b>	
axial storage pumps (single-stage or multi-stage)	0,6
axial or diagonal storage pump	0,6
<b>propeller-turbines</b>	
axial pump-turbine (single-stage or multi-stage) operating as turbine	0,7
axial pump-turbine (single-stage or multi-stage) operating as pump	0,6
axial or diagonal pump-turbine with adjustable runner blades operating as turbine	0,8
axial or diagonal pump-turbine with adjustable runner blades operating as pump	0,6
axial or diagonal pump-turbine with fixed runner blades operating as turbine	0,7
axial or diagonal pump-turbine with fixed runner blades operating as pump	0,6

<sup>1)</sup> For hydraulic machines of special design (e.g. double flow machines, Francis turbines with splitter vanes, outer turbines) scaling-up formulae with other  $V_{ref}$  values and other values of the exponent of ratio  $Re_{ref}/Re_M$  in the relations given in 3.8.2.2 basing on individual loss considerations and experience may be applied after mutual agreement.

<sup>2)</sup> Tubular turbines include: bulb turbines, pit turbines, rim-generator turbines, S-turbines.

### 3.2.2.2 Values of loss distribution coefficient $V_{ref}$

The values of  $V_{ref}$  listed in table 7 are referred to  $Re_{ref} = 7 \times 10^6$ . They represent the ratio of relative scalable losses to relative total losses  $(1 - \eta_{hopt})$  for the point of optimum hydraulic efficiency at the reference Reynolds number  $Re_{ref} = 7 \times 10^6$  for different types of reaction machines (see annex F).

### 3.2.2.3 Computation of the runner/impeller mechanical power factor $P_{ED}$ (or coefficient $P_{nD}$ ) referred to a constant value $Re_M$ for reaction machine

When  $Re_M \neq Re_M$ , it is necessary to correct  $P_{ED}$  to  $P_{ED}$  or  $P_{nD}$  to  $P_{nD}$  as follows:

Turbines	Pumps
$P_{ED} = P_{ED} \frac{\eta_{hM}}{\eta_{hM}}$	$P_{ED} = P_{ED} \frac{\eta_{hM}}{\eta_{hM}}$
$P_{nD} = P_{nD} \frac{\eta_{hM}}{\eta_{hM}}$	$P_{nD} = P_{nD} \frac{\eta_{hM}}{\eta_{hM}}$

### 3.8.2.3 Presentation of model performance

The three basic types of hydraulic machines:

- single-regulated machine;
- double-regulated machine;
- non-regulated machine

are dealt with separately. Each type of machine is divided into turbine (or pump-turbine operating as turbine) and into pump (or pump-turbine operating as pump).

As the model efficiency guarantees for a specified value of  $Re_{MSP}$  are usually stated as a function of the prototype data  $E_P$  and  $Q_{1P}$  (or  $P_{mP}$ ) for turbines or  $Q_P$  (or  $E_P$ ) for pumps, the model performance data are converted to the prototype data using the relevant formulae (see 3.8.2.5). The influence of cavitation on the model performance and on the efficiency scale-up are dealt with in 3.8.2.3.7 and 3.8.2.4.2.

For all the following cases the first step is the determination of  $\eta_{hoptM}$ ,  $\delta_{ref}$  and  $\Delta\eta_h$  (see 3.8.2.2).

#### 3.8.2.3.1 Single-regulated turbine (figure 64)

The procedure described below applies to any type of impulse or reaction hydraulic machine.

The guaranteed efficiency is usually given for one specified speed and one or more specified specific hydraulic energies. As a result, it is necessary to obtain from the model test data a sufficient number of points or curves to cover the guarantees.

If the tests are carried out by choosing energy coefficients or speed factors nearly equal to the specified ones, it is possible to obtain a set of points or curves<sup>1)</sup>  $\eta_{hM}(Q_{nD})$  or  $\eta_{hM}(Q_{ED})$  to be used for comparison with guarantees. Because testing at exactly constant speed factor is not possible, the following procedure is recommended:

- measurement of a number of points sufficient to draw the three-dimensional surface (hill diagram) of:  $\eta_{hM}(E_{nD}, Q_{nD})$  or  $\eta_{hM}(E_{ED}, Q_{ED})$ ;
- sectionalize the three-dimensional surface representing the hydraulic efficiency at the energy coefficients or speed factors specified. Figure 64 shows the three-dimensional representative surface  $\eta_{hM}$  drawn versus energy and discharge coefficients and its section at the specified values of  $E_{nD} = E_{nDsp}$ .

The determination of the three-dimensional surface (hill diagram) is necessary if the guarantees are based on annual energy production.

For each  $E_{nDsp}$  (or  $E_{EDsp}$ ) the  $\eta_{hM}$  values obtained following one of the above procedures, enable the mechanical runner power coefficient  $P_{nD}$  (or factor  $P_{ED}$ ) curve to be calculated, for comparison with model guarantees.

<sup>1)</sup> For the determination of the best smooth curves, see for instance annex H.

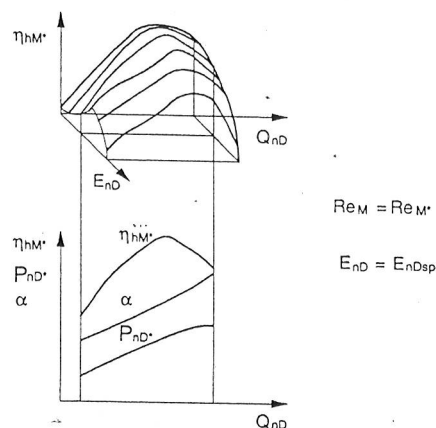


Figure 64 – Single-regulated turbine. Three-dimensional surface of hydraulic efficiency and curves of performance at  $E_{nD}$  constant

### 3.2.3.2 Single-regulated pump (figure 65)

The guaranteed efficiency and discharge are usually given for one specified speed and a specified range of specific hydraulic energy. As a result, it is necessary to obtain from the model test data a sufficient number of points or curves to cover the guarantees.

For different guide vane openings the  $\eta_{hM^*}(Q_{nD})$  and  $E_{nD}(Q_{nD})$  or  $\eta_{hM^*}(E_{nD})$  and  $Q_{nD}(E_{nD})$  curves<sup>1)</sup> are drawn and the relevant mechanical power coefficients  $P_{nD^*}$  are calculated (see figure 65). The guide vane openings will be chosen taking into account the guaranteed discharge and the power limits.

### 3.2.3.3 Double-regulated turbine (figure 66)

The guaranteed efficiency is usually given for one specified speed and one or more specified specific hydraulic energy. As a result, it is necessary to obtain from the model test data a sufficient number of points or curves to cover the guarantees.

In the tests are carried out by choosing energy coefficients or speed factors nearly equal to the specified ones, it is possible to obtain a set of points or curves<sup>1)</sup>  $\eta_{hM^*}(Q_{nD})$  or  $\eta_{hM^*}(Q_{ED})$  to compare with guarantees: the tests are usually performed considering the double-regulated turbine as a set of single-regulated turbines having different constant runner blade angles. Figure 66 shows the performance curve drawn for a Kaplan model turbine, measuring a number of points at six different runner blade angles  $\beta_1, \beta_2$ , etc. and keeping  $E_{nD}$  constant (equal to  $E_{nDsp}$ ): the on cam hydraulic efficiency  $\eta_{hM^*}$  curve is the envelope curve, determining the optimum guide vane/runner blade relationship<sup>2)</sup>.

<sup>1)</sup> For the determination of the best smooth curves, see for instance annex H.

<sup>2)</sup> The optimum relationships ( $\alpha, \beta$ ) on model and on prototype are only approximately the same (see 3.4).

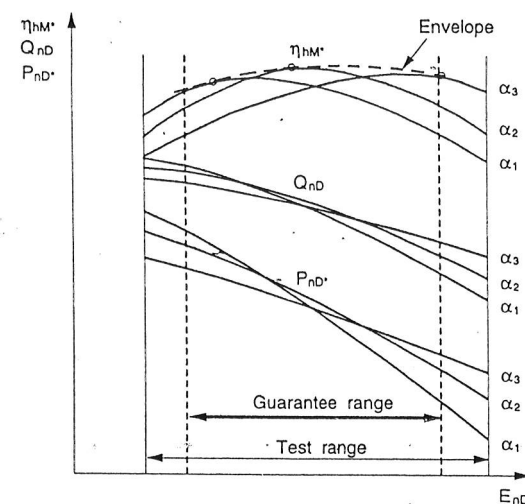


Figure 65 – Single-regulated pump. Performance curves

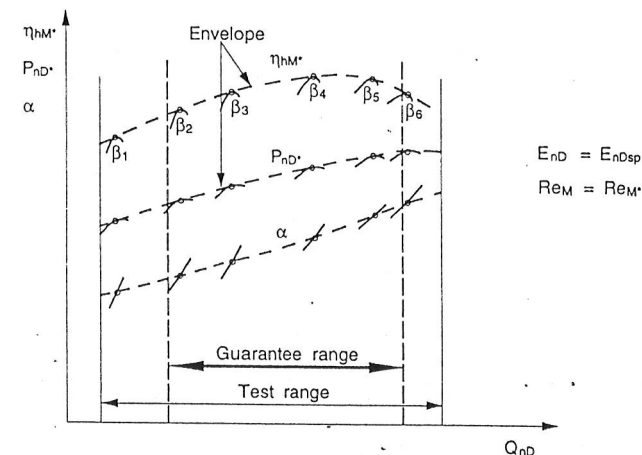


Figure 66 – Double-regulated turbine. Performance curves at  $E_{nD}$  constant

Since it is impossible to carry out testing at exactly constant energy coefficient or speed factor, the following procedure is recommended:

- measure a sufficient number of points to draw a three-dimensional surface (hill diagram) of:  $\eta_{hM^*}(E_{nD}, Q_{nD})$  or  $\eta_{hM^*}(E_{ED}, Q_{ED})$ , for the chosen runner blade angles;
- sectionalize the hill diagram representing the hydraulic efficiency at the energy coefficients or speed factors specified.

in this way the on-cam  $\eta_{HM}^*$  values are determined as in figure 66.

The determination of the hill diagram is necessary if the guarantees are based on annual energy production.

For each  $E_{nDsp}$  (or  $n_{EDsp}$ ) the  $\eta_{HM}^*$  values obtained, following one of the above procedures, enable the mechanical runner power coefficient  $P_{nD}^*$  (or factor  $P_{ED}^*$ ) curve to be calculated, for comparison with model guarantees.

#### 3.8.2.3.4 Double-regulated pump (figure 67)

The guaranteed efficiency and discharge are usually given for one specified speed and a specified range of specific hydraulic energy. As a result, it is necessary to obtain from the model test data a sufficient number of points or curves to cover the guarantees.

The procedure is the same as that for double-regulated turbines (see 3.8.2.3.3). Figure 67 shows the performance curves drawn for a double-regulated model pump keeping  $E_{nD}$  constant =  $E_{nDsp}$ .

For each  $E_{nDsp}$  (or  $n_{EDsp}$ ) the  $\eta_{HM}^*$  values obtained following one of the above procedures, enable the mechanical runner power coefficient  $P_{nD}^*$  (or factor  $P_{ED}^*$ ) curve to be calculated, for comparison with model guarantees.

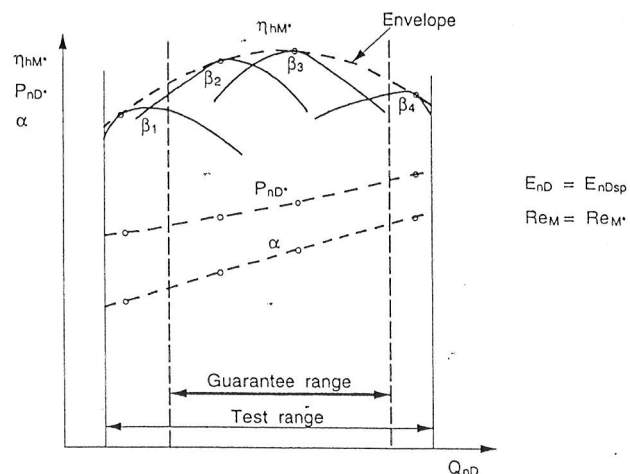


Figure 67 – Double-regulated pump. Performance curves at  $E_{nD}$  constant

#### 3.8.2.3.5 Non-regulated turbine (figure 68)

The guaranteed efficiency is usually given for one specified speed and a specified range of specific hydraulic energy. There is only one independent variable:  $E_{nD}$  (or  $Q_{nD}$ ) or  $n_{ED}$  (or  $Q_{ED}$ ) as shown in table 6.

The performance curves<sup>1)</sup> including the mechanical power coefficient  $P_{nD}^*$  or factor  $P_{ED}^*$ , computed through the hydraulic efficiency  $\eta_{HM}^*$ , are shown in figure 68. They are directly used for the comparison with the model guarantees.

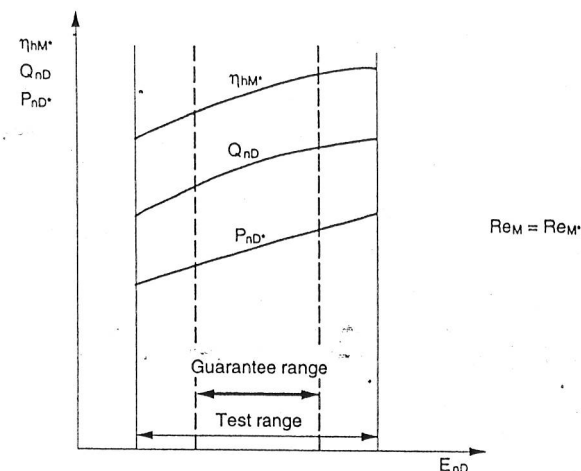


Figure 68 – Non-regulated turbine. Performance curves

#### 3.8.2.3.6 Non-regulated pump (figure 69)

The guaranteed efficiency and discharge are usually given for one specified speed and a specified range of specific hydraulic energy. There is only one independent variable:  $E_{nD}$  (or  $Q_{nD}$ ).

The performance curves<sup>1)</sup> including the mechanical runner power coefficient  $P_{nD}^*$ , computed through the hydraulic efficiency  $\eta_{HM}^*$ , are shown in figure 69. They are directly used for the comparison with the model guarantees.

<sup>1)</sup> For the determination of the best smooth curves, see annex H.

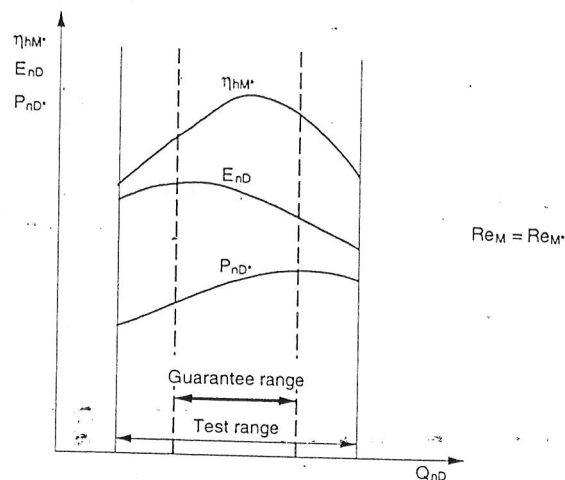


Figure 69 – Non-regulated pump. Performance curves

### 3.2.3.7 Influence of cavitation on model power, discharge and/or specific hydraulic energy and efficiency

is recommended to verify the influence of cavitation, characterized by the Thoma number (or a cavitation coefficient), on model performance<sup>1)</sup>. In 2.3.3.3.5 and 2.3.3.3.6 the test procedure is explained.

these tests reveal that within the range of guarantees an influence exists, figure 70 explains a procedure for correcting the efficiency curve, measured at  $\sigma_M > \sigma_{pl}$ , at a sufficient number agreed operating points. The cavitation influences on discharge and efficiency found at  $\sigma_{pl}$  are superimposed on the performance curves, measured at  $\sigma_M > \sigma_{pl}$ . The values of the hydraulic performance quantities, to be taken into account for the comparison with the guarantees, shall be those that consider the influence of cavitation under plant conditions, if any.

Figure 71 shows the curves of  $P_{ED}$ ,  $Q_{ED}$ , and  $\eta_{hM}$  drawn at one measured point by varying the Thoma number  $\sigma$  for a Francis model turbine or pump-turbine operating as a turbine; the curves of figure 72 refer to a model pump, or pump-turbine operating as a pump. In this last case, the curve of  $Q_{ED}$  has been replaced by the curve of  $E_{nD}$  because it is more relevant to pump performance. In the case of a pump,  $\sigma_{nD}$  replaces  $\sigma$  as  $E$  is variable during cavitation tests<sup>2)</sup>.

<sup>1)</sup> The NPSE and  $\sigma$ -values are determined in the low pressure reference section 2 of the model (see 1.3.3.6.5 and 3.6.6). Since only the free water levels in the suction channel of the plant are usually known, it is necessary, when isolating  $\sigma$ -factors at guaranteed performance points, to take into account the specific hydraulic energy dissipated between the tailwater level and section 2. In the case of a pump having a suction channel where the free water level can be measured close to section 2, the pump inlet losses can be considered negligible and the specific hydraulic energy at section 2 is assumed to correspond to its submergence. In other cases, an agreement shall be reached between the parties.

<sup>2)</sup> For pumps, it may also be useful to keep  $E_{nD}$  nearly constant, as shown in figure 71.

The Thoma number measured on the model is transferred to the prototype NPSE<sub>p</sub> using the formulae given in 3.8.2.5.3.

Where guarantees are given on the prototype, the cavitation influence on the scale-up formula is given in 3.8.2.4.2.

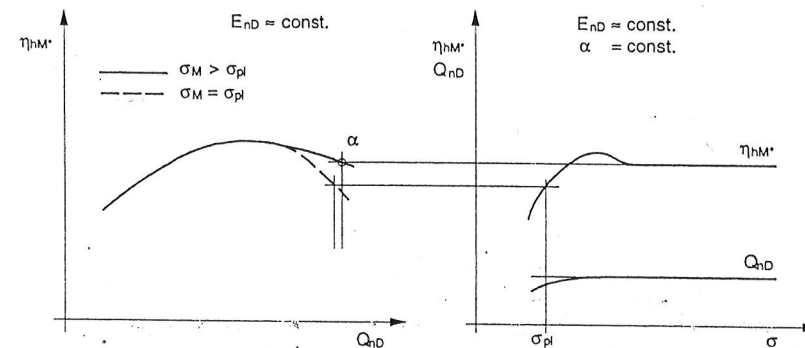


Figure 70 – Efficiency curve correction in order to take into account cavitation influence (e.g. tubular machines at overload operation)

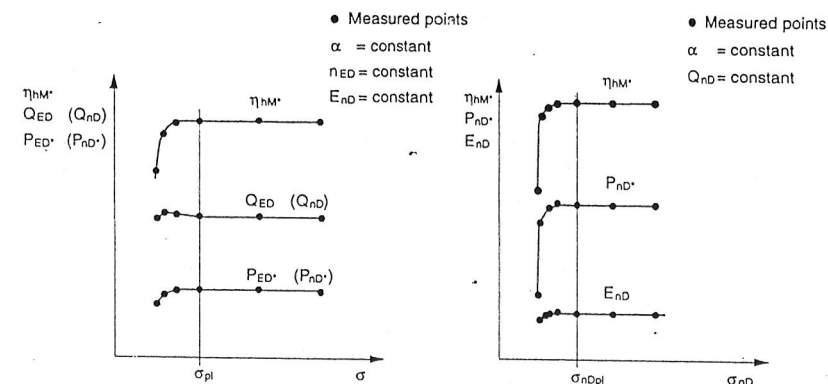


Figure 71 – Francis model turbine. Cavitation curves

Figure 72 – Model pump. Cavitation curves

## 8.2.4 Computation of prototype performance

### 8.2.4.1 Efficiency scale-up

For a reaction machine, if the guarantees are referred to prototype, the model efficiencies  $\eta_{hM}$  measured at different Reynolds numbers  $Re_M$  are scaled up to the prototype Reynolds number  $Re_P$  using the following formula:

$$(\Delta\eta_h)_{M \rightarrow P} = \delta_{ref} \left[ \left( \frac{Re_{ref}}{Re_M} \right)^{0.16} - \left( \frac{Re_{ref}}{Re_P} \right)^{0.16} \right]$$

The value of  $Re_{ref}$  and the formula to calculate  $\delta_{ref}$  are given in 3.8.2.2 a).

If the model hydraulic efficiency has been measured at constant Reynolds number  $Re_{M^*}$ , or has been scaled to a constant Reynolds number  $Re_{MSP}$ ,  $\Delta\eta_h$  is a constant value within the range of guaranteed efficiencies if, as usually happens,  $n_P$  and consequently  $Re_P$  are constant (see figure F.3).

If the model hydraulic efficiency has been measured at different Reynolds numbers,  $\Delta\eta_h$  shall be calculated for each measured point, taking into account the relevant  $Re_M$  (see figure F.4).

For an impulse turbine, if it has been contractually agreed to take into account a scale effect on efficiency,  $(\Delta\eta_h)_{M \rightarrow P}$  may be calculated according to annex K.

Other data concerning the main hydraulic performance of the prototype (discharge, specific hydraulic energy and mechanical runner/impeller power) are obtained from the formulae of 3.8.2.5. The prototype mechanical runner/impeller power is computed taking into account the scale effect on the hydraulic efficiency.

The procedure of drawing<sup>1)</sup> the curves of prototype performance, and of determining the curves to be compared with the prototype guarantees is the same as the one established for guarantees given on the model (see 3.8.2.3).

### 8.2.4.2 Influence of cavitation on applicability of scale up formula

While no scientifically founded theory for scale-up under cavitating conditions exists, it is generally agreed that the scale-up calculated for non-cavitating conditions can be applied at  $\sigma$ -values where the performance is not influenced by cavitation.

By convention, this scale-up may continue to be applied if the increase or decrease of hydraulic efficiency, due to the decrease of Thoma number  $\sigma$ , does not exceed 0,5 %, unless otherwise agreed (see figure 73).

Where the efficiency is affected by more than 0,5 %, the relationship between model and prototype performance is less certain and an *a priori* agreement regarding this relationship shall be reached between the parties.

The value of  $P_{mP}$  is determined on the basis of the values of  $\eta_{hP}$ ,  $Q_P$ ,  $E_P$  at  $\sigma_{pl}$ .

<sup>1)</sup> For the determination of the best smooth curves, see annex H.

In large tubular turbines, if Froude's similarity cannot be fulfilled (see 2.3.1.5.1), a scale-up method of the cavitation characteristics from model to prototype should take into account the vertical distribution of cavitation, as for example shown in [17].

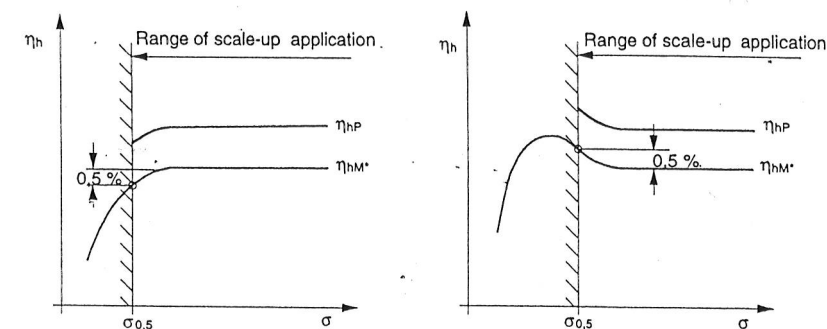


Figure 73 – Francis model turbine: cavitation curves. Examples of limits for application of scale-up formula

### 3.8.2.5 Formulae for computation of prototype performance within the guaranteed efficiency range

The model test data provide for each point, the discharge  $Q_{1P}$ , the specific hydraulic energy  $E_P$  and the mechanical runner/impeller power  $P_{mP}$  of the geometrically similar prototype operating in hydraulically similar conditions (see 2.3.1.2), by using the formulae listed below.

#### 3.8.2.5.1 Reaction machines

The scale effect due to a Reynolds number influence on hydraulic efficiency is taken into account on mechanical runner/impeller power<sup>1)</sup>. Since available data for scaling-up discharge and specific hydraulic energy do not show consistent trends, it has been assumed that only efficiency and power (due to efficiency increase) are influenced by scale effect<sup>2)</sup>.

Two procedures are possible:

a) Direct calculation from model measured data

$$\eta_{hP} = \eta_{hM} + (\Delta\eta_h)_{M \rightarrow P}$$

where  $(\Delta\eta_h)_{M \rightarrow P}$  is calculated by the formula given in 3.8.2.4.1.

<sup>1)</sup> In the case of axial turbines operating under low specific hydraulic energy far from the best efficiency point, some measurements show a power different from that calculated according to this standard.

<sup>2)</sup> Sometimes, tests on prototypes show shifting effects on  $Q_{1P} = f(E_P)$  curves and consequently on  $P_{mP} = f(E_P)$  curves compared to corresponding model curves. Shifting effects on  $Q_{1P} = f(E_P)$  have to be taken into account in determining the maximum mechanical power of a pump. A possible approach is given in the JMSE S008 Standard [18], which applies the formula:

$$P_{mP} = P_{mM} \left( \frac{P_{1P}}{P_{1M}} \right)^3 \left( \frac{D_P}{D_M} \right)^5$$

$$Q_{1P} = Q_{1M} \left( \frac{D_P}{D_M} \right)^2 \left( \frac{E_P}{E_M} \right)^{0.5} = Q_{1M} \left( \frac{D_P}{D_M} \right)^3 \frac{n_P}{n_M}$$

$$E_P = E_M \left( \frac{D_P}{D_M} \right)^2 \left( \frac{n_P}{n_M} \right)^2$$

or turbine:

$$P_{mP} = \rho_{1P} Q_{1P} E_P \eta_{hP} = P_{mM} \frac{\rho_{1P}}{\rho_{1M}} \left( \frac{D_P}{D_M} \right)^2 \left( \frac{E_P}{E_M} \right)^{1.5} \frac{\eta_{hP}}{\eta_{hM}} = P_{mM} \frac{\rho_{1P}}{\rho_{1M}} \left( \frac{D_P}{D_M} \right)^5 \left( \frac{n_P}{n_M} \right)^3 \frac{\eta_{hP}}{\eta_{hM}}$$

$$\text{sing } P_{mM} = \rho_{1M} Q_{1M} E_M \eta_{hM}$$

or pump:

$$P_{mP} = \frac{\rho_{1P} Q_{1P} E_P}{\eta_{hP}} = P_{mM} \frac{\rho_{1P}}{\rho_{1M}} \left( \frac{D_P}{D_M} \right)^2 \left( \frac{E_P}{E_M} \right)^{1.5} \frac{\eta_{hM}}{\eta_{hP}} = P_{mM} \frac{\rho_{1P}}{\rho_{1M}} \left( \frac{D_P}{D_M} \right)^5 \left( \frac{n_P}{n_M} \right)^3 \frac{\eta_{hM}}{\eta_{hP}}$$

$$\text{sing } P_{mM} = \frac{\rho_{1M} Q_{1M} E_M}{\eta_{hM}}$$

) Calculation from the dimensionless factors (or coefficients) previously computed from model measured data

$$\eta_{hP} = \eta_{hM} + (\Delta \eta_h)_{M \rightarrow P}$$

$$Q_{1P} = Q_{ED} D_P^2 E_P^{0.5} = Q_{nD} D_P^3 n_P$$

$$E_P = \frac{1}{n_{ED}^2} D_P^2 n_P^2 = E_{nD} D_P^2 n_P^2$$

$$\text{or turbine: } P_{mP} = P_{ED} \rho_{1P} D_P^2 E_P^{1.5} \frac{\eta_{hP}}{\eta_{hM}} = P_{nD} \rho_{1P} D_P^5 n_P^3 \frac{\eta_{hP}}{\eta_{hM}}$$

$$\text{or pump: } P_{mP} = P_{ED} \rho_{1P} D_P^2 E_P^{1.5} \frac{\eta_{hM}}{\eta_{hP}} = P_{nD} \rho_{1P} D_P^5 n_P^3 \frac{\eta_{hM}}{\eta_{hP}}$$

The above formulae can also be applied when the measured hydraulic efficiency of the model has been referred to a constant Reynolds number ( $\eta_{hM}^*$ ) (see 3.8.1).

### 3.8.2.5.2 Impulse turbines (Pelton)

The formulae in 3.8.2.5.1 apply under the following conditions:

- if no scale effect is taken into account, it is assumed that  $\eta_{hP} = \eta_{hM}$ ;
- if it is contractually agreed to take a scale effect into account, then  $(\Delta \eta_h)_{M \rightarrow P}$  may be calculated according to annex K.

### 3.8.2.5.3 Formulae for computation of prototype NPSE<sub>P</sub>

The net positive suction specific energy of the prototype is calculated by one of the following formulae:

$$NPSE_P = \sigma \cdot E_P = \sigma_{nD} \cdot n_P^2 D_P^2$$

## 3.8.3 Computation of steady-state runaway speed and discharge

### 3.8.3.1 Determination of the model steady-state runaway curves

The Reynolds number scale effect is assumed zero in the range near to the runaway operation. The effect of the Thoma number on the runaway curves may be significant (see 3.8.3.2).

In the case of a single-regulated machine model, for each point a set of readings and/or recordings of physical quantities used to determine the model steady-state runaway speed and discharge is recorded, with  $T_{mM} = 0$  (see 2.3.3.3.7).

The average values of  $E_M$ ,  $Q_{1M}$ ,  $n_M$  and  $NPSE_M$  are then computed;  $n_{ED,R}$  and  $Q_{ED,R}$  (or  $E_{nD,R}$  and  $Q_{nD,R}$ ) are finally derived using the formulae of 1.3.3.12.

The runaway curve<sup>1)</sup> is drawn for different openings  $\alpha$  or  $s$  in figure 74 to obtain the maximum steady state runaway speed  $n_{ED,Rmax}$  and discharge  $Q_{ED,Rmax}$ .

For a double-regulated machine model, a runaway curve is usually drawn for each runner/impeller blade angle  $\beta$ . The envelope curve of these curves is drawn to define the maximum runaway speed and discharge (see figures 78 and 79).

For a non-regulated machine model, the runaway curve is reduced to a point when using dimensionless factors or coefficients.

The runaway tests shall be carried out by varying the guide vane opening, runner/impeller blade angle or needle stroke, over all the guaranteed range.

For Pelton turbines, the maximum runaway speed is determined taking into account the influence of the number of nozzles (see figure 75).

If, during the tests, it is not possible to reach  $T_{mM} = 0$ , the runaway conditions can be determined by extrapolation (see figure 76).

<sup>1)</sup> For a pump, the runaway speed and discharge are usually called reverse runaway speed and reverse runaway discharge.

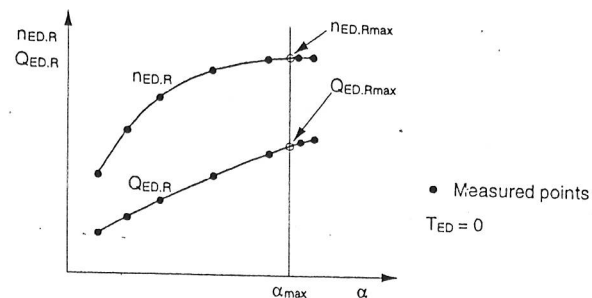


Figure 74 – Runaway curves for a single-regulated turbine (Francis)

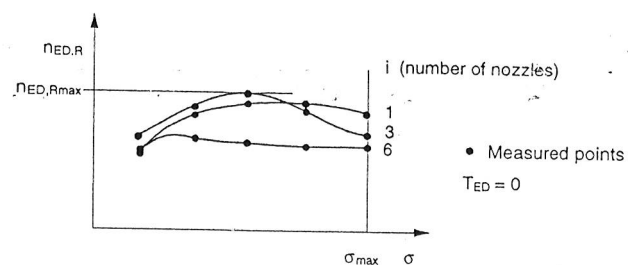


Figure 75 – Runaway curves for a single-regulated turbine (six-nozzle Pelton)

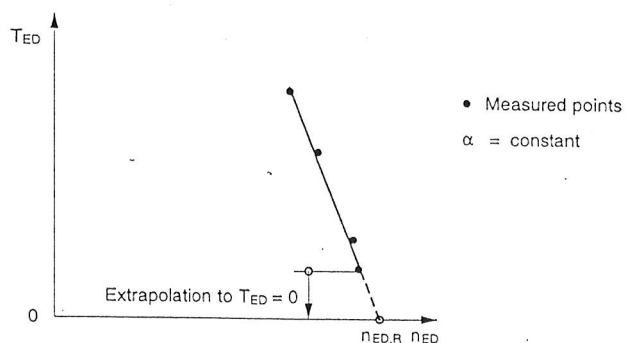


Figure 76 – Runaway speed determined by extrapolation. Example for a single-regulated turbine (Francis)

### 3.8.3.2 Influence of cavitation on steady-state runaway speed and discharge

It is recommended that the influence of Thoma number on model performance is also verified at runaway conditions. Subclause 2.3.3.3.7 details the test procedure.

Figure 77 shows the cavitation influence for a medium specific speed Francis turbine model at guide vane opening  $\alpha_{\max}$ .

Cavitation has a large influence on runaway curves of a Kaplan turbine model. Figure 78 shows the cavitation curves  $n_{ED,R}$  and  $Q_{ED,R}$  at different guide vane openings  $\alpha$  and runner blade angles  $\beta$ . The same phenomenon is represented in figure 79, which shows the  $n_{ED,R}(Q_{ED,R})$  curves at high  $\sigma$  and at  $\sigma = \sigma_{pl}$ .

The Thoma number or the cavitation coefficient measured on the model is usually transferred to prototype  $NPSE_p$  using the formulae given in 3.8.2.5.3.

In large tubular turbines, if the Froude similitude cannot be fulfilled (see 2.3.1.5.1), a conversion method of cavitation characteristics from model to prototype should take into account the vertical distribution of cavitation as, for example, shown in reference [19].

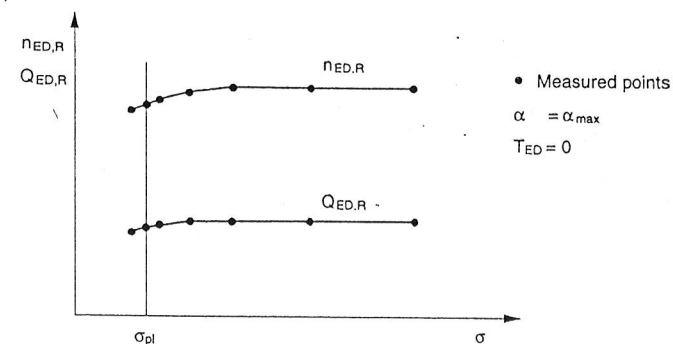


Figure 77 – Influence of Thoma number on runaway speed and discharge of a single-regulated turbine (Francis)

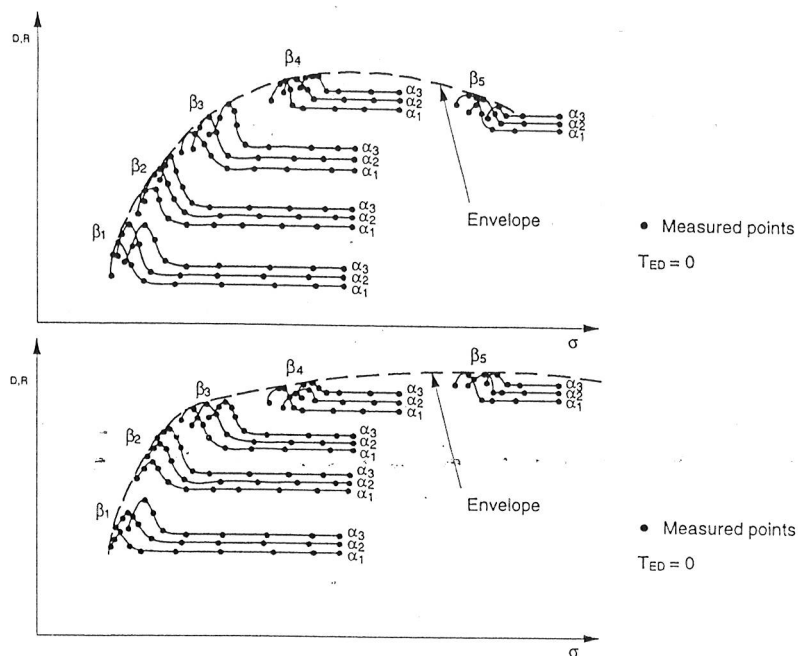


Figure 78 – Influence of the Thoma number on runaway speed and discharge of a double-regulated turbine (Kaplan)

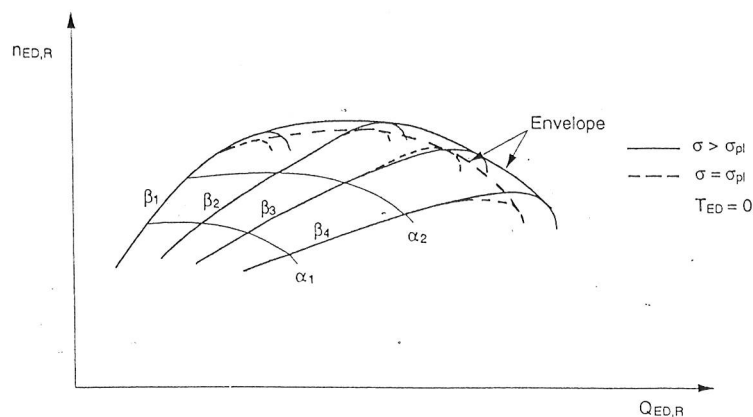


Figure 79 – Influence of the Thoma number on the off cam runaway curves of a double-regulated turbine (Kaplan)

### 3.8.3.3 Computation of the prototype steady-state runaway curves

If runaway guarantees are given for the prototype, no scale effect is usually considered: this means that  $P_{ED,M} = P_{ED,P}$  in the range near to the runaway point. The prototype runaway data are computed at  $\sigma_{pl}$  from the model test results using formulae based on the affinity laws (see 3.8.3.4) and hence the maximum runaway speed and discharge points are determined. If required, the friction losses of the unit thrust bearing, guide bearings and shaft seal and the mechanical and windage losses of the electrical machine are taken into account, unless otherwise agreed, as described in annex G.

### 3.8.3.4 Formulae for computation of prototype runaway characteristic

Two procedures are possible:

a) Direct calculation from model measured data

$$\eta_{R,P} = \eta_{R,M} \left( \frac{D_M}{D_P} \right)^{0,5} \quad Q_{1,RP} = Q_{1,RM} \left( \frac{D_P}{D_M} \right)^2 \left( \frac{E_P}{E_M} \right)^{0,5}$$

The formula

$$P_{mP} = P_{mM} \frac{\rho_{1P}}{\rho_{1M}} \left( \frac{D_P}{D_M} \right)^2 \left( \frac{E_P}{E_M} \right)^{1,5}$$

is used to draw a curve  $P_{mP}(\eta_P)$  necessary to take into account the bearings and shaft seal friction losses and the windage losses (see annex G).

b) Calculation from the dimensionless factors (or coefficients) previously computed from model measured data

$$\eta_{R,P} = \eta_{ED,R} \frac{E_P^{0,5}}{D_P} \quad Q_{1,RP} = Q_{ED,R} D_P^2 E_P^{0,5}$$

The formula

$$P_{mP} = P_{ED} \cdot \rho_{1P} \cdot D_P^2 \cdot E_P^{1,5}$$

is used to draw a curve  $P_{mP}(\eta_P)$  necessary to take into account the bearings and shaft seal friction losses and the windage losses (see annex G).

For the computation of NPSE<sub>P</sub>, see 3.8.2.5.3.

## 3.9 Error analysis

### 3.9.1 Basic principles (see ISO 5168)

Starting from the measurements made on the model the different sources of error shall be examined to determine the corresponding uncertainties.

#### 3.9.1.1 Definition of the error

The error in the measurement of a quantity is the difference between that measurement and the true value of the quantity.

A measurement of a physical quantity is free from uncertainties arising from systematic and random errors.

Systematic errors cannot be reduced by repeating measurements since they arise from the characteristics of the measuring apparatus, the installation and the operating conditions. However, random errors can be reduced by repetition of measurements since the random error of the mean of  $n$  independent measurements is  $\sqrt{n}$  times smaller than the random error of an individual measurement (see annex L).

### 3.1.2 Definition of uncertainty

The range within which the true value of a measured quantity can be expected to lie, with a suitably high probability, is termed the uncertainty in the measurement. For the purpose of this standard, the probability to be used shall be 95 % confidence level.

The uncertainty in the measurement of a quantity  $X$  may be expressed as an absolute value  $e_X$  or as a relative value:  $f_X = e_X / X$ .

### 3.1.3 Types of errors

Three types of error shall be considered:

- spurious errors (see 3.9.1.3.1);
- random errors (see 3.9.1.3.2);
- systematic errors (see 3.9.1.3.3).

#### 3.1.3.1 Spurious errors

These are errors such as human errors, or instrument malfunction, which invalidate a measurement. For example, the transposing of numbers in recording data or the presence of pockets of air in leads from a water line to a manometer. Such errors should not be incorporated into any statistical analysis and the corresponding measurement shall be discarded. Where the error is not large enough to make the result obviously invalid, the point shall be repeated or some rejection criteria may be applied to decide whether the data point could be rejected (see for example [20]).

#### 3.1.3.2 Random errors and associated uncertainty

Random errors are caused by numerous, small, independent influences which prevent a measurement system from delivering the same reading (repeatability of the measurement system) when supplied with the same input value of the quantity to be measured. The measurements deviate from their mean in accordance with the laws of chance, such that their distribution usually approaches a normal (gaussian) distribution as the number of measurements is increased.

The random error is influenced by the care taken during the measurements, the number of measurements and the operation conditions. The scatter of the readings observed during a test results from the combination of the random error arising from the instrumentation and of the influence of the operating conditions. The repetition of points at a given operating condition enables the value of the uncertainty associated with random errors to be established by statistical methods (see 3.9.2.2.1 and annex L).

When the sample size (i.e. the number of measurements) is small, it is necessary to correct the statistical results that are based on the assumption of a normal distribution, by means of the Student's  $t$  value, as explained in annex L. Student's  $t$  is a factor which compensates for the uncertainty in the standard deviation increasing, for a given confidence level, as the sample size is reduced.

### 3.9.1.3.3 Systematic errors and associated uncertainty

A systematic error is one that invariably has the same magnitude and the same sign under the same conditions of measurement. Therefore it cannot be reduced by increasing the number of measurements if the equipment and conditions of measurements remain unchanged.

Systematic errors do not affect the repeatability of measurements during a test.

The uncertainty associated with systematic errors cannot be assessed experimentally without changing the equipment or conditions of measurements. The only way to verify the main measuring system and to obtain an order of magnitude of the systematic error is to measure each basic quantity by two different systems, if they are available.

The alternative is to make a subjective judgement on the basis of experience and consideration of the equipment involved.

If the error has a unique known value then this should be added to (or subtracted from) the result of the measurement and there is no longer systematic uncertainty in the measurement due to this source.

If the systematic error of a measuring device is unknown but its error limits (class of accuracy) are specified, the interval between them may be assumed as the systematic uncertainty of that device with a confidence level better than 95 %.

Notwithstanding the difference shown above between systematic and random uncertainties, the probability distribution of the uncertainty values of each systematic component is essentially gaussian and the accepted convention calculating the total systematic uncertainty  $f_s$  from the individual systematic uncertainties is the root-sum-square method.

#### 3.9.1.4 Total uncertainty

The total uncertainty in a measurement ( $f_t$ ) is obtained by combining the systematic ( $f_s$ ) and random ( $f_r$ ) uncertainties (see 3.9.1.3.3 and 3.9.1.3.2). It defines a range within which the true value is assumed to lie with a probability of 95 % and any point in this range is equally valid.

Given the same type of probability distribution of the systematic and random uncertainties, they can be combined by the root-sum-squares method. Subclause 3.9.2.2.4 explains how to determine the total uncertainty in model tests.

### 3.9.2 Determination of uncertainties in model tests

#### 3.9.2.1 Sources of errors

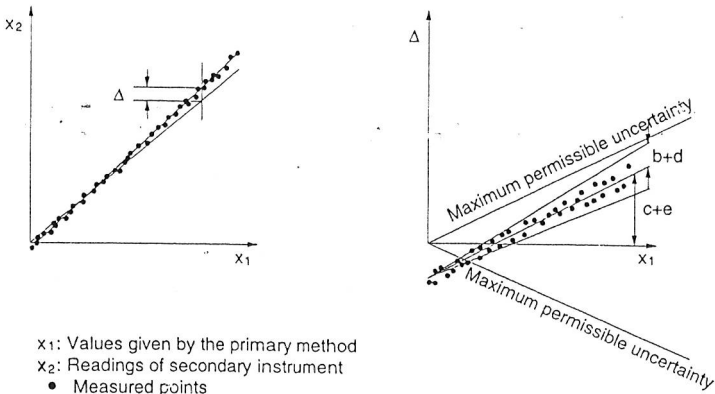
Table 8 provides a summary of the most important sources of error which can occur during model tests.

Clause J.1 gives an example of analysis of the sources of error and of uncertainty evaluation when measuring a quantity by a secondary electronic device.

2.1.1 Errors arising during the calibration of a secondary instrument

sides possible spurious errors which should be eliminated, systematic and random errors occur during the calibration of a secondary measuring instrument. The bias<sup>1)</sup> of the primary method and of the secondary instrument and the errors in physical properties are systematic errors, whereas the repeatability of the primary method and of the secondary instrument are random errors; the errors due to physical phenomena and influence quantities may be of partly systematic and partly random nature.

a total uncertainty in the calibration of the secondary instrument may be calculated by combining, by the root-sum-square method, the component uncertainties (see table 8 and use J.1), as far as each of them can be evaluated. In practice, a calibration result represented by the example shown in figure 80 may be used to estimate the value of errors ns b) to e) of table 8. Item f) is generally negligible, item a) (bias of the primary method) could be obtained from a higher level in the calibration chain (traceability of the primary method) or certified by a neutral authority.



x<sub>1</sub>: Values given by the primary method  
x<sub>2</sub>: Readings of secondary instrument  
• Measured points  
b), c), d), e): see Table 8

Figure 80 - Example of calibration curve

2.1.2 Errors arising during the tests

Whatever the nature of its individual components, the total error in the calibration (item g) described in 3.9.2.1.1 becomes a systematic error in the measured quantity when this calibration is used for subsequent model tests.

<sup>1)</sup> The bias error is the systematic component of the error of a measuring instrument.

Table 8 - Summary of errors

During calibration		During test	
a) Bias of primary method	Total error of primary method	g) Total error in the calibration of the secondary instrument ( $f_{cal}$ )	Total error in the measurement ( $f_t$ )
b) Repeatability of primary method			
c) Bias of secondary instrument	Total error of secondary instrument	h) Additional systematic error in secondary instrument i) Errors in physical properties k) Errors due to physical phenomena and influence quantities <sup>1)</sup> l) Repeatability of secondary instrument	Systematic error in the measurement ( $f_s$ ) Random error in the measurement ( $f_r$ )
d) Repeatability of secondary instrument			
e) Error due to physical phenomena and influence quantities <sup>1)</sup>			
f) Errors in physical properties			

NOTE: Items a) to l) are cross-referenced with annex J

1) Influence quantity : a quantity which is not the subject of the measurement but that affects the result of the measurement

NOTE: Items a) to l) are cross-referenced with annex J  
<sup>1)</sup> Influence quantity: a quantity which is not the subject of the measurement but that affects the result of the measurement

The errors due to physical phenomena and influence quantities occurring during the tests (item k) may be neglected if the conditions of measurement (ambient temperature, voltage and frequency of the power supply, flow pattern, etc.) are maintained within a reasonable range during calibration and tests.

Since error in the determination of physical properties (item j) is generally small, the systematic error is largely controlled by the choice of the calibration method, the characteristics of the measuring apparatus, the installation and the operating conditions. For example, the value of the kinetic energy calculated with the mean velocity differs from its true value if the velocity distribution at the measuring section is not uniform (see 3.5.2.4, note 1).

The repeatability of the secondary instrument appears once again during the tests (item l) and results in a random error which may be characterized as stated in 3.9.2.2.1.

### 3.9.2.2 Estimation of the uncertainty

#### 3.9.2.2.1 Uncertainty associated with random errors

An agreement between the parties prior to the test should specify the maximum permissible value of the uncertainty,  $f_r$ , for each quantity subject to guarantee. In the absence of such an agreement, the maximum permissible value of the random uncertainty in the hydraulic efficiency near the optimum should be  $(f_{rh})_r = \pm 0,1 \%$ .

The actual value of the random uncertainties shall be estimated during the test at some operating points in a range in which the model runs in stable conditions (e.g. in the range near the point of maximum efficiency). For each of these points, the measurements shall be repeated a sufficient number of times (e.g. at least five) for applying the procedure described in annex L.

If, in these check points, the observed random uncertainties are lower than the previously agreed values, the maximum permissible levels of the random uncertainty are deemed satisfied in the whole guaranteed operating range, even if the direct evaluation of the random uncertainty in operating points with disturbed conditions gives higher values than the agreed value. In disturbed operating conditions (for instance a Francis turbine operating at partial load), the scatter of the measurements may be greatly increased; these higher values may nevertheless be accepted, for they arise from the model and not from the instrumentation.

If, in the check points, more than 5 % of the results are outside the agreed range, an accurate analysis of the conditions of measurement shall be made and the measurements shall be repeated or a new uncertainty bandwidth value due to the random errors agreed.

#### 3.9.2.2.2 Uncertainty associated with systematic errors

The first step in estimation of this uncertainty is to identify each component which can influence its value. The second step is to allocate uncertainty limits to allow for each of these components. This may be done, in part at least, by statistical analysis (see for example ISO 5168).

The systematic error of a measurement is given mainly by the systematic error due to the calibration of the secondary instrument, and by the errors in physical properties.

The following considerations are useful in evaluating the systematic uncertainty (see table 8 and annex J).

- a) As explained in 3.9.2.1.2, almost all the sources of systematic errors are covered by the calibration of the secondary instrument. In most cases, the systematic uncertainty in the measurement of a quantity may be taken as equal to the total uncertainty in the calibration of the secondary instrument used for the test  $f_s \approx f_{cal}$ , but it shall be borne in mind that in some circumstances other sources of error may need to be taken into account.
- b) According to the measuring method and instrument used, systematic uncertainty consists of some of the following components:
  - the total uncertainty  $f_{t1}$  proper to the primary method shall be established before the calibration (see 3.9.2.1.1);
  - the uncertainty  $f_d$  is due to the random error of the secondary instrument during a calibration and to the scatter of several calibrations carried out at various periods if no systematic trend appears. For instance, if the calibration coefficient used during the test results from the average of  $n$  calibrations characterized by a standard deviation  $s_c$ , this component uncertainty may be taken as equal to:

$$f_d = \pm \frac{ts_c}{\sqrt{n}}$$

where  $t$  is the Student's coefficient for  $(n - 1)$  degrees of freedom (see table L.2);

- the bias of the secondary instrument and the uncertainty due to the effect of physical phenomena and influence quantities are covered by the calibration, and the residual uncertainty in the applied correction can generally be omitted;
  - the errors in physical properties, if any, are small; for instance, the uncertainty  $f_p$  in the water density is lower than  $\pm 0,05 \%$ ;
  - an additional uncertainty may arise from the regression process used to determine the calibration curve. Although this uncertainty can be evaluated in accordance with ISO 7066, a conventional value of say  $\pm 0,05 \%$  may be assumed.
- c) The systematic uncertainty  $f_{s2}$  in a measurement made by the secondary method may then be obtained by combining these component uncertainties by the root-sum-square method.

Each clause concerning the measurement of one of the quantities necessary to determine the hydraulic performance of the model gives an indication of the relevant systematic uncertainty.

This value applies when the measurements are made in normal conditions by experienced personnel with apparatus of high quality, in accordance with the provisions of this standard, and can be used as a guide to establish the value of systematic uncertainty.

Prior to the test, an agreement between the parties shall specify the systematic uncertainty bandwidth for the different quantities, including the hydraulic efficiency. The actual value of the systematic uncertainties, like those of the random uncertainties, depends on many factors, some of which can only be evaluated after completion of the test. A review of these factors shall be made and agreement established as to whether the expected uncertainties have to be changed on technical grounds or not.

### 3.2.3 Uncertainty in a derived quantity

The uncertainty (systematic or random) of a derived quantity is determined by combining the uncertainties of the component measurements by the root-sum-square method.

For example, the systematic uncertainty in hydraulic efficiency  $(f_{\eta h})_s$  is computed from the individual systematic uncertainties in discharge  $(f_Q)_s$ , specific hydraulic energy  $(f_E)_s$ , torque  $(f_T)_s$ , speed of rotation  $(f_n)_s$  and density of water  $(f_p)_s$  by:

$$(f_{\eta h})_s = \pm \sqrt{(f_Q)_s^2 + (f_E)_s^2 + (f_T)_s^2 + (f_n)_s^2 + (f_p)_s^2} \quad (\text{see annex J})$$

For contractual purposes it is conventionally accepted to omit the uncertainty associated with the scale-up formula of the hydraulic efficiency.

### 3.2.4 Total uncertainty

The total uncertainty (see table 8) in any quantity is given by:

$$f_t = \pm \sqrt{f_s^2 + f_r^2}$$

When the random uncertainty (evaluated as prescribed in 3.9.2.2.1) is lower than or equal to the maximum permissible value (generally  $\pm 0,1 \%$ ) it is assumed to be conventionally equal to this value, which shall then be used to calculate the total uncertainty.

When, in some operating points, the conditions of measurement are disturbed and the scatter of the readings (see 3.9.2.2.1) results in an increase of the observed random uncertainty, it is reasonable to take into account the observed value instead of the previously agreed one for calculating the total uncertainty.

## 10 Comparison with guarantees

### 10.1 General

It is recommended that the test results, calculated according to 3.8, are compared with guarantees using the methods of presentation and analysis described below, taking into account the total uncertainty bandwidth (see 3.10.2) and the contractual limits (see 3.10.3). For simplicity's sake, only prototype power, discharge and/or specific hydraulic energy, hydraulic efficiency and steady state runaway speed and discharge are considered hereafter (see 1.4.2).

Comparison with prototype guarantees shall consider the effect of cavitation (see 3.8.2.4.2 and 8.3.2).

Comparison with guarantees given on the model is made directly using the same procedures.

It is recommended that hydraulic efficiency is presented versus discharge (or specific hydraulic energy, in case of non-regulated machines) and not versus power.

The systematic uncertainty  $(f_p)_s$  in density of water may generally be neglected.

### 3.10.2 Interpolation curve and total uncertainty bandwidth

Different methods and criteria can be used to draw the interpolation curve ranging from the manual to the more sophisticated ones (one of the possible methods of drawing is briefly described in annex H). The final choice of the interpolation method shall be clearly defined and agreed between the parties.

Taking into account the total uncertainties calculated per 3.9.2, each measured point can be represented on a diagram by an ellipse. The semi-axes of this ellipse represent the total uncertainty, at a confidence level of 95 %, in the two quantities chosen as co-ordinates of the diagram. Any point within this ellipse is equally valid.

An uncertainty band corresponding to the upper and lower envelopes of these ellipses is superimposed on the curve drawn through the test points (interpolation curve). All the points within this band are equally valid and hence this band constitutes an acceptable bandwidth for the comparison with the guarantees.

The ellipses need only be used when evaluating the guaranteed points or whenever the result of the comparison is not sufficiently clear (see figure 83, details X and Y). In most other cases, it is possible to simplify the procedure and to determine the total uncertainty bandwidth by reducing the ellipses to their principal axis when for example the error on the abscissa can be neglected (see figure 86), or the measured curve across the guaranteed point is almost horizontal, or has only a small gradient.

If the guarantees are given by points, it is recommended that the measured points be selected as near as possible to the guaranteed points: figures 81 and 82 show two examples concerning the hydraulic efficiency of a single and a double-regulated turbine, respectively.

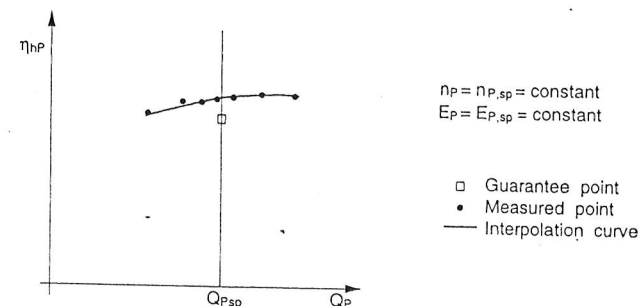


Figure 81 – Single-regulated machine

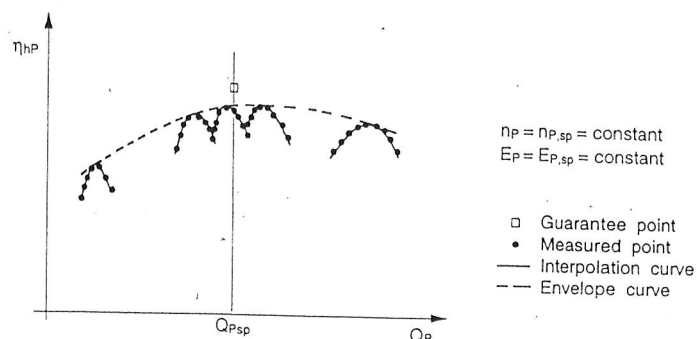


Figure 82 – Double-regulated machine

### 10.3 – Power, discharge and/or specific hydraulic energy and efficiency in the guarantee range

The following classes of machines will be dealt with:

- regulated turbine;
- non-regulated turbine;
- non-regulated or regulated pump.

#### 10.3.1 Regulated turbine

The hydraulic efficiency guarantee is given at one or more specified powers or discharges, it is met if, at the specified speed and specified specific hydraulic energy, the guaranteed single values lie below the upper limit of the total uncertainty bandwidth at the specified powers or discharges.

If the hydraulic efficiency guarantee is given as a weighted or arithmetic average efficiency, it is met if, at the specified speed and specified specific hydraulic energy, the guaranteed average efficiency is less than the average efficiency calculated at the same specified discharges (or powers) using the upper limit of the total uncertainty bandwidth.

In the case of guarantees given at different  $E_{p,sp}$ , a diagram similar to figure 83 shall be drawn for each specified specific hydraulic energy.

For double-regulated turbines, the curves to be compared with the guarantees are drawn as envelope curves.

Figure 83 gives an example of comparison with guarantees given at four operating points, at a specified  $E_p$ , in the case of a single-regulated turbine. It shows that:

- a) the hydraulic efficiency guarantee is not met at D (see detail X);
- b) the mechanical runner power guarantee is not met because the guaranteed power is not reached even if the upper limit of the uncertainty bandwidth is taken into account (see detail Y).

The curve  $\alpha(Q_p)$  is drawn to determine:

- the maximum opening  $\alpha_{max}$  for the runaway test (see figure 86);
- if a sufficient safety margin exists between the guaranteed power and the mechanical runner/impeller power saturation.

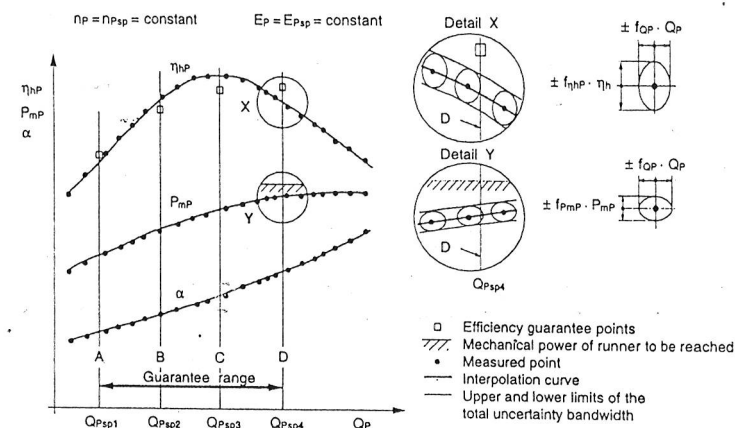


Figure 83 – Single-regulated turbine. Comparison between guarantees and measurements

#### 3.10.3.2 Non-regulated turbine

If the hydraulic efficiency guarantee is given at one or more specific hydraulic energy, it is met if, at the specified speed, the guaranteed single values lie below the upper limit of the total uncertainty bandwidth.

If the hydraulic efficiency guarantee is given as weighted or arithmetic average efficiency, it is met if, at the specified speed, the guaranteed average efficiency is less than the average efficiency calculated at the same specific hydraulic energies using the upper limit of the total uncertainty bandwidth.

The mechanical runner power limit is usually defined, if not otherwise agreed, by a lower limit  $kP_{mP,sp}$  and a higher limit  $(k + 0,03) P_{mP,sp}$ ,  $k$  being a mutually agreed value lying somewhere between 0,97 and 1,0. Normally, the value of  $k$  is 0,985. The choice of  $k$  shall be compatible with the guaranteed limit of  $P_{mP}$ .

Figure 84 gives an example of comparison with guarantees given at three operating points and with limit values:

- a) the hydraulic efficiency guarantees are met in points A, B and C;
- b) the discharge limit<sup>1)</sup> to be exceeded in point A is satisfied;
- c) the power limit not to be exceeded in point C is satisfied (see detail X), because it has been chosen  $k = 0,970$  and the lower limit of the total uncertainty bandwidth is lower than the guaranteed higher limit  $P_{mP} = (0,970 + 0,030) P_{mP,sp}$ .

<sup>1)</sup> The prototype guaranteed discharge should be referred to the ambient pressure. Although the symbol of the prototype discharge should be  $Q_{1P}$  (see 1.3.3.4.5), the symbol  $Q_p$  is normally used.

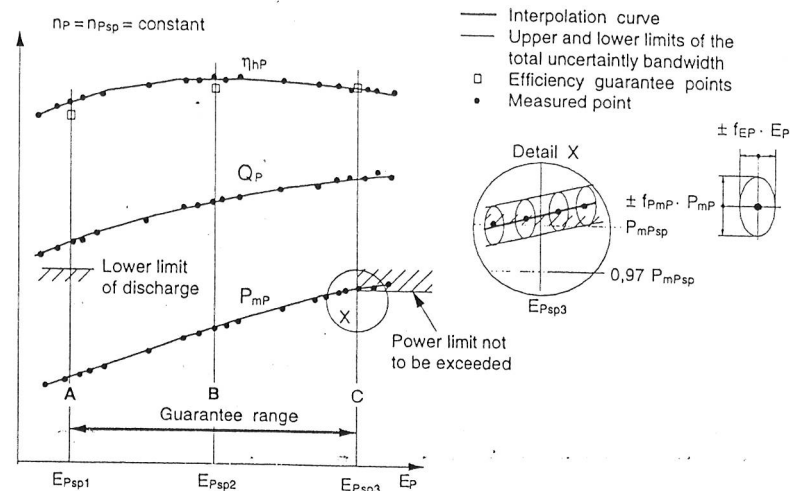


Figure 84 – Non-regulated turbine. Comparison between guarantees and measurements

### 1.3.3 Non-regulated/regulated pump

discharge limit is usually defined, if not otherwise agreed, at one or more points by a lower  $kQ_{Psp}$  and a higher limit  $(k + 0,03) Q_{Psp}$ ,  $k$  being a mutually agreed value lying somewhere between 0,97 and 1,0. Normally, the value of  $k$  is 0,985.

discharge guarantee is met if, at the specified specific hydraulic energy, there is intersection or contact between the band defined by the discharge limits and the total uncertainty bandwidth defined by the envelope of the uncertainty ellipses of the measured points defining discharge characteristic (see figure 85).

checking the hydraulic efficiency guarantee, the value to be compared with the guaranteed value is the upper limit of the total uncertainty bandwidth on efficiency at the operating point defined by the intersection of the interpolation curve drawn through the measured points with characteristic curve  $E_p = f(Q_p)$  (see for example point A' of figure 85).

regulated pump is operated at different openings, the above considerations apply to the variant envelope curves.

Figure 85 gives an example of comparison with guarantees given for three operating conditions at a non-regulated pump:

the hydraulic efficiency guarantees are met at points A' and B', but not at point C';

the minimum discharge limit is not met at point A';

the power limit not to be exceeded at point C' is satisfied.

for variable speed pumps, the change of the  $E(Q)$  and  $E(P)$  characteristics in function of speed to be taken into account.

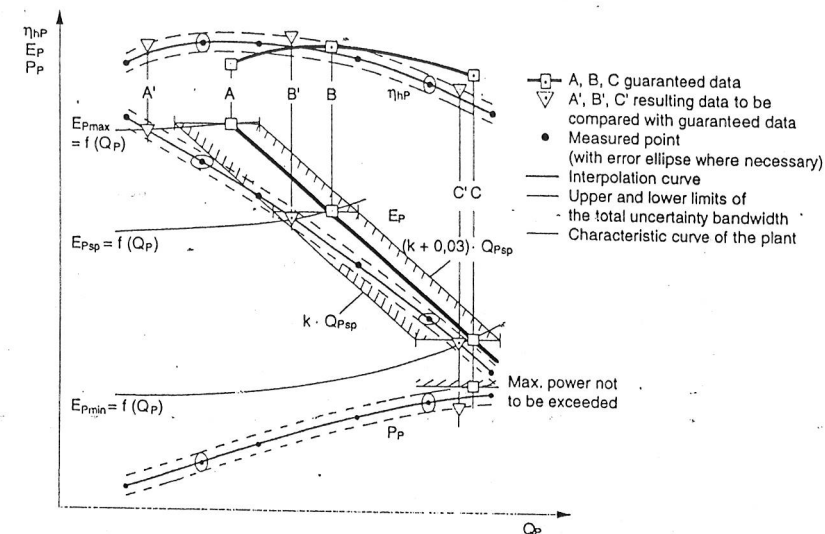


Figure 85 – Non-regulated pump. Comparison between guarantees and measurements

### 3.10.3.4 Prototype mechanical losses

If the prototype power  $P_p$  is guaranteed, the prototype mechanical losses shall be taken into account (see 1.4.2.1.1).

If the prototype efficiency  $\eta_p$  is guaranteed, the following formula applies:

$$\eta_p = \eta_{hP} \cdot \eta_{mP} \quad (\text{see } 1.3.3.9.3)$$

### 3.10.3.5 Penalty and premium

It is recommended that the contract should state in detail the method of calculating penalties and/or premium from the test results.

To determine the penalty on efficiency, the guarantee shall be compared with the upper limit curve of the total uncertainty band.

To determine the premium on efficiency, the guarantee shall be compared with the lower limit curve of the total uncertainty band.

### 3.4 Runaway speed and discharge

The shape of runaway curves and the influence of cavitation for different types of machines are covered in 3.8.

The example of Figure 86 refers to a Francis turbine. It shows the prototype steady-state runaway speed curve, calculated from the measured model speed factors, against guide vane opening.

In this example, the guarantees of maximum steady-state runaway speed and discharge are as shown in details X and Y: at openings less than  $\alpha_{\max}$  the lower limit of the uncertainty bandwidth is lower than the value not to be exceeded.

For a double-regulated machine, the guarantee shall be verified under the worst runaway condition which can occur in the guarantee ranges of the Thoma number and specific hydraulic energy, depending on guide vane opening and runner blade angle.

For a non-regulated machine, there is only one measured point to be compared with the guaranteed value.

Unless otherwise agreed, the mechanical and windage losses of the motor/generator and the mechanical losses of the hydraulic machine (see annex G) are taken into account.

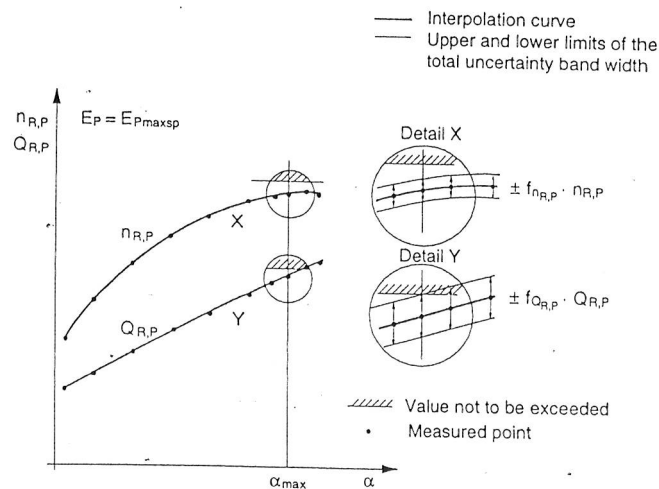


Figure 86 – Francis turbine. Runaway speed and discharge curves. Comparison between guarantees and measurements

### 0.5 Cavitation guarantees

The influence of the cavitation on the performance of the machine is dealt with in 2.3 and 3.8, and some recommendations are given for comparison of prototype guarantees with performance data resulting from model tests.

When determining the Thoma number  $\sigma_0$ , which is the lowest value of  $\sigma$  for which efficiency remains unchanged, the uncertainty bandwidth of the non-cavitating efficiency shall be taken into account.

Figure 87 shows a test curve  $\eta_{hM}(\sigma)$ . If the guarantee prescribes  $\sigma_1 \leq k \sigma_{pl}$ , the guarantee in this case is not fulfilled, since the Thoma number  $\sigma_1$  for which a drop of 1 % in efficiency is observed is higher than the plant Thoma number  $\sigma_{pl}$  reduced by a mutually agreed safety coefficient  $k$ , even if the total uncertainty bandwidth is taken into account.

In the prototype, the cavitation guarantees may also be given in term of  $NPSE_{P1} \leq (NPSE_{pl} - K)$ ,  $K$  being a mutually agreed safety margin.

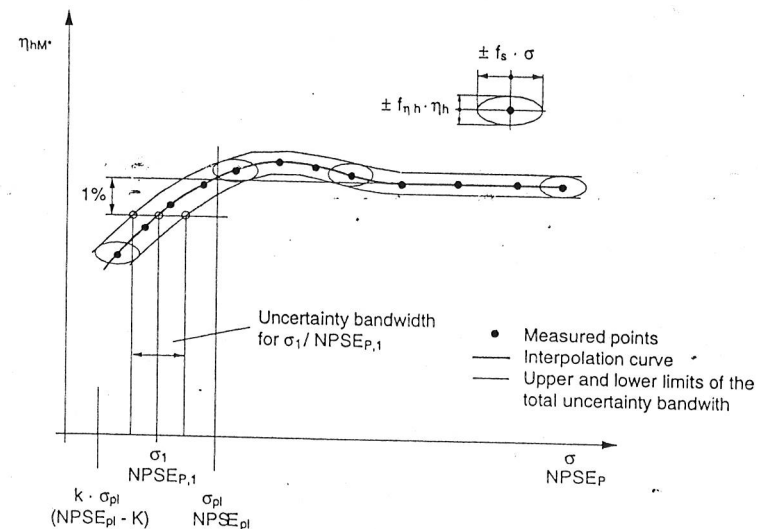


Figure 87 – Model turbine. Cavitation curve and comparison with the guarantee on the influence of the cavitation on the efficiency

## Additional performance data – Methods of measurement and results

### 1 Introduction to additional data measurement

#### 1.1 General

re so called "additional data" (torque, forces, pressure fluctuations etc.) defined in subclause 1.4.4 provide information for the design and operation of the hydraulic machine in the hydroelectric power plant. Therefore, additional types of measurements are needed, which can be specified.

is currently neither possible nor desirable to prescribe requirements for measurements of additional data" as rigorously as prescribed for the main hydraulic performance. The measurement methods and evaluation techniques for "additional data" are rapidly evolving.

formation stated in this clause shall thus be taken as recommendation or guidance to the user in order to carry out measurements with the needed accuracy and under comparable conditions.

each operating point of a hydraulic machine is characterized by a variety of mechanical and hydraulic quantities (usually of oscillating nature) which occur during both steady state and transient operations. The model is always operated in steady state conditions. In general, it is not possible to simulate on the model the prototype transient operating sequences, the data for which can only be derived from a series of steady-state operations.

subclause 4.2 describes requirements for data acquisition and processing in addition to those prescribed in subclause 3.1.

is often unnecessary to measure some of the additional data on the model if these values can be predicted with sufficient accuracy based on data from similar hydraulic machines (e.g. guide and guide vane torque, radial thrust etc.). The measurements of additional data shall be defined by the technical program, (see 2.3.3.3.2).

he hydraulic machine has to be considered as a component of the whole hydro-electric installation. In this connection it is advisable to investigate unstable operation due to excitation of natural frequencies of the hydraulic circuit. Model tests can be used to identify possible excitation frequencies and mode shapes of the machine at various operating points. Subclauses 4.3 and 4.4 are devoted to these procedures of identification.

or a "safe" mechanical design of the prototype, hydraulic loads acting on various components of the prototype machine can be derived from model test data scaled up using appropriate proportion laws. Subclauses 4.5 and 4.6 describe the methods and the test conditions for deriving such hydraulic loads with their mean and dynamic components.

start up, shut down and/or any change of operation modes will lead to transient operation of the machine far from the "normal" operating range. Therefore, in certain cases it is required to explore this extended operating range with respect to the relevant hydraulic and mechanical quantities. Subclause 4.7 deals with measurements of the hydraulic characteristics in the extended operating range (the so-called 4-quadrants range for a pump-turbine).

Finally, subclause 4.8 describes how to investigate during model tests the feasibility of index tests on prototype.

#### 4.1.2 Test conditions and test procedures

The additional measurements are usually performed with the same model machine on the same test installation and require the same instrumentation as used for the main hydraulic performance tests according to clauses 1 to 3 of this standard. It has to be checked if the same test conditions can be applied as during the main hydraulic performance tests or shall be adapted. In any case, disturbing effects due to vibrations, resonance, mechanical deformations, increased leakage flow, etc., or defects of the additional measuring equipment shall be minimized. Possible exceptions to the requirements of clauses 2 and 3, if any, are dealt with in the relevant subclauses of clause 4.

IEC 60994 provides specification for instrumentation requirements and the measurement of fluctuating quantities. In addition, relevant specifications are given in the corresponding subclauses of clause 4. Supplementary recommendations for measurement of these additional data can be found in the existing IEC and ISO standards.

Depending on the measuring arrangement, the scope of various test series and the admissible and required test conditions, the test procedure and the test program can be defined. The measurement of various types of additional data can be combined with each other and/or with the measurement of the main hydraulic performance.

The same procedures with respect to calibration, preliminary and acceptance tests, check of zero readings, etc., as described in subclause 2.3 are also applicable to measurements of additional data.

The test conditions and basic analysis methods shall be agreed upon prior to the tests.

#### 4.1.3 Uncertainty in measurements

The total uncertainty in the measurements of additional data is generally higher than the uncertainty in the measurement of the main hydraulic performance quantities, for the following reasons:

- a) the off-design operating range in which the quantity is measured;
- b) the unsteady nature of the measured quantities;
- c) the limitation of the available instrumentation and calibration procedures.

The measuring methods shall be selected such that the uncertainty corresponds to the mutually agreed accuracy for any given purpose. In many cases, figures for uncertainties should be given in physical units (Pa, N, N·m, ...).

The individual aspects of uncertainties are described in the relevant subclauses 4.3 to 4.8.

#### 4.1.4 Model to prototype conversion

Prototype values can be calculated by converting the model test data according to the general similarity laws. The appropriate conversion procedures are described in the following subclauses. It is common practice to transpose the results from model to prototype using the appropriate dimensionless terms.

however, it shall first be checked whether hydraulic and mechanical similarity laws are efficiently established for the particular quantity. If not, the conversion shall consider the dynamic-structural aspects of the prototype machine within the entire hydroelectric system, including such factors as flow pattern at entrance and exit, resonance, external excitation, etc.

Factors in the model test facility, such as the following which could affect the test results, should be eliminated to the extent possible:

- influences due to flow regimes;
- influences of mechanical structures;
- others.

## 2 Data acquisition and processing for measurement of fluctuating quantities

### 2.1 General

Subclause 3.1 describes the measurement of average values of the main hydraulic performance quantities. Many of the methods used allow recording of the fluctuating component of the quantity as well.

This subclause 4.2 describes requirements for data acquisition and processing for the termination of the fluctuating quantities. Data processing includes the calculation, evaluation and presentation of statistical quantities representing the model measurements. IEC 60994 shall be taken into account.

The procedure for measurement, data acquisition and data processing shall be agreed upon prior to the tests.

The measured quantities will be:

- either of periodic nature;
- or of non-periodic, stochastic and intermittent nature.

The fluctuating quantities can be measured:

- with their mean components (measurement of  $\bar{X}$  in Figure 7);
- or as fluctuating component only (measurement of  $\tilde{X}$  in Figure 7).

The measurement methods shall be able to record fluctuating quantities in sufficient resolution to describe their characteristic occurrence. Measurements can be made using:

- pressure transducers;
- accelerometers;
- strain gauges;
- other transducers for mechanical quantities.

To allow further data analysis, the measurement chain from transducer to data storage system shall fulfill various criteria provided by the signal analysis theory (see reference [21] in annex P). In particular the criteria described in subclause 3.1 shall be applied. However, the fluctuating nature of the quantities considered in this subclause leads to additional requirements described below.

## 4.2.2 Data acquisition

### 4.2.2.1 Signal conditioning

The purpose of measurement and the methods of data acquisition and processing determine the appropriate signal conditioning. The main purposes of conditioning are:

- removal of high frequency noise to prevent aliasing effects (analog filter);
- elimination of irrelevant signal components (analog, digital filter, or software methods);
- offset adaptation.

### 4.2.2.2 Analog to digital conversion

Most data acquisition systems are based on periodic sampling followed by analog to digital conversion. Figure 88 shows a typical data acquisition system.

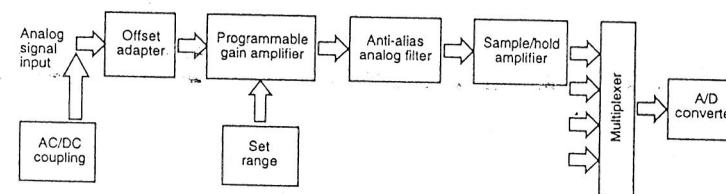


Figure 88 – Typical data acquisition system

When the steady-state value of a signal is not relevant and is greater than the peak to peak value, offset adaptation can improve the quality of the stored fluctuating component of the signal. AC coupling of the converter inputs can induce signal distortions in the low frequencies. Selectable DC offset adds a constant to the analog signal. The signal range can be centered on the converter range without low frequency distortions.

Programmable gain amplifiers adapt the analog signal range to the dynamic range of the A/D converter.

Analog anti-alias low-pass filters shall be used for periodic sampling. The sampling frequency is limited by the filter characteristics. Simultaneous sampling of all signals can be done with a sample and hold amplifier on each measurement channel. Sampled signals can then be multiplexed and converted sequentially. If the signals are sampled sequentially, the resulting delay shall be considered (see 4.2.2.4).

Most analog to digital converters used in signal analysis deliver a stream of integer values corresponding to discrete increments of the physical input. This operation induces an irreversible loss of data and shall be done with care.

he resolution and precision of a analog to digital converter determine its quality. The resolution is normally stated in bits. The sign bit is not always counted.

he quality of the digitized signal also depends on the matching between the analog signal extreme values and the converter range. Therefore, each measurement channel shall be conditioned so that the signal best fits the converter range.

### 2.2.3 Sampling rate

eriodic sampling requires all energy in the signal to be contained between zero and half the sampling frequency, (see reference [21] in annex P). If this condition is not fulfilled, aliasing effects will introduce an irreversible corruption of the sampled signal.

o prevent aliasing, an analog low-pass filter shall be used before sampling. If the filter has a flat gain function up to  $f_{\max}$ , the required sampling frequency is:

$$f_s > 2 f_{\max} + f_{\text{trans}}$$

here  $f_{\text{trans}}$  is the transition frequency (see Figure 89), which depends on:

- the type and order of the analog anti-aliasing filter;
- the filter cut-off frequency;
- the characteristics of the analog to digital converter;
- the possible high frequency content of the signal to be measured;
- the acceptable noise level.

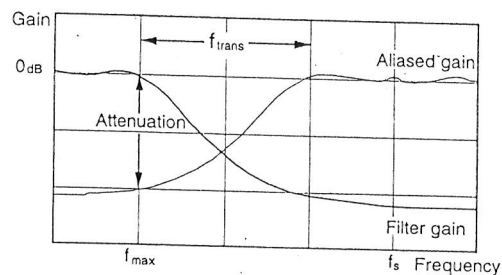


Figure 89 – Frequency response of analog anti-aliasing filter

### 2.2.4 Phase information

some cases, the phase relationship between different fluctuating quantities is important. In such cases, the information on phase shift shall be carefully dealt with to prevent possible phase distortions caused by the data processing system.

When the measurement channels have different signal conditioning electronics and the phase is important, this influence shall be determined and corrected.

If the channels are sampled sequentially, the phase distortion  $\Delta\phi$  for channel  $i$  ( $i = 1, 2, \dots, n$ ) compared to channel 0 depends on:

- the time  $\Delta t$  between sampling of consecutive channels;
- the position of channel  $i$ ;
- the frequency of interest  $f$ .

The phase distortion is:

$$\Delta\phi = 2\pi \cdot \Delta t \cdot i \cdot f \quad \Delta\phi \text{ can be constant or equal to } 1/(n \cdot f_s)$$

### 4.2.2.5 Data storage

Both analog recorders and digital media can be used for data storage. In the first case, raw signals are for example recorded on magnetic tapes and can be recovered for visualization and further analysis. The magnetic recorder is considered as part of the acquisition system and its frequency response should match acquisition criteria. In the second case, digitized data are stored in mass storage media such as disks, tapes, etc.

### 4.2.2.6 Data acquisition procedure

The following information should be available in order to identify the data acquisition procedure:

- resolution of the analog to digital conversion in terms of number of bits;
- sampling frequency;
- frequency response of anti-aliasing filters;
- frequency responses of the measurement chain;
- number of records and the number of samples in each record;
- data storage procedure.

### 4.2.3 Data processing

Once data acquisition criteria are fulfilled, data processing is performed in order to extract information of interest. A variety of transformations can be applied to time-history signals in order to analyze:

- their statistical behavior;
- their spectral content (in the frequency domain);
- correlation or other relationships between signals.

Time domain analysis parameters are:

- averaged values;
- characteristic amplitudes<sup>1)</sup>, standard deviations, r.m.s. values;
- probability density functions, probability distributions;
- others.

<sup>1)</sup> A characteristic amplitude means e.g. half the difference between the maximum and minimum values of a signal. It can be determined with the aid of probability distribution applying counting methods and assuming a certain amount of probability (e.g. 97 %). Amplitudes occurring outside of this probability are ignored.

frequency domain analysis parameters are:

- amplitude spectrum (square root of auto power spectrum);
- auto power spectrum (energy spectrum for finite energy signals);
- cross power spectrum;
- transfer functions;
- coherence functions;
- others.

because 4.3.6 provides more detailed information on data processing of pressure fluctuations. This information, especially the subclause 4.3.6.1, is generally also valid for data processing of other measured fluctuating quantities, such as shaft torque fluctuations (clause 4.4), axial and radial thrust (subclause 4.5), guide vane torque (subclause 4.6.2).

## Pressure fluctuations

### 1.1 General

#### 1.1.1 Pressure fluctuations in hydraulic machinery

Pressure fluctuations are a natural occurrence in hydraulic machinery. They can be of a periodic or stochastic nature. They are due to the action of the water passages and vanes on the flow fields within the machine. They are influenced by machine design, operating conditions and by the dynamic response of the water conduits and rotating components. Pressure fluctuations are actually a part of hydro-acoustic phenomena involving unsteady pressure and velocity distributions. They can also be associated with mechanical fluctuations of shaft torque, rotational speed, hydraulic load on guide vanes etc. as well as with vibrations of the machine.

Low frequency disturbances are of special interest because they can propagate to the whole power conduit and the rotating parts of the electric machine. They occur typically between 0,2 and 3 times the runner rotational frequency.

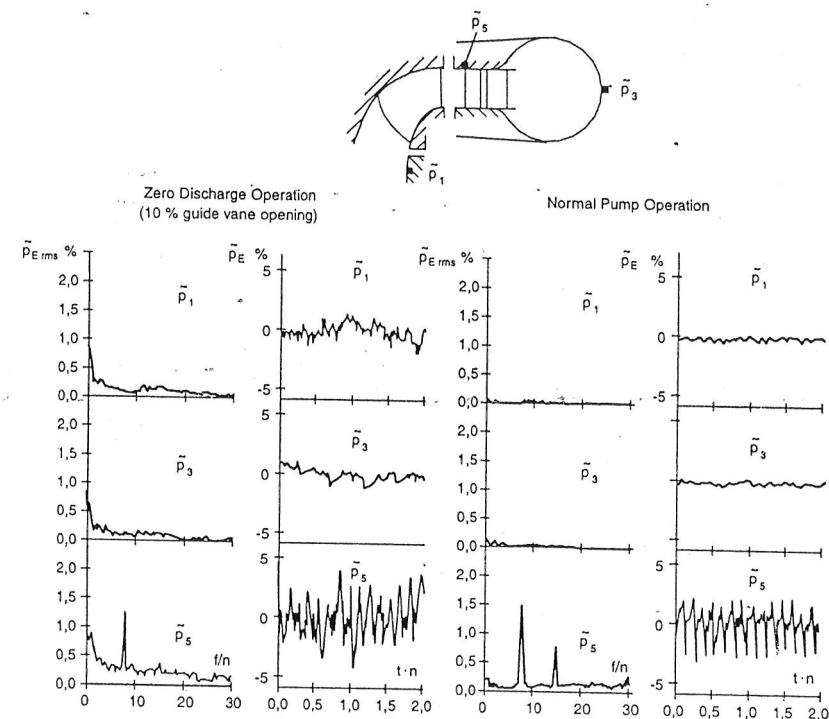


Figure 90 – Normal pump mode and zero discharge operations of an  $n_{0E} = 0,102$  pump-turbine model

The draft tube surge of Francis and propeller turbines and pump-turbines is perhaps the most commonly identified phenomenon among low frequency pressure fluctuations. In these machines, a strong runner outlet swirl can develop, inducing pressure fluctuations. In addition, draft tube cavitation can change the natural frequencies of the hydraulic system.

In double-regulated Kaplan or diagonal (Dériaz) turbines, on-cam control of the guide vane opening and of the runner blade setting leads to a minimal runner outlet swirl and no serious draft tube surge is generated.

In impulse turbines, the runner is separated from the nozzle by a constant-pressure condition. For this reason, there is no interaction between runner and water conduits. Impulse turbines are not considered in this subclause.

turbines and pumps produce an excitation at the rotational frequency multiplied by the number of runner/impeller blades usually defined as the blade passing frequency. Due to the interaction of the runner/impeller blades with the guide vanes / stay vanes / spiral case, higher frequencies are generated up to  $k$  multiplied by the blade passing frequency,  $k$  being typically between 1 and 2 for turbines and 1 and 4 for pumps and pump turbines.

Stochastic pressure fluctuations due to turbulent flow separation or intermittent pressure surges due to vortex breakdown can take place in various conditions of the extended operating range.

Some examples of pressure fluctuations associated with reaction machines are shown in Figure 90 through Figure 93 for various operating conditions. Pressure transducer locations are proposed in Figure 94.

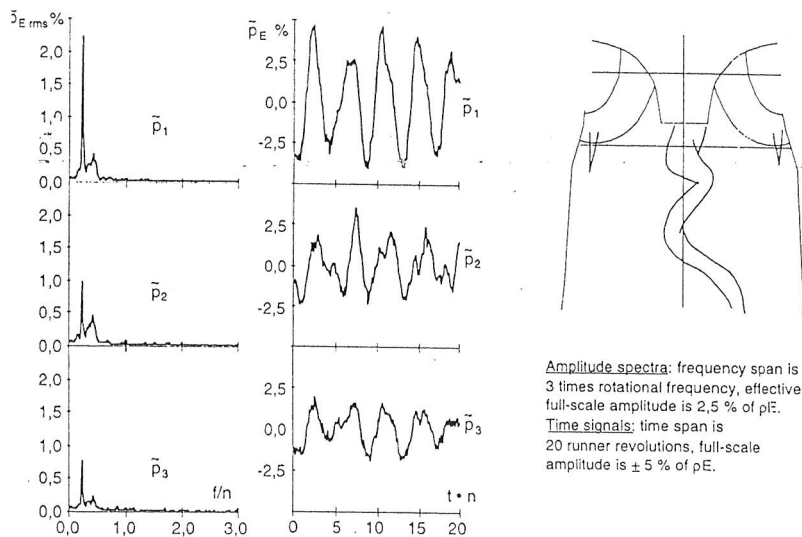


Figure 91 – Part load operation of an  $n_{OE} = 0,321$  Francis turbine model:  $Q_{nD}/Q_{nDopt} = 0,719$

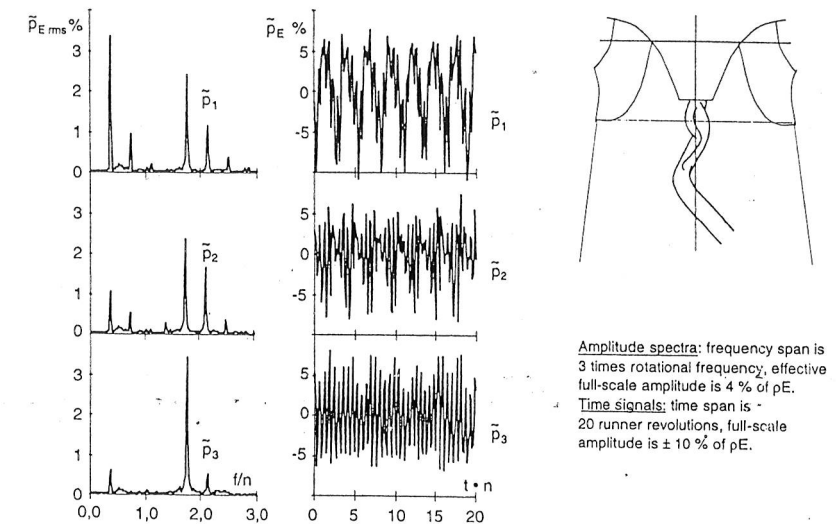


Figure 92 – Higher part load operation of an  $n_{OE} = 0,226$  Francis turbine model:  $Q_{nD}/Q_{nDopt} = 0,764$

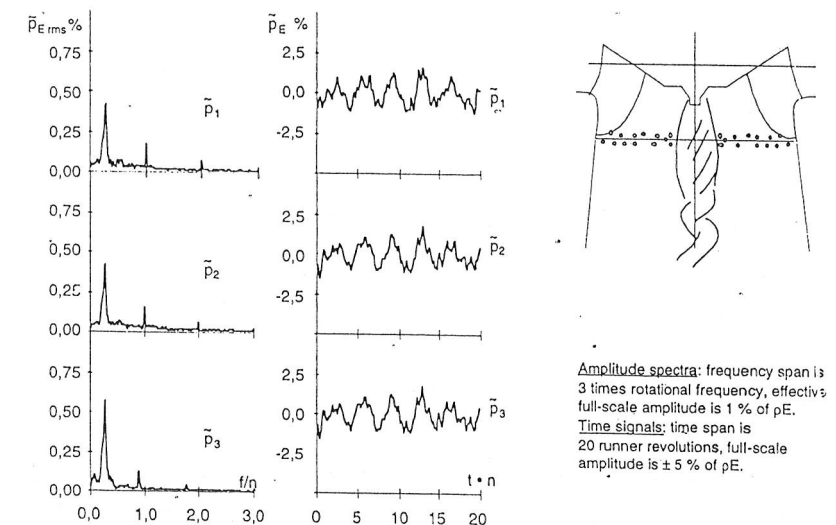


Figure 93 – Full load operation of an  $n_{OE} = 0,173$  Francis turbine model:  $Q_{nD}/Q_{nDopt} = 1,218$

### 4.1.2 Influence of the hydraulic circuit and rotating machinery

Model tests of an isolated hydraulic machine do not fully reproduce all possible prototype dynamic phenomena because hydro-acoustic waves can be significantly influenced by the boundary conditions.

Pressure fluctuations are not only characteristics of the model but they can also be affected by characteristics of the test facility. Possible conditions affecting similitude include the following:

- water conduit (pipe length, wall stiffness);
- test fluid characteristics (free gas content);
- dynamic behavior of rotating components;
- Reynolds and Froude numbers.

### 4.1.3 Purpose of the measurements

Pressure fluctuation measurements are usually conducted to obtain the following information:

- relative magnitude of the pressure fluctuations within specified operating range;
- nature of the pressure fluctuations, periodic or stochastic;
- dominant frequency of the pressure fluctuations, if any;
- effect of palliative methods such as air admission (effectiveness and suitable location);
- intensity of the pressure fluctuations of the model compared with other models of similar specific speed.

Favourable conditions where no significant interactions with the external systems, see Figure 99, are involved, quantitative model test results can be directly transposed to the prototype.

Nevertheless, due to the various interactions with the external systems or the differences of model characteristics between model and prototype, the amplitude and frequency of the prototype pressure fluctuations can deviate considerably from those directly transposed from model tests. Since the present state of the art does not permit to quantify such deviations, pressure measurements of pressure fluctuations of the model are conducted in most cases to obtain at least qualitative information or to assess the magnitude of pressure fluctuations.

### 4.2 Special requirements for model and installation

The model and test installation shall comply with general requirements for the testing of hydraulic machinery, see subclause 2.1. It shall provide full control of test specific hydraulic energy, rotational speed and pressure at the low pressure side. Once the desired test conditions are set, they shall remain steady during the time necessary for the measurement of fluctuating quantities.

Transparent parts on the low pressure side of the runner should be large enough for observation of cavitation not only on the runner blades, but also in the upper portion of the draft tube.

In order to avoid resonance effects between the test circuit and the model, the natural frequency of the test circuit should be sufficiently outside of the range of interest of model frequencies (see 4.3.4.1). Hydraulic disturbances from the feed pump, throttling devices, bypasses, bends etc. shall not affect the model in this range of frequencies.

The draft tube should be connected to a conduit or tank with a cross-sectional area large enough to overcome dynamic coupling of the model with the low pressure part of the test circuit.

The model construction shall be stiff enough to prevent excessive deformations. Vibrations of the model test rig and rotational speed fluctuations due to the governing system should not induce pressure fluctuations in the considered frequency band.

The test installation should operate in closed circuit mode, so the gas content can be kept low and constant. The model inlet flow shall be free of traveling bubbles.

In the case of models with a full spiral case, a straight uniform pipe, if feasible, at least 6 diameters long, should be installed on the high pressure side of the model. This allows an estimation of both the pressure waves propagation conditions and the hydro-acoustic power of these pressure waves at the spiral case inlet using the signals of the  $p_3$  and  $p_6$  pressure transducers outlined in Figure 94.

### 4.3.3 Instrumentation and calibration

#### 4.3.3.1 Instruments for pressure fluctuation measurements

Pressure transducers should be mounted with their membrane flush with the hydraulic profile. When this cannot be done, cavities shall be carefully bled and their natural frequencies evaluated: they shall not induce distortions in the frequency band of interest (see 4.3.1.1 and IEC 60994, 6.3).

The transducers shall be sensitive enough to measure effective pressure fluctuations of  $\pm 0,1\%$  of  $p_E$ .

The maximum permissible error of the measuring chain shall be smaller than  $\pm 5\%$  of the measuring range used. This error can be reduced by a preliminary calibration procedure (see 4.3.3.2).

The maximum permissible error of the signal processing equipment shall be smaller than  $\pm 1\%$  for the amplitude and smaller than  $\pm 10^\circ$  for the phase.

Figure 94 shows an example of suggested locations of transducers for a Francis or propeller turbine or pump-turbine. The measurement of  $p_1$ ,  $p_2$  and  $p_3$  as listed below is strongly recommended. Transducers  $p_1$  and  $p_2$  should be placed 0,3 to 1,0 diameter from the low pressure side of the runner/impeller.

- $p_1$  pressure transducer on the downstream side of the draft tube cone;
- $p_2$  pressure transducer on the upstream side of the draft tube cone;
- $p_3$  pressure transducer at the spiral case inlet.

Depending on pressure fluctuation data desired, the following transducers can also be installed:

p<sub>4</sub> additional pressure transducers in the draft tube cone: in the same section as p<sub>1</sub> and p<sub>2</sub> preferably 90° apart, in the draft tube bend or at locations corresponding to manholes on the prototype;

p<sub>5</sub> pressure transducers in the distributor (e.g. between runner / impeller and guide vanes);

p<sub>6</sub> additional pressure transducers along the intake;

p<sub>7</sub> pressure transducers in the draft tube outlet.

Force and torque measurements as listed below can also be performed concurrently with pressure fluctuation measurements:

f<sub>1</sub> axial and radial thrust transducers on the shaft – runner coupling flange (see subclause 4.5);

t<sub>1</sub> torque transducer on the shaft (see subclause 4.4).

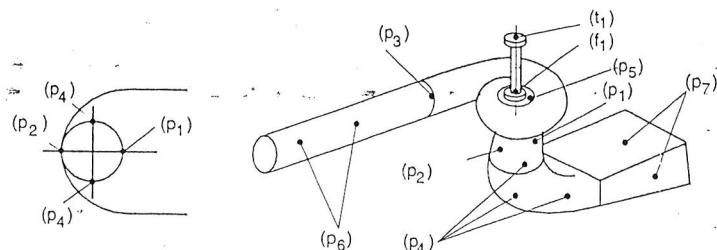


Figure 94 – Suggested locations of transducers

### 3.3.2 Calibration

Dynamic calibration for pressure measurement systems can be performed. It consists of the determination of the transfer function between the input pressure signal and the output electric signal.

The absolute phase shift between the pressure and the output signal is not usually required. Phase shifts between output signals due to different signal conditioning systems, however, could be known or compensated.

Gain and phase corrections can be determined by exciting all transducers with the same pressure fluctuation, in the same range of frequencies and amplitudes as for the model test. The calibration shall ensure that differences in gain and phase between channels are within the uncertainty margin of the signal processing equipment (see 4.3.3.1).

## 3.4 Detailed procedures

### 3.4.1 Test specific hydraulic energy

The test specific hydraulic energy is selected to provide good conditions for the adjustment of steady-state operation parameters. Also, the test specific hydraulic energy shall be chosen so that pressure fluctuation frequencies and amplitudes are within the limits of the instrumentation.

Moreover, if a resonance between the model and the test installation is suspected, it is recommended to conduct the measurements under different test specific hydraulic energies (see 4.3.2).

Test specific hydraulic energy according to Froude similitude should be adopted whenever it is practical. In the case of large machines with small specific hydraulic energy, the Froude influence is considerably increased (see 2.3.1.5).

### 4.3.4.2 Cavitation reference level for pressure fluctuation measurements

If Froude similitude cannot be fulfilled, the flow field in the draft tube cone and consequently the pressure fluctuations will be influenced by vapour cavity development.

A cavitation reference level shall be agreed upon (see 2.3.1.5.1). For vertical units, this level can be at or below the low pressure side of the runner / impeller.

### 4.3.4.3 Model test operating conditions

Typical exploration paths, ranges of test points, for a pump or a pump turbine are represented in Figure 95 and typical exploration paths for a Francis or propeller turbine are represented on the  $E_{HD} - Q_{HD}$  diagram in Figure 96.

In the case of a turbine, the test points should cover at least the specified discharge operating range under a constant test specific hydraulic energy and at the Thoma number related to the cavitation reference level defined in 4.3.4.2. This can be completed by additional explorations.

Detailed tests at part load and at full load, at guide vane openings for which remarkable fluctuations occur, give a fair idea of fluctuation phenomena with slightly different operating conditions. These consist in one variation of energy coefficient with constant test specific hydraulic energy, Thoma number and guide vane opening, one variation of Thoma number and possibly a variation of test specific hydraulic energy.

In the extended operating range, considerable pressure fluctuations can occur. This refers particularly to turbines in runaway conditions and to pump-turbines (or pumps) in extreme operating conditions (for example in reverse rotation pump mode).

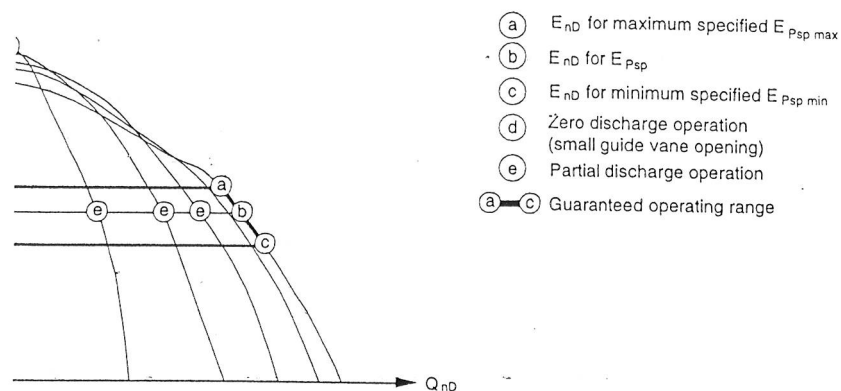


Figure 95 – Pump diagram with exploration paths

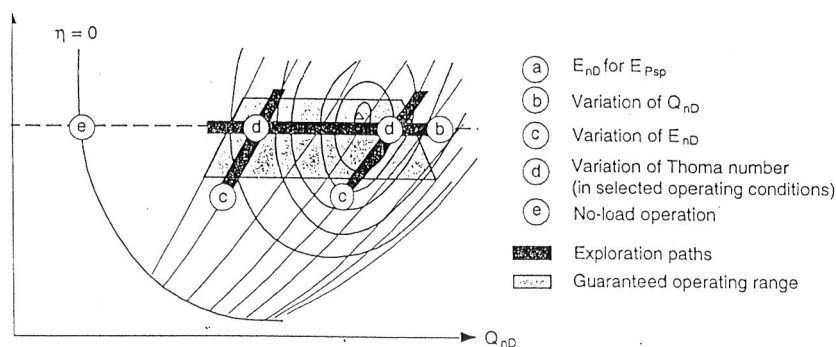


Figure 96 – Turbine hill-chart with exploration paths

or plants with large variations of specific hydraulic energy, tests should also be performed for different energy coefficients, with corresponding values of Thoma number.

This amount of data is desirable for an appropriate diagnosis of pressure fluctuations.

### 3.4.4 Air admission

Air admission for the reduction of pressure fluctuations can be tested on models. Such tests give only an approximate idea of the effects of air admission to be expected on the prototype, because similitude cannot be sufficiently ensured.

### 4.3.5 Measurement

For each test point, the fluctuating signal is sampled over a time period, sufficient for the purpose of the test, e.g. investigation of low frequency surges.

Draft tube cavitation should be observed and cavity patterns should be recorded.

Sampling and recording of signals shall comply with subclause 4.2.

### 4.3.6 Analysis, presentation and interpretation of results

#### 4.3.6.1 Analysis

According to either the periodic or non-periodic nature of the pressure fluctuations, a frequency domain or a time domain analysis should be chosen.

##### 4.3.6.1.1 Time-domain analysis

Time-domain analysis is mostly useful for processing random and intermittent fluctuations (see Figure 90 to Figure 93). For pressure fluctuation tests, time-domain analysis can be made by determination of the standard deviation of the signal. The comparison of the standard deviation with the frequency-domain estimation of the signal amplitude gives an indication of the random fluctuations superimposed on the periodic signal, while the characteristic amplitude determined by statistical methods gives an indication of the absolute magnitude of fluctuations.

The signals can be viewed in the time-domain also for checking purposes.

##### 4.3.6.1.2 Frequency-domain analysis

Frequency domain analysis of the pressure fluctuations should be done with a Fourier analyzer. By the use of a multi-channel analyzer it is possible to track periodic phenomena simultaneously occurring at different frequencies and to evaluate phase shifts between channels. The Fourier analyzers usually express the magnitude of the spectrum components in engineering units.

Frequency spectra can be estimated by an average of discrete Fourier transforms computed on a succession of time records. In order to minimize leakage effects due to the finite time records and to preserve a good definition of frequencies appropriate weighting windows, such as Hanning or Kaiser-Bessel, should be used.

Frequency spectra obtained by the discrete Fourier transforms provide the best fit, over a given time record, between the sampled time domain data and superposition of sine waves. The time record length is the same for all frequencies within a transform. Higher frequencies are thus averaged over a greater number of periods than low frequencies. For this reason, the discrete Fourier transform is not suitable for the characterization of signals with a time-varying frequency content.

In wavelet / joint time frequency methods, the time weighting window is a function of frequency. The same number of periods is used for the computation of all frequency-coefficients. The result accurately represents the frequency content of the signal of interest as a function of time.

### 3.6.1.3 Non-dimensional frequencies and pressures

Pressure fluctuation frequencies are made non-dimensional by the runner/impeller rotational frequency  $n$ .

$$\text{Frequency coefficient } f_n = \frac{f}{n}$$

Pressure fluctuation amplitudes are made non-dimensional by the pressure  $p_E$  representative of the test specific hydraulic energy.

$$\text{Pressure fluctuation factor } \bar{p}_E = \frac{\bar{p}}{p_E}$$

### 3.6.2 Presentation and interpretation of pressure fluctuations

#### 3.6.2.1 General

Pressure oscillatory data represented in non-dimensional terms ( $f_n, \bar{p}_E$ ) should be presented versus test parameter so as to provide a global information on the pressure fluctuations to be expected on the prototype in the investigated operating conditions. The test parameter can be:

- discharge coefficient or factor;
- energy coefficient or speed factor;
- Thoma number;
- test specific hydraulic energy;
- air flow-rate or other.

The analysis and presentation of measured pressure signals  $p_1$ ,  $p_2$  and  $p_3$  (see Figure 94) are strongly recommended.

The diagrams below give examples of presentation of results.

#### 3.6.2.2 Waterfall diagram

The waterfall diagram in Figure 97 presents amplitude-frequency spectra as a function of the selected test parameter in a 3-D style display. It provides a fast overview of all pressure fluctuations in the considered frequency band and operating range.

#### 3.6.2.3 Summarized diagram

The summarized diagram in Figure 98 presents spectral data associated with the dominant frequency for each measurement channel as functions of the selected test parameter in 2-D displays.

The dominant frequency is that associated with the maximum spectral amplitude of the signal channel in the frequency band of interest.

The summarized diagram indicates:

- the dominant frequency;
- the phase shift to the reference channel at the dominant frequency;
- the narrow-band amplitude at the dominant frequency;
- the wide-band amplitude.

The narrow-band effective amplitude is estimated as the effective magnitude,  $\bar{p}_{rms}(f)$  of the discrete Fourier transform coefficient at the dominant frequency. The wide-band effective amplitude is estimated as the standard deviation,  $\bar{p}_{eff}$  of the time signal.

Iso-amplitude curves of the pressure fluctuations can be drawn in the  $E_{nD}$ - $Q_{nD}$  or  $\eta_{ED}$ - $Q_{ED}$  diagrams, provided that a sufficient number of paths have been explored, see Figure 96.

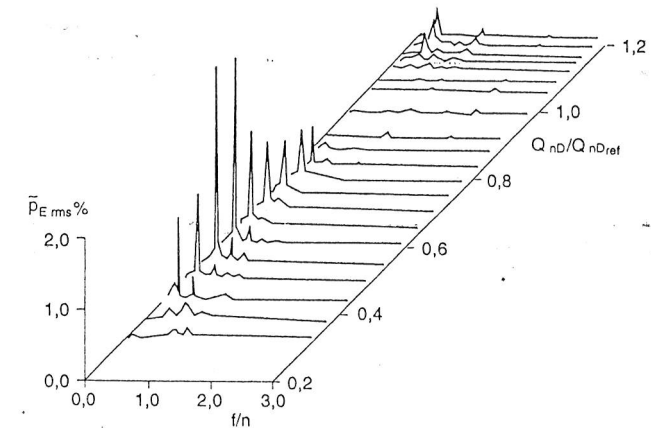


Figure 97 – Example of waterfall diagram of pressure fluctuations in the draft tube of a Francis turbine for path (b) of Figure 96, transducer  $p_1$

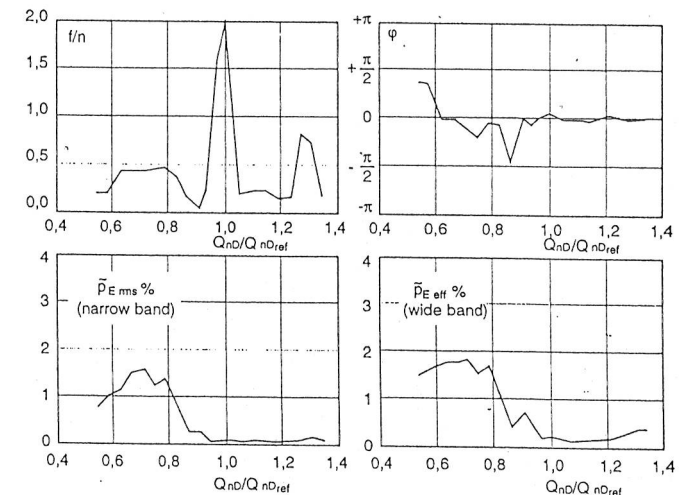


Figure 98 – Example of summarized diagram of pressure fluctuations in the draft tube of a Francis turbine for path (b) of Figure 96, transducer  $p_2$

## 1.7 Transposition to prototype

### 1.7.1 Pressure fluctuation amplitudes

favourable conditions for the model tests (see 4.3.1.2) and in case that no significant interaction with the external system is present, pressure fluctuation amplitudes are fairly well transposable from the model to the prototype.

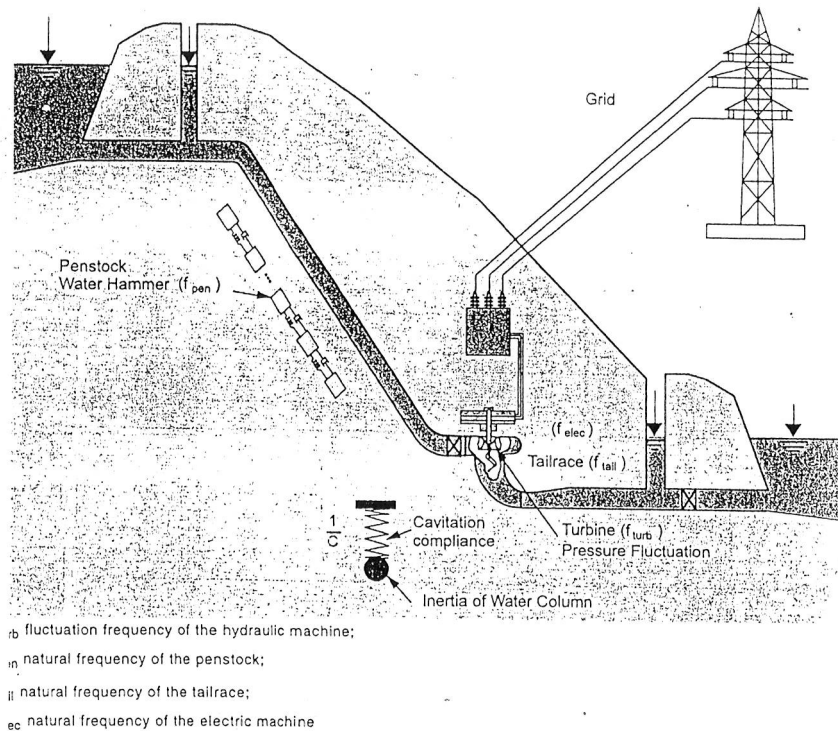


Figure 99 – Interaction of the external systems on the machine pressure fluctuations

When any interaction with external systems exists, the prediction of prototype pressure fluctuation amplitudes requires a dynamic response analysis of the full-size machine layout, including water conduits, manifold, gate chambers, tailrace tunnels etc. Due to the complexity of the prototype plant configuration, it is practically very difficult to make such analysis on a comprehensive numerical model including all relevant system components as outlined in Figure 99.

As a part of such analysis, it is only possible to check the occurrence of resonance by comparing the dominant frequency of the pressure fluctuations with the natural frequency of each of the following external system components:

- penstock;
- tailrace;
- electrical layout.

In case that any resonance with the external system is anticipated, the prediction of the prototype pressure fluctuation amplitudes is not included in the processing of model test pressure fluctuation measurements.

### 4.3.7.2 Fluctuation frequencies

The frequency coefficient defined in 4.3.6.1.3 is transposable from model to prototype for:

- a) pressure fluctuations due to inertial forces within the runner outlet flow, such as the precession of the swirl;
- b) free oscillations of the water plug in the draft tube against the gaseous volume due to either cavitation or air injection, if any;
- c) pressure fluctuations due to the interaction of runner/impeller blades and guide vanes.

### 4.3.7.3 Excitation magnitude

The magnitude of pressure fluctuations has the same scale ratio as the pressure associated with the turbine specific hydraulic energy. This is true only at the emission of disturbances. Pressure waves propagate in the piping system, are reflected, and the observed amplitudes are strongly influenced by standing waves. The similitude of pressure amplitudes is lost in case of dynamic interaction with the hydraulic circuit.

The excitation magnitude can be more adequately determined by the estimation of the active hydro-acoustic power associated with the hydraulic oscillation. This power is defined for a given cross-section as the product of the instantaneous pressure fluctuations with the instantaneous discharge fluctuations. It is practically determined from the measurements of  $p_3$  and  $p_6$ , see ref. [28] in Annex P. As the active hydro-acoustic power is not influenced by standing waves in the water conduit, it characterizes the power of the disturbance emission either from the machine (positive value) or from the test rig conduit (negative value).

### 4.3.7.4 Natural frequency of the draft tube water column

The stability of operation of a fixed runner blade reaction turbine is strongly dependent on the value of the draft tube natural frequency with respect to the frequency range of the pressure fluctuations. The physics related to the natural frequency of a draft tube is complex and under research.

The natural frequency of a draft tube  $f_0$  can be conceptually considered as the frequency of the free oscillation of the water column against the elastic gaseous volume due to either cavitation or air injection, if any.

Then, the draft tube natural frequency  $f_0$  is estimated by the following formula:

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{\int \frac{-\partial V_{vap}}{\partial NPSE} \frac{dL}{A}}}$$

where

$V_{vap}$  is the gas cavity volume in the draft tube, and

$\int dL/A$  is the ratio of length to cross-sectional area, integrated along the draft tube center line over the domain where the water column behaves as an inertia mass against the elastic gaseous volume.

<sup>1)</sup> The term  $\frac{-\partial V_{vap}}{\partial NPSE}$  is called the "cavitation compliance" of the draft tube.

Consequently, the draft tube natural frequency depends on the following operating parameters:

discharge ratio  $\frac{Q_{nD}}{Q_{nDref}}$ ;

Thoma number;

Froude number;

injected air flowrate.

It is possible to identify the draft tube natural frequency of the model by a method as described below, the possibility of the occurrence of resonance can be evaluated for each reed operating point along the exploration path by comparing it to the frequency range of the assure excitations.

can be identified by an indirect method according to the following procedure:

At a given cross-section, the free oscillations of the draft tube are characterized by pressure fluctuations of a same phase. It is then possible to identify the corresponding frequencies from at least 2 pressure transducers, e.g.  $p_1$  and  $p_2$ , and to check if one of those frequencies is affected by any variation of the cavity volume with the discharge. From the analytical expression of  $f_0$ , it can be seen that the draft tube natural frequency value is decreased with the onset and the growth of the cavity volume. Moreover, resonance can occur, which leads to an amplification of the pressure fluctuations either at the swirl precession frequency or at its 2nd harmonic and, then, this resonance can help in identifying  $f_0$ .

An example of the influence of the discharge coefficient on the natural frequency of a model Francis turbine draft tube is shown in Figure 100 at part load. Sometimes the  $f_0$  curve intersects the frequency curve of the swirl precession which corresponds to a resonance risk.

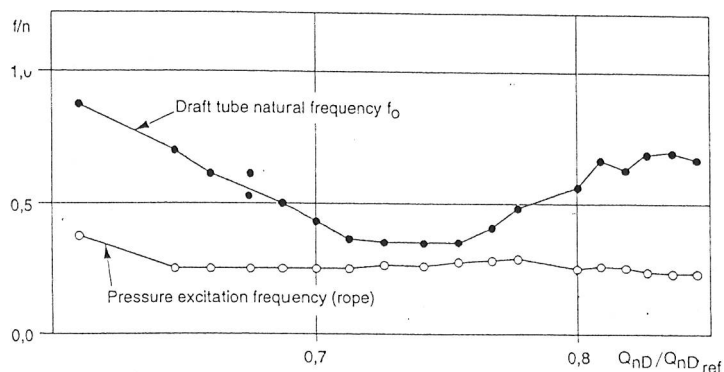


Figure 100 – Example of discharge coefficient influence on the natural frequency of a model Francis turbine draft tube

In case of doubt, a confirmation of this identification can be obtained by varying the following test parameters:

- the Thoma number (decreasing the Thoma number increases the volume of the cavity and leads to a decrease of  $f_0$ );
- the Froude number by varying the test specific hydraulic energy (decreasing the Froude number increases the volume of the cavity and leads to a decrease of  $f_0$ ).

Two other ways can be also used for the determination of  $f_0$  but they both involve more measuring time and the use of specific systems. They consist in:

- exciting the draft tube with a specific system which forces an external pressure fluctuation, and analyzing the frequency response of the pressure transducers;
- measuring the various volumes of cavity in the draft tube when varying operating discharge coefficient  $Q_{nD}$  and Thoma number value in order to estimate the frequency value with the analytical expression of  $f_0$ .

If the Thoma similitude and Froude similitude are fulfilled, the natural frequency of the draft tube can be transposed from the model to the prototype as follows:

$$\frac{f_{0M}}{f_{0P}} = \frac{n_M}{n_P} = \frac{D_P}{D_M} \sqrt{\frac{E_M}{E_P}}$$

#### 4.3.8 Uncertainties

The uncertainty of the pressure fluctuation measured on the model is influenced by the following factors:

- a) uncertainty of the instrumentation;
- b) interaction with the test circuit;
- c) interaction with the electric machine.

With good measurement conditions, it is possible to determine the pressure fluctuation of the model with uncertainties as shown below.

- a) amplitude:  $\pm 10\%$ ;
- b) dominant frequency:  $\pm 2\%$  of the model rotation frequency;
- c) phase difference:  $\pm 10^\circ$ .

Conversion from model to prototype value can involve error caused by the following factors:

- a) deviation in Froude similitude;
- b) interaction with water conduit;
- c) interaction with the electric machine.

In case that significant influence caused by the above factors is involved, it is difficult to estimate the prototype values accurately. On the contrary, with favourable conditions, the uncertainties of the predicted values for the prototype are expected to be as follows:

- a) amplitude:  $\pm 30\%$ ;
- b) dominant frequency:  $\pm 5\%$  of the prototype rotation frequency;
- c) phase difference:  $\pm 30^\circ$ .

#### 4 Shaft torque fluctuations

##### 4.1 General

Fluctuations of shaft torque in hydraulic machines can be induced by:

- ) variations of the pressure forces acting on the runner/impeller blades;
- ) variations of the electro-magnetic forces acting on the generator/motor.

Observations of torque fluctuations are considered only as an extension to the processing of pressure fluctuations (see subclause 4.3). Torque fluctuations induced by the electric machine governing system can occur and shall be identified as such.

##### 4.2 Recommendations for measurement

The torque transducer shall be mounted on the shaft between the generator/motor and the runner/impeller. See also subclause 4.5 and Figure 49 in subclause 3.6.4. Its frequency band shall cover the range of relevant frequencies (see 4.3.1.1).

Neither the speed governing system and power transmission of the test rig, nor the torsional natural frequency of model shaft shall produce significant contributions to shaft torque variation within the frequency band of interest.

##### 4.3 Analysis of model test results

Torque fluctuations are processed and displayed in the same way as pressure fluctuations (see 4.3.6). Amplitudes are made non-dimensional as for torque factors or coefficients (see 1.3.3.13.1 and 1.3.3.13.3). They are expressed in relative values. The reference can be the test efficiency or full load torque factor (or coefficient).

If there is no dynamic influence from the generator/motor at the frequency of interest, torque fluctuation amplitudes represent the global action of fluctuating pressure forces acting on the runner.

##### 4.4 Transposition to prototype

Torque fluctuation frequencies are transposable to the prototype if:

- ) they are the same as the pressure fluctuation frequencies;
- ) there is no dynamic influence from the generator/motor at the frequency of interest.

Model tests of a hydraulic machine will not reproduce the amplitudes of torque fluctuations on the prototype if they are significantly influenced by non-homologous boundary conditions: electric circuit, mechanical assembly and hydraulic piping system.

In particular, measured torque fluctuations in runaway or condenser operation are not relevant if the action of the model governing system is clearly dominant.

#### 4.5 Axial and radial thrust

##### 4.5.1 General

This subclause deals with steady-state measurement of forces (thrust) and moments acting on the runner/impeller of hydraulic machines.

In most cases it is sufficient to measure only the axial thrust in the course of the regular testing program. For the measurement of radial forces and moments, special arrangements have to be installed. Test arrangements are described below for the measurement of one component (axial thrust) up to the measurement of six components (all forces and moments acting on runner/impeller).

The measurement of the fluctuations of these axial and radial forces is part of the measurement methods and arrangement described later on. The data processing of these fluctuations is generally made in the same way as for pressure fluctuations (see 4.3.6).

##### 4.5.1.1 Purpose of measurements

The forces and moments due to hydrodynamic action are part of the overall load on the rotating part in a hydraulic machine. Important design parameters, such as forces acting on axial and radial bearings and embedded parts, stresses and deflections of the shaft, etc., can be computed and / or derived from model measurements.

The purpose of the measurements is to determine the magnitude and direction of forces and moments as function of the various operating conditions.

##### 4.5.1.2 Definitions

The forces and moments acting on the runner/impeller are defined in a stationary Cartesian system of coordinates (see Figure 101).

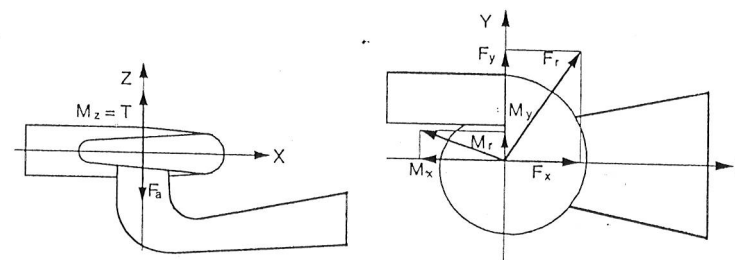


Figure 101 – Definition of coordinate system

The origin of the coordinates is determined by the reference level as specified in 1.3.3.7.6.

$F_x$  radial force, x-component;

$F_y$  radial force, y-component;

$F_z$  axial force ( $-F_z = F_a$  axial thrust);

$\vec{F}_r$  radial force ( $\vec{F}_r = \vec{F}_x + \vec{F}_y$ );

$M_x$  moment, x-axis;

$M_y$  moment, y-axis;

$M_z$  moment, z-axis (= shaft torque T);

$\vec{M}_r$  radial moment ( $\vec{M}_r = \vec{M}_x + \vec{M}_y$ );

The angles of the radial force and radial moment can be calculated in the defined coordinate system:

$$\varphi_{Fr} = \arctan \frac{F_y}{F_x} \quad \varphi_{Mr} = \arctan \frac{M_y}{M_x}$$

### 5.1.3 Influencing effects

In this subclause only the forces and moments caused by the hydrodynamic interaction between the runner/impeller and the test fluid are considered. Therefore, forces due to the following effects shall also be taken into account:

- weight of runner/impeller;
- centrifugal forces;
- hydrostatic effects (buoyancy);
- hydrodynamic effects in labyrinth seals;
- mechanical forces (friction);
- resonance effects.

The following subclauses describe how the above effects should be considered in each particular case.

## 5.2 Axial thrust

### 5.2.1 Test program

The test should cover the whole operating range with special attention to the region where the maximum axial thrust occurs or is expected. The test shall be carried out at specified prototype operating conditions. The number of test points between minimum and maximum specific hydraulic energy and from minimum to maximum discharge shall be sufficient to characterize the axial thrust. It is recommended that the test range extend beyond the contractually specified operating range and that the possible influence of cavitation on axial thrust be considered.

In addition to the normal operating range, axial thrust should be measured for off-design conditions such as those listed below:

- runaway conditions;
- off-cam conditions in double regulated machines;
- operating points during transient conditions with expected high axial thrust (e.g. transition from pump to turbine mode at maximum guide vane opening in pumps and pump-turbines);
- no-load conditions which can cause up-thrust in axial machines.

## 4.5.2.2 Measuring arrangements

### 4.5.2.2.1 Direct measurement

Numerous arrangements have been developed to measure the axial thrust acting onto a runner/impeller. In a typical testing arrangement the oil pressure within a hydrostatic bearing is measured as a reference quantity related to the hydraulic force acting onto the runner/impeller along its axis of rotation (see Figure 102).

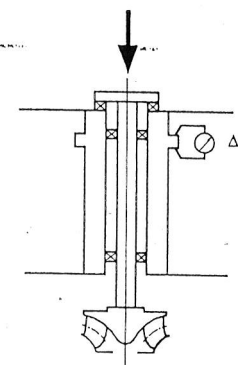


Figure 102 – Typical testing arrangement for axial thrust measurement

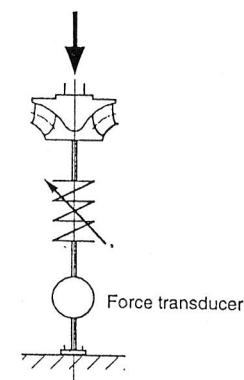


Figure 103 – Typical calibration arrangement for axial thrust measurement

Another typical arrangement uses the deflection of connecting parts between axial bearing and the housing which can be measured by means of strain gauges or inductive distance meters.

The axial thrust can also be determined with a measuring device for all six components of forces and moments (see Figure 105 d).

pending on the arrangement used, the following influencing effects shall be taken into count:

- hydrostatic forces on the shaft;
- oil viscosity;
- gravity forces;
- others.

### 5.2.2.2 Indirect determination

The axial thrust can be determined by a sufficient number of pressure measurements along the outer contour of the runner/impeller with the consideration of the calculated thrust component due to the change of momentum of flow. Corresponding pressure taps are shown in Figure 4. All those pressures should be referred to a reference pressure taken for instance in a reference section of the machine (see figure 1).

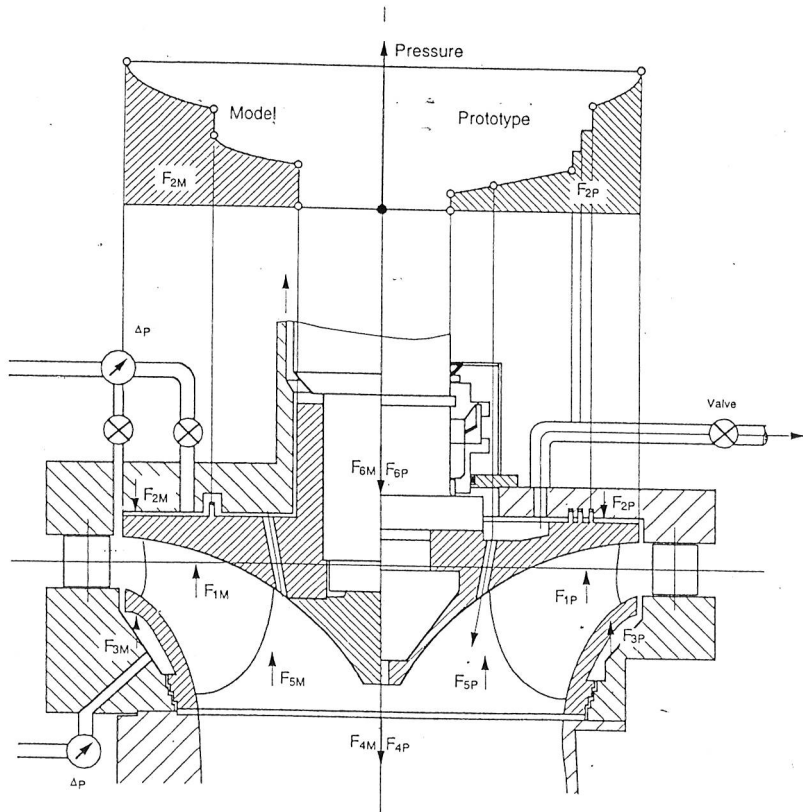


Figure 104 – Individual elements of axial force acting on a radial machine

### 4.5.2.3 Calibration

For calibration, a force is applied in axial direction to the model runner/impeller shaft. The magnitude of force is defined by:

- certified masses;
- masses together with a load cell;
- hydraulic jack together with a load cell (see Figure 103);
- others.

The reference forces applied to the shaft are related to the signal of the axial thrust measurement instrument in order to establish a calibration curve.

### 4.5.2.4 Checks during and after measurements

Before and after each test series, the measuring signal shall be recorded and checked at reference condition (e.g. at stand-still). It is recommended to check the axial thrust measurements varying the rotational speed at one operating point. This check indicates whether the calibration, compensation and evaluation are valid.

### 4.5.2.5 Transposition to prototype

The axial force  $F_{aM}$  measured on the model cannot always be directly transformed to prototype conditions. For a correct transposition, it is useful to consider separately the individual force elements of the total axial force for model and prototype.

Figure 104 and Table 9 show the axial force elements of total axial thrust in the example of a radial machine with a vertical shaft. The procedure as outlined can be applied to axial machines by omitting axial force elements on the runner band and crown.

Test data shall be corrected to account for all differences between the model and prototype regarding the runner/impeller (seal geometry, balance holes, balance pipes). Note that even complete geometrical similarity between model and prototype does not automatically provide similarity of flow in these regions.

The model axial thrust is composed of the following elements

$$F_{aM} = F_{1M} + F_{2M} + F_{3M} + F_{4M} + F_{5M} + F_{6M}$$

Hence

$$F_{1M} = F_{aM} - (F_{2M} + F_{3M} + F_{4M} + F_{5M} + F_{6M})$$

The following dimensionless axial force factors/coefficients (see 1.3.3.13.2 and 1.3.3.13.4):

$$F_{1ED} = \frac{F_1}{D^2 \cdot \rho \cdot E} \quad \text{axial force factor;}$$

$$F_{1nD} = \frac{F_1}{D^4 \cdot n^2 \cdot \rho} \quad \text{axial force coefficient;}$$

permit the calculation of prototype axial force using the following equations:

$$F_{1P} = F_{1M} \cdot \left( \frac{D_P}{D_M} \right)^2 \cdot \frac{E_P}{E_M} \cdot \frac{\rho_P}{\rho_M} = F_{1ED} \cdot D_P^2 \cdot \rho_P \cdot E_P$$

$$F_{1P} = F_{1M} \cdot \left(\frac{D_P}{D_M}\right)^4 \cdot \left(\frac{n_P}{n_M}\right)^2 \cdot \frac{\rho_P}{\rho_M} = F_{1nD} \cdot D_P^2 \cdot n_P^2 \cdot \rho_P \cdot E_P$$

ice for the axial thrust at prototype:

$$F_{aP} = F_{1P} + F_{2P} + F_{3P} + F_{4P} + F_{5P} + F_{6P}$$

prototype axial force can be determined also by a combined approach of measurement calculation. In this case the computer program used for calculation of the prototype axial e is calibrated by calculating the model axial force and subsequent comparison with model results. The same program can also be used to calculate the prototype axial force in case increased crown pressure due to wear of runner/impeller seals.

Table 9 – Individual force elements of axial thrust and their treatment

Force element	Model	Prototype
Hydrodynamic 1)	Determined from measurement by subtracting $F_2$ to $F_6$ from $F_{aM}$ .	Transformed by using $F_{1ED}$ or $F_{1nD}$ .
Crown	Calculated from parabolic pressure distribution. Measurement of static pressure is advisable. Not existing for axial type machines.	Calculated from parabolic pressure distribution. Not existing for axial type machines.
Band	Calculated from parabolic pressure distribution. Not existing for axial type machines.	Calculated from parabolic pressure distribution. Not existing for axial type machines.
Runner/impeller weight	Determined by weighing or considered in calibration procedure; in case of inclined axis, only the axial component shall be considered.	Determined by calculation.
Runner/impeller buoyancy	Determination from runner/impeller volume $F_5 = V \cdot \rho_w g$ or considered in calibration procedure. In case of inclined axis, only the axial component shall be considered.	Determined by calculation. $F_5 = V \cdot \rho_w g$
Hydrostatic shaft force	Pressure acting on areas exposed to atmosphere.	Pressure acting on areas exposed to atmosphere.

2.6 Uncertainty

a uncertainty in determination of prototype axial force results from the uncertainty in model asurement and from approximations in transposition from model to prototype.

th good measurement conditions it is possible to determine the mean values of the model al hydraulic force with an uncertainty of less than  $\pm (5 \text{ to } 10) \%$  of the extreme values urring during normal operation conditions. The uncertainty in corresponding derived ototype values is approximately  $\pm (10 \text{ to } 20) \%$  of the maximum mean values.

F<sub>1</sub> results from the axial hydrodynamic forces acting on the runner/impeller flow passage.

4.5.3 Radial thrust

4.5.3.1 Test program

The magnitude and direction of radial thrust (forces and moments) are necessary to determine stresses and deflections of the shaft, bearing and adjacent structure. The measurements should cover all main operating ranges with particular attention to those operating points where extreme values of radial thrust occur (mean and/or fluctuating).

Typical examples of operating conditions where extreme radial forces can occur, are:

- runaway condition;
- zero discharge for pump;
- operating points associated with transient conditions;
- cavitation conditions.

4.5.3.2 Measuring arrangements

The radial thrust can be determined by measurement of the following quantities (see Figure 105):

- reaction forces in one or two shaft bearings;
- supporting forces of the bearing housing;
- deflection of the shaft;
- multidirectional strain in a special measuring section of the shaft close to the runner/ impeller.

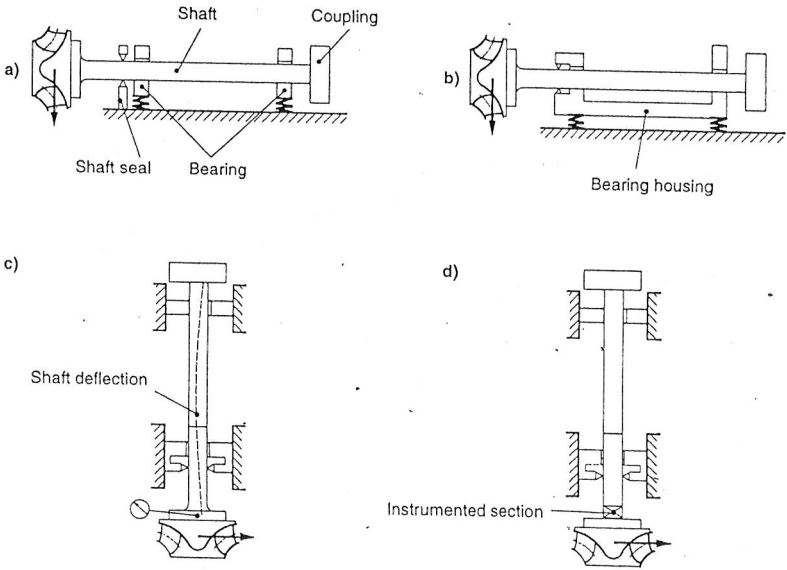


Figure 105 – Typical arrangements for radial thrust measurement (horizontal or vertical shaft).

Arrangement d) of Figure 105 permits measurement of all six components of forces and moments ( $F_x$ ,  $F_y$ ,  $F_z$ ,  $M_x$ ,  $M_y$ ,  $M_z$ ) in both the rotating and the stationary system. The signals of the strain gauge bridges are transferred from the shaft to the stationary part by means of slip rings or a telemetry device. The angle of rotation is continuously measured and the signals are transformed to stationary coordinates.

Depending on the arrangement used, measurements of radial thrust can be affected by non-hydraulic forces as shown in Table 10.

Measurement of radial thrust can be significantly influenced by a hydrodynamic bearing effect of the radial seals. This influence can be reduced by using increased seal clearances in the model for radial thrust measurement.

Table 10 – Non-hydraulic forces influencing radial thrust measurement

Origin of non-hydraulic forces		Arrangements of measurement			
		a	b	c	d
Shaft	(natural frequency)	x	x	x	x
Coupling	(inertia)	x	x	x	
Bearing housing	(inertia)		x		
Shaft seals	(reaction)	x		x	

### 5.3.3 Calibration

The basic calibration is usually done by applying forces and moments on the shaft using a known lever arm and certified masses. The actual forces and moments are related to the readings of the respective instruments. If oil pressure is used to determine bearing forces, the oil temperature shall be recorded and the influence of viscosity (if any) taken into account for evaluation. If the measurement is done in the rotating system (arrangement d), the calibration shall be carried out in rotating condition.

Since only the hydrodynamic radial thrust shall be determined, the following effects shall be taken into account by calibration:

- weight of the runner/impeller;
- buoyancy;
- unbalance of rotating parts.

The weight and buoyancy of the runner/impeller are only relevant if model and/or prototype do not have a vertical shaft. The weight is taken into account by measuring the radial thrust at low rotation in air. Weight and buoyancy are taken into account by measuring at slow rotation in water. The centrifugal force due to unbalance of the rotating parts is taken into account by measuring the radial force at fast rotation in air.

### 5.3.4 Checks before and during measurements

Before and after each test series, the measuring signal shall be recorded and checked at reference condition (e.g. at stand-still). It is recommended to check the radial thrust measurements varying the rotational speed at one operating point. This check indicates whether the calibration, compensation and evaluation are valid.

The speed variation test can also show significant deviations for a certain speed of rotation which indicates a model-specific resonance effect.

### 4.5.3.5 Transposition to prototype

The radial force measured in the model can be transposed to prototype provided that all influencing effects are eliminated and only hydrodynamic forces are considered.

The following dimensionless radial forces and moment factors/coefficients (see 1.3.3.13):

$$F_{rED} = \frac{F_r}{D^2 \cdot \rho \cdot E} \quad \text{radial force factor}$$

$$M_{rED} = \frac{M_r}{D^3 \cdot \rho \cdot E} \quad \text{radial moment factor}$$

$$F_{rED} = \frac{F_r}{D^4 \cdot n^2 \cdot \rho} \quad \text{radial force coefficient}$$

$$M_{rED} = \frac{M_r}{D^5 \cdot n^2 \cdot \rho} \quad \text{radial moment coefficient}$$

permit the calculation of prototype radial force and moment by using the following equation:

$$F_{rP} = F_{rM} \cdot \left( \frac{D_P}{D_M} \right)^2 \cdot \frac{\rho_P}{\rho_M} \cdot \frac{E_P}{E_M} = F_{rED} \cdot D_P^2 \cdot \rho_P \cdot E_P$$

$$F_{rP} = F_{rM} \cdot \left( \frac{D_P}{D_M} \right)^4 \cdot \left( \frac{n_P}{n_M} \right)^2 \cdot \frac{\rho_P}{\rho_M} = F_{rED} \cdot D_P^4 \cdot n_P^2 \cdot \rho_P$$

$$M_{rP} = M_{rM} \cdot \left( \frac{D_P}{D_M} \right)^3 \cdot \frac{\rho_P}{\rho_M} \cdot \frac{E_P}{E_M} = M_{rED} \cdot D_P^3 \cdot \rho_P \cdot E_P$$

$$M_{rP} = M_{rM} \cdot \left( \frac{D_P}{D_M} \right)^5 \cdot \left( \frac{n_P}{n_M} \right)^2 \cdot \frac{\rho_P}{\rho_M} = M_{rED} \cdot D_P^5 \cdot n_P^2 \cdot \rho_P$$

Transposition of radial forces from model to prototype requires definition of the axial position of the plane in which the radial thrust is referred. Preferably this could be the plane corresponding to the defined reference level (see Figure 5, subclause 1.3.3.7).

The transposition from model to prototype shall also take into account non-homologous mechanical components and conditions (see 4.1.4).

### 4.5.3.6 Uncertainty

The uncertainty in prototype radial force depends on the model measurement uncertainty and the approximations in transposition from model to prototype.

Even with good measurement conditions, it is not possible to determine the mean values of model radial forces with uncertainties smaller than  $\pm (5 \text{ to } 10) \%$  of the maximum mean values.

The corresponding prototype mean values of the radial forces cannot be determined with an uncertainty smaller than  $\pm (10 \text{ to } 20) \%$  of the maximum mean value. The uncertainty of the fluctuations can be even higher.

## Hydraulic loads on control components

### 1 General

#### 1.1 Type of control components

In order to control power or discharge, most types of hydraulic reaction machines are equipped with:

- guide vanes, and/or
- adjustable runner/impeller blades.

- control elements of impulse turbines (e.g. Pelton turbines) are the nozzle(s) with adjustable needle(s) and deflector(s).

Sometimes gates or valves can be used as control components, but they are not considered in the following.

#### 1.2 Purpose of load measurements

The purpose of such tests is to check or determine by means of model measurements the hydraulic loads i.e. forces and torques acting on the control components of a machine. The model is always operated at steady state operating conditions (see 4.1.1).

Model results (absolute or dimensionless values) can be used to:

- check the extreme values of hydraulic loads which are relevant for the prototype design (mean values and fluctuating components);
- establish at which operating conditions the fluctuating amount of a hydraulic load becomes important and which are the relevant excitation frequencies;
- check at which operating conditions the hydraulic torque has opening or closing tendency;
- produce input data for calculation of prototype loads during transient operating conditions;
- determine torques acting on aligned and misaligned guide vanes as required for the design and adjustment of guide vane and guide vane protective devices.

#### 1.3 Design of control components for hydraulic loads measurements

Model components prepared for hydraulic load measurements are often of special design. If strain gauges are used, the deformation of the instrumented component under hydraulic load must be such that sufficient strain is produced. This can be achieved by an appropriate design, however the impact on the mechanical safety and the natural frequency of the measuring component must be checked. It is also important to check how much the model measurements will be affected by friction forces or torques. If friction effects are not negligible, their effects will be eliminated from the final model test results because their relative value is different on the prototype.

As a consequence of the design, it can be necessary to perform such tests at a reduced test specific hydraulic energy, in order to avoid inadmissible hydraulic loads or resonance conditions. Therefore, it is important to determine the natural frequency in water of such measuring components.

Sometimes it is preferable to prepare additional measuring components which are only installed for hydraulic load tests, so that the main hydraulic performance tests can be done without limitations and without risk of damaging measuring components.

#### 4.6.1.4 Signal processing

The measuring signal from calibration and/or measurement can be recorded manually or automatically. However, for extensive measurements with many test points or many measuring components, automatic data acquisition is recommended. This also facilitates the data processing and display of test results in the same way as for pressure fluctuation (see 4.3.6).

#### 4.6.2 Guide vane torque

##### 4.6.2.1 Number and position of measuring guide vanes

Experiences from many tests demonstrate that due to hydraulic and/or structural design, the inflow and outflow conditions for distributors of reaction machines can change along the circumference of a spiral case or of an intake of a tubular turbine. Therefore, the torque shall be measured on several guide vanes located at representative circumferential positions:

- a) for a spiral case: two in the zone influenced by the nose vane and one opposite to it;
- b) for a semi-spiral case: more than three measuring guide vanes can be required;
- c) for a tubular turbine: two in the zone influenced by the bulb support or by the pit and one in the perpendicular direction.

When similar test data already show the circumferential influence, it can be agreed that only one or two measuring guide vanes are used.

When the number of stay vanes and guide vanes are different, the torque shall be measured on two adjacent guide vanes, unless data of similar arrangements are available which show no significant differences between two adjacent guide vanes.

If the impact of a misaligned guide vane on the neighboring guide vane torques shall be established, it is necessary to measure the torque on three adjacent guide vanes, whereby the one in the middle is misaligned.

##### 4.6.2.2 Number of test points

The operating conditions and the number of test points depend strongly on the type of the machine and the purpose of the test. In turbine operation the main governing parameter is the discharge factor or guide vane opening. The speed factor influence is small and practically negligible for high specific speed turbines. It is often sufficient to measure the guide vane torque only at the limits of the operating range defined by the specified values  $E_{nDmax}$  and  $E_{nDmin}$  (see Figure 107). For higher specific speed Francis turbines and for axial turbines, it is sufficient to measure the guide vane torque only at one constant specified value  $E_{nD}$  within the operating range. In this case, the evaluation shall be made by using a guide vane torque factor  $T_{G,0D}$  defined in 4.6.2.6.

The number of test points shall be increased if the extended operating range is to be investigated. Transient analysis requires a sufficient number of test points.

If guide vane torques are measured with a misaligned guide vane, it is important to agree on the possible geometric configurations and hydraulic operating conditions so that the measuring program does not become too extensive.

#### 4.6.2.3 Measuring arrangement

In most cases the hydraulic torque acting on a guide vane is determined by measuring the torsional deformation of the guide vane stem using bonded strain gauges. The upper end of the measuring stem is fixed into the adjusting mechanism of the guide vane. It is possible to use the normal guide vane stem, often with a reduced diameter, or to replace the normal stem by a special measuring stem, sometimes of a different material with a suitable elastic modulus and load hysteresis. Figure 106 illustrates two typical design examples.

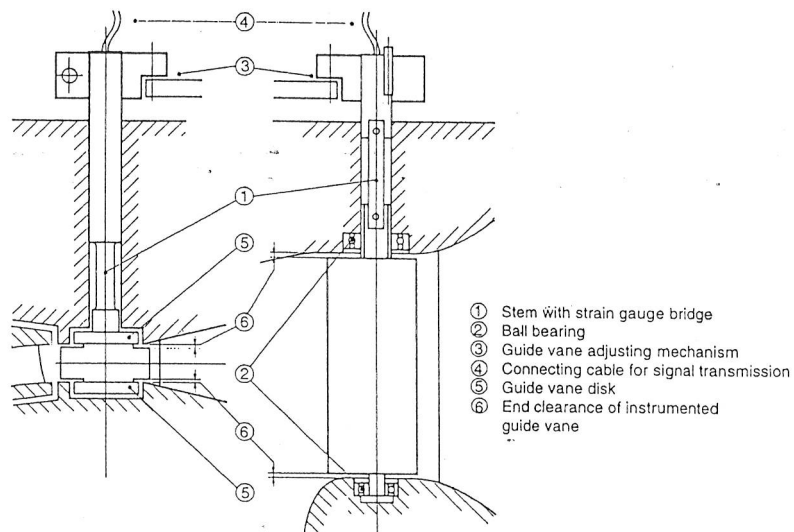


Figure 106 – Design examples for torque measuring guide vanes

In order to avoid disturbing effects by friction due to lateral and/or axial hydraulic forces, special attention shall be paid to the design of the support of the measuring stem (for example ball bearings can be applied) and to the guide vane end clearances, which can be increased for the torque measurement. The design of the guide vane disks (if any) shall be such that during measurement no disturbing axial thrust can result.

If the measuring section is not located in dry air, it is important that a good surface protection against humidity is applied. The electric insulation resistance should be checked periodically.

#### 4.6.2.4 Calibration

For calibration, static loads are usually applied on the measuring guide vane in opening and closing directions by means of a known lever arm and certified masses. The calibration can be made with the guide vane installed in the model machine or by installing the guide vane in a special calibration device.

The stability of the no-load operating point and the hysteresis due to loading and unloading shall be checked, as well as the drift of the measuring signal under constant load. The result of calibration is usually an averaged calibration curve with the output signal versus calibration torque.

#### 4.6.2.5 Checks before and during measurement

It is recommended that after installation of the guide vane in the model, a check loading is made (especially when the guide vane was calibrated in a separate calibration device) in order to prove the correct mechanical installation (no friction) and to check the processing of the measuring signal and the sign for opening and closing tendency.

Preliminary tests including a rotational speed variation shall demonstrate that filtering the noise of the measuring signal does not affect the signal itself and that resonance conditions are avoided. Before and after each test series, the measuring signal at zero-load shall be recorded and checked.

In pump mode it should be possible to identify the impeller blade passing frequency as dominating excitation frequency. This can also be the case for pump-turbines in turbine mode.

#### 4.6.2.6 Calculation of dimensionless torque factors and prototype guide vane torques

For each operating point a mean value  $T_G$  is determined which can be used to calculate a dimensionless guide vane torque factor  $T_{G,ED}$  or  $T_{G,QD}$ .

Definition of guide vane torque factors (see 1.3.3.13.1):

$$T_{G,ED} = \frac{T_G}{\rho \cdot D^3 \cdot E}$$

or

$$T_{G,QD} = \frac{T_G \cdot D}{\rho \cdot Q^2}$$

Based on hydraulic similarity conditions, the prototype guide vane torque can be calculated either using one of the torque factors or the absolute model values.

$$T_{G,P} = T_{G,M} \cdot \left( \frac{D_P}{D_M} \right)^3 \cdot \frac{E_P}{E_M} \cdot \frac{\rho_P}{\rho_M} = T_{G,ED} \cdot D_P^3 \cdot E_P \cdot \rho_P$$

or

$$T_{G,P} = T_{G,M} \cdot \left( \frac{Q_P}{Q_M} \right)^2 \cdot \frac{D_M}{D_P} \cdot \frac{\rho_P}{\rho_M} = T_{G,QD} \cdot Q_P^2 \cdot \frac{1}{D_P} \cdot \rho_P$$

It is to be noted that the resulting hydraulic prototype guide vane torque does not include friction in the guide vane bearing, seals and adjustment mechanism. Usually the bearing friction torque is rather small due to vibrations of the guide vanes, whereas the friction in the adjusting mechanism linking guide vanes and servo motor(s) is more important. The total amount of prototype friction torque is to be determined by calculation or by experience from site measurements.

### 5.2.7 Graphical presentation of results

For normal operation in both turbine mode or pump mode the guide vane torque or the corresponding factor is usually represented versus the guide vane angle at defined hydraulic conditions (e.g. at a selected  $E_{p,sp}$ ). Moreover, in pump mode the relevant value of the guide vane torque or of the corresponding factor usually corresponds to the envelope curve  $E_{nD}$  versus  $Q_{nD}$ .

Guide vane torques occurring in one or more quadrants (see 4.7.2) are usually measured at several constant guide vane angles and are presented as a function of the speed factor  $n_{ED}$  or discharge factor  $Q_{ED}$ .

Examples of test results are presented in Figure 107, Figure 108 and Figure 109.

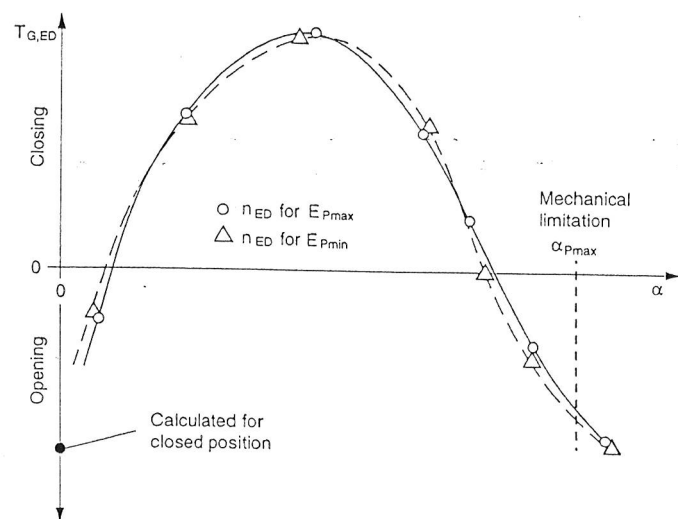


Figure 107 – Guide vane torque factor versus guide vane angle measured at different constant specific hydraulic energies in turbine mode

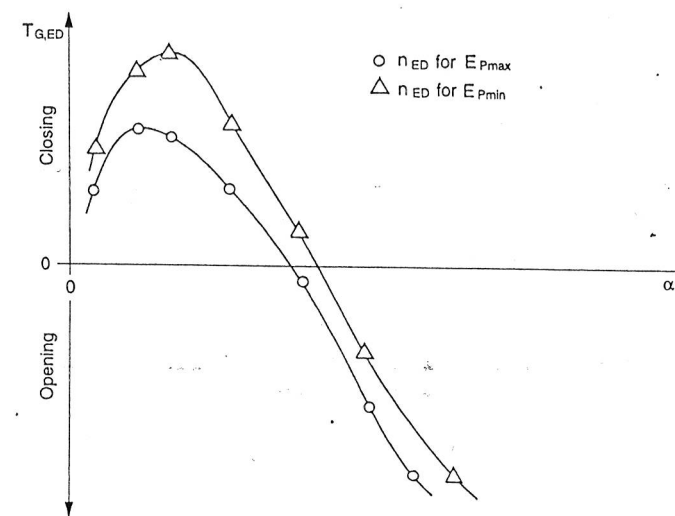


Figure 108 – Guide vane torque factor versus guide vane angle measured at different constant specific hydraulic energies in pump mode

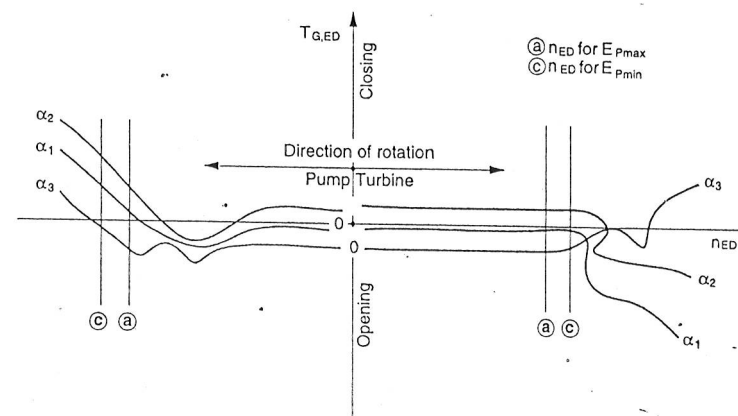


Figure 109 – Guide vane torque factor versus speed factor measured at different constant guide vane angles in the four quadrants of a pump-turbine

### 3.2.8 Comparison of guide vane torque fluctuations on model and prototype

In most cases the guide vane torque fluctuations measured on the model should not be directly scaled up to prototype conditions without applying corrections because of the following aspects:

- the hydroelastic similarity laws are not fulfilled;
- damping effects due to water added mass and bearing design are different;
- the ratios of excitation frequencies and natural frequencies are different.

### 3.2.9 Uncertainty

The uncertainty of model guide vane torque results is influenced by the following factors:

- hysteresis of the calibration curve of the instrumented guide vanes;
- repeatability and drift of the zero torque point;
- influence of any friction effects.

Under good measurement conditions, it is possible to determine the mean values of model hydraulic torque with an uncertainty of about  $\pm 5\%$  of the maximum mean values. The uncertainty in corresponding derived prototype values is about  $\pm (5 \text{ to } 10)\%$  of the maximum prototype mean value.

The amplitudes of guide vane torque fluctuations of the model in normal operation can be determined with an uncertainty smaller than about  $\pm 10\%$ , whereas predicted prototype values can have an uncertainty up to  $\pm (50 \text{ to } 100)\%$ .

The zero torque guide vane angles, if any, can be determined with an uncertainty smaller than  $1^\circ$  on the model and can be predicted for the prototype with an uncertainty of about  $\pm 2^\circ$ . This zero torque angle can vary along the circumference depending on the variation of inflow and/or flow conditions.

## 3.3 Runner blade torque

### 3.3.1 Number of instrumented blades

In the case of diagonal and axial type machines with adjustable runner/impeller blades, the runner blade torque is usually measured on one blade.

### 3.3.2 Number of test points

The number of test points depends on the purpose of the test. For a double regulated machine the runner blade torque depends on the runner blade angle, guide vane angle and on the operating point. During normal operation, runner blade and guide vane angles are at on-cam positions. In transient conditions, numerous off-cam positions occur. Therefore, it is necessary to measure enough test points for checking the runner blade torque values occurring in off-cam operation.

### 4.6.3.3 Test procedure

In most cases such tests are performed at high Thoma number values, i.e.  $\sigma > \sigma_{pl}$ . However, at large discharge values, cavitation on the runner blades can affect the resulting blade torque. Therefore, at some selected operating points, the impact of variable  $\sigma$  on runner blade torque can also be checked.

On most models the runner blade angle is adjusted manually at stand still. As a consequence, runner blade torque tests are performed at selected constant runner blade angles whereas a hydraulic parameter, e.g. the speed factor  $n_{ED}$ , and the guide vane angle are varied systematically, covering the whole range of interest.

### 4.6.3.4 Measuring arrangement

Usually the hydraulic torque acting on a runner or impeller blade is determined by measuring the torsional deformation of the blade trunnion using bonded strain gauges. The end of the trunnion is fixed inside the hub. It is possible to use the normal trunnion, often with a reduced diameter, or to replace the normal trunnion by a special measuring trunnion, sometimes of a different material with a suitable elastic modulus and load hysteresis. Figure 110 illustrates a design example using telemetry.

In order to avoid disturbing effects by friction, the measuring trunnion can be supported by ball bearings, and the blade-hub and tip clearances can be somewhat increased.

The arrangement shall be such that only the torsional strain is measured.

If the measuring section is not located in dry air, it is important that a good surface protection against humidity is applied. The electric insulation resistance should be checked periodically.

The measuring signal from the hub is transmitted either through the shaft to slip rings or by telemetry to the recording device outside the model machine.

### 4.6.3.5 Calibration

For calibration, static loads are usually applied on the measuring runner blade in opening and closing directions by means of a known lever arm and certified masses. The calibration can be made with the instrumented blade installed in the hub or by installing the instrumented blade in a special calibration device.

The stability of the zero torque point and the hysteresis due to loading and unloading shall be checked, as well as the drift of the measuring signal under constant load. The result of calibration is usually an averaged calibration curve with the output signal versus the calibration torque.

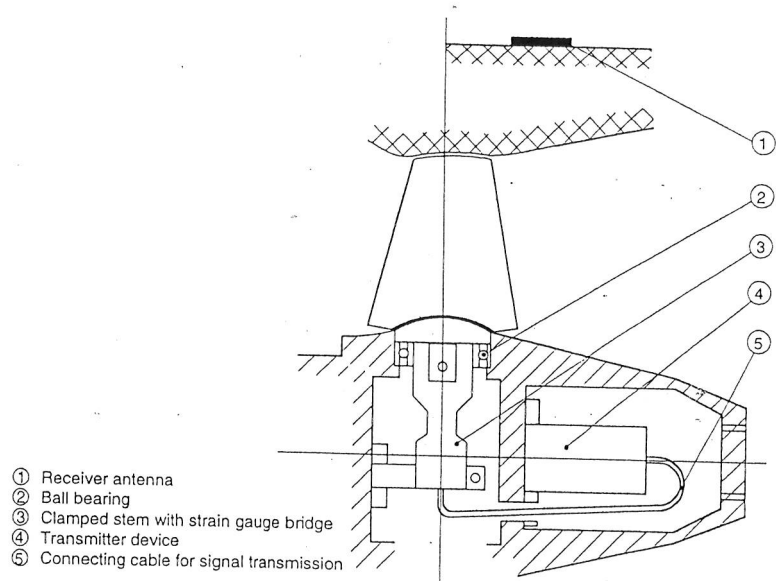


Figure 110 – Example for runner blade torque measuring arrangement using telemetry

#### 6.3.6 Checks before and during measurement

It is recommended that after installation of the instrumented runner blade in the model, a check adding is made at standstill (especially when the runner blade was calibrated in a separate vibration device) in order to prove the correct mechanical installation (no friction) and to check the processing of the measuring signal and the sign for opening and closing tendency.

Preliminary tests, including a rotational speed variation, shall demonstrate that filtering the noise of the measuring signal does not affect the signal itself and that resonance conditions are avoided. Before and after each test series the measuring signal at zero-load shall be recorded and checked.

#### 6.3.7 Consideration of centrifugal effects

The measured torque is a result of the hydraulic pressure distribution around the blade and of the momentum due to the resulting centrifugal force which normally does not act in direction of the blade-trunnion centre-line. When different blade materials are used for model and prototype, it is necessary to separate both torque components. It is recommended to determine the blade torque due to centrifugal effects separately, by means of a test with the runner spinning in air with different rotational speeds and blade angles or by appropriate calculation.

Consequently, for each operating point the hydrodynamic blade torque  $T_{Bh}$  is the difference between the measured torque  $T_{Blot}$  and the torque due to centrifugal effects  $T_{Bc}$ :

$$T_{Bh} = T_{Blot} - T_{Bc}$$

#### 4.6.3.8 Calculation of dimensionless torque factors and prototype hydrodynamic runner blade torque

For each operating point a mean value  $T_{Bh}$  is determined as the difference between the measured torque  $T_{Blot}$  and the torque due to centrifugal effects  $T_{Bc}$ .  $T_{Bh}$  can be used to calculate a dimensionless torque factor  $T_{Bh,ED}$ .

Definition of blade torque factors/coefficients (see 1.3.3.13):

Hydraulic blade torque factor:

$$T_{Bh,ED} = \frac{T_{Bh}}{\rho \cdot D^3 \cdot E}$$

Runner blade torque coefficient due to centrifugal effects:

$$T_{Bc,ED} = \frac{T_{Bc}}{\rho_B \cdot n^2 \cdot D^5} \quad \text{where } \rho_B \text{ is the density of blade material}$$

Based on hydraulic similarity conditions, the prototype runner blade torque can be calculated either using the torque factors/coefficients or the absolute model values.

Hydraulic prototype runner blade torque:

$$T_{Bh,P} = T_{Bh,M} \cdot \left( \frac{D_P}{D_M} \right)^3 \cdot \frac{E_P}{E_M} \cdot \frac{\rho_P}{\rho_M} = T_{Bh,ED} \cdot D_P^3 \cdot E_P \cdot \rho_P$$

Prototype runner blade torque due to centrifugal effects:

$$T_{Bc,P} = T_{Bc,M} \cdot \left( \frac{D_P}{D_M} \right)^5 \cdot \frac{n_P^2}{n_M^2} \cdot \frac{\rho_{BP}}{\rho_{BM}} = T_{Bc,ED} \cdot D_P^5 \cdot n_P^2 \cdot \rho_{BP}$$

Total prototype runner blade torque:

$$T_{Blot,P} = T_{Bh,P} + T_{Bc,P}$$

It is to be noted that the hydraulic prototype runner blade torque does not include friction in the runner blade bearings and seals nor in the adjusting mechanism. Usually the bearing friction torque is rather small due to vibrations of the runner blades, whereas the friction in the adjusting mechanism linking runner blades and servo motor(s) is more important. The total amount of prototype friction torque is to be determined by calculation or by experience from site measurements.

#### 4.6.3.9 Graphical presentation of results

For normal turbine mode operation the runner blade torque or the corresponding factor is usually represented for each runner blade angle as a function of the speed factor  $n_{ED}$  or discharge factor  $Q_{ED}$  for different constant guide vane openings. An example of test results is presented in Figure 111.

### 3.10 Comparison of runner blade torque fluctuations on model and prototype

most cases the runner blade torque fluctuations measured on the model should not directly scaled up to prototype conditions without applying corrections because of the following facts:

- the hydroelastic similarity laws are not fulfilled;
- damping effects due to water added mass and bearing design are different;
- the ratios of exciting frequencies and natural frequency are different.

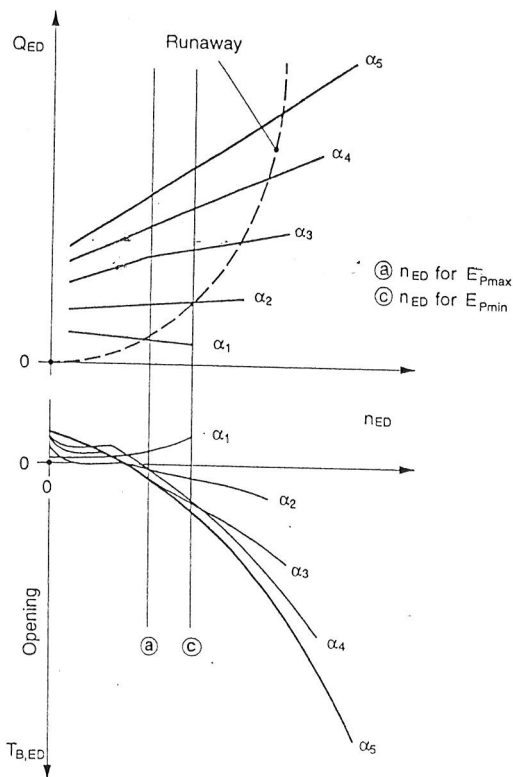


Figure 111 – Performance and hydraulic runner blade torque characteristics of an axial turbine measured at one constant runner blade angle  $\beta$  and various constant guide vane angles  $\alpha$ .

#### 4.6.3.11 Uncertainties

The uncertainty of model runner blade torque results is influenced by the following factors:

- a) hysteresis of the calibration curve of the instrumented runner blade;
- b) repeatability and drift of the zero torque point;
- c) influence of any friction effects;
- d) influence of cavitation.

With good measurement conditions, it is possible to determine the mean values of model hydraulic torque with an uncertainty smaller than about  $\pm 5\%$  of the maximum mean values. The uncertainty in corresponding derived prototype values is about  $\pm (5 \text{ to } 10)\%$  of the maximum prototype mean values.

Amplitudes of runner blade torque fluctuations on the model in normal operation can be determined with an uncertainty smaller than about  $\pm 10\%$ , whereas predicted prototype values can have an uncertainty of up to about  $\pm (50 \text{ to } 100)\%$ .

#### 4.6.4 Pelton needle force and deflector torque

In most cases it is not necessary to measure needle forces and deflector torques because either sufficient data are available from model or site tests or the data can be calculated.

##### 4.6.4.1 Number of measuring needles and deflectors

In multi-jet Pelton turbines, it is sufficient to measure the hydraulic load on only one needle and/or one deflector, because the flow differences between the various nozzles are not significant for these measurements.

##### 4.6.4.2 Test procedure

The needle force and the deflector torque mainly depend on their position and on the discharge. There is also an impact of the splashing water in the housing on the deflector torque. The speed factor of the runner has no influence on the needle force and only a small influence on the deflector torque. Needle force and deflector torque can therefore be determined by one test series, where the stroke is varied systematically from closed to fully open position, and at some selected stroke positions the deflector angle is also varied.

##### 4.6.4.3 Measuring arrangement

- a) Needle force: the hydraulic force acting on the needle can be directly measured by means of load cell fixed inside the inner servomotor and mechanically connected to the rod end of the needle. It is also possible to extend the needle rod through the distributor such that the load cell can be fixed outside. In addition, the static pressure should be recorded in the nozzle body to consider a possible force resulting from different diameter ratios between nozzle opening and needle rod on model and prototype.
- b) Deflector torque: the hydraulic torque acting on the deflector can be determined by measuring deformations with strain gauges applied at its supporting structure or adjusting mechanism. In case of horizontal shaft Pelton turbines, deflector torque includes both hydraulic torque and gravitational torque acting on the deflector. Therefore, the gravitational torque should be measured beforehand in air to obtain the proper hydraulic torque from the measured torque.

The design shall be such that the force or torque measurement is not significantly affected by friction effects. If the measuring section is not located in dry air, it is important that a good surface protection against humidity is applied. The electric insulation resistance should be checked periodically.

#### 6.4.4 Calibration

Preferably the calibration is made with the same measuring arrangement as used for the tests in order to check and/or to consider the friction forces of the bearing and seal system.

Needle force: the load cell installed on the needle rod is loaded statically with certified masses.

Deflector torque: provisions shall be made to apply on the deflector known forces or torques using a calibrated load cell or certified masses. In case of a force, it is important to determine its direction and the distance to the pivot (length of the lever arm).

#### 6.4.5 Checks before and during measurement

Before and after each test series, the measuring signal at standstill (nozzle not completely closed, deflector not touching its stop) shall be recorded and checked. Preliminary tests shall demonstrate that the force factor and/or torque factor are not dependent on the test rotational speed nor on the test specific hydraulic energy.

#### 6.4.6 Calculation of dimensionless force and torque factors and prototype data

For each operating point, a mean value  $F_N$  and/or  $T_D$  is determined which can be used to calculate a dimensionless needle force factor  $F_{N,ED}$  and/or a dimensionless torque factor  $T_{D,ED}$ .

Definition of needle force factor (see 1.3.3.13.2):

$$F_{N,ED} = \frac{F_N}{\rho \cdot D^2 \cdot E}$$

Definition of deflector torque factor (see 1.3.3.13.1):

$$T_{D,ED} = \frac{T_D}{\rho \cdot D^3 \cdot E}$$

Based on hydraulic similarity conditions, the prototype needle force and/or deflector torque can be calculated either using the force and/or torque factors or the absolute model values.

Calculation of hydraulic prototype needle force:

$$F_{N,P} = F_{N,M} \cdot \left( \frac{D_P}{D_M} \right)^2 \cdot \frac{E_P}{E_M} \cdot \frac{\rho_P}{\rho_M} = F_{N,ED} \cdot D_P^2 \cdot E_P \cdot \rho_P$$

If needle rod diameters on model and prototype are non-homologous, a correction shall be applied to get the total force  $F_{Ntot,P}$ .

Calculation of hydraulic prototype deflector torque:

$$T_{D,P} = T_{D,M} \cdot \left( \frac{D_P}{D_M} \right)^3 \cdot \frac{E_P}{E_M} \cdot \frac{\rho_P}{\rho_M} = T_{D,ED} \cdot D_P^3 \cdot E_P \cdot \rho_P$$

#### 4.6.4.7 Graphical presentation of results

Usually the needle force factor is represented as a function of the needle stroke  $s$  referred for example to the nozzle outlet diameter:  $F_{N,ED} = f(s/d)$ . At closed position of the nozzle,  $s = 0$ . An example is presented in Figure 112.

Usually the deflector torque factor is represented as a function of the deflector position.

#### 4.6.4.8 Comparison of fluctuations of needle force and deflector torque on model and prototype

Because there is no impact of the flow in the runner on the needle, the fluctuations of the needle force are negligible. At fully opened position, the deflector is exposed to splashing water from the runner inducing torque fluctuations. At deflecting positions, torque fluctuations are mainly due to splashing water of the deflected jet. Since in most cases the hydraulic similarity with respect to the two-phase flow in the housing is not fulfilled, deflector torque fluctuations measured on the model should not be directly scaled-up to prototype conditions.

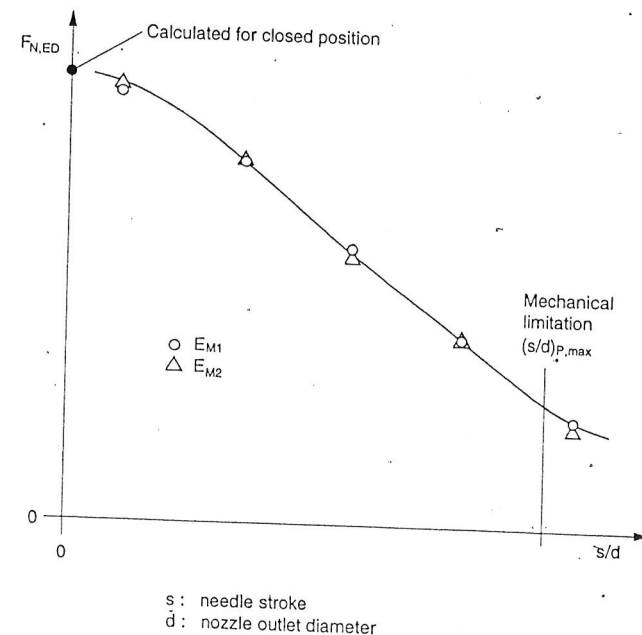


Figure 112 – Pelton needle force factor as a function of relative needle stroke

### 6.4.9 Uncertainty

The uncertainty in the measurement of model needle force and deflector torque is influenced by the following factors:

- hysteresis of the calibration curve of the instrumented components;
- repeatability and drift of the zero force or torque point;
- influence of any friction effects.

With good measurement conditions, the mean values of the model deflector torque or of the needle force can be determined with an uncertainty of about  $\pm 5\%$  of the maximum mean values. The uncertainty in corresponding derived prototype values could be about  $\pm (5 \text{ to } 10)\%$  of the maximum prototype mean value.

## 7 Testing in an extended operating range

### 7.1 General

In addition to the determination of hydraulic characteristics of a machine in a limited range of specific hydraulic energies and discharges, it is also important to know its complete characteristics covering possible operating conditions outside the normal operating range. The most extended field of operation exists for pumps and pump-turbines due to two directions of discharge and two directions of rotation (four-quadrants operation).

As stated in 4.1.1, model tests do not reproduce transient operation of the prototype. However, the obtained data are meaningful and are a necessary input for the calculations of transient phenomena and loads for prototype design.

### 7.2 Terminology

A comprehensive representation of hydraulic characteristics of a hydraulic machine is given by the four-quadrant-diagram.

#### 7.2.1 Definition of the quadrants

The four quadrants are defined by the combination of the positive or negative direction of discharge and rotational speed as follows (see Table 11, Figure 113 and Figure 114).

Table 11 – Definition of quadrants and operating modes

Quadrant		Direction (sign) of				Mode
Number	Name	Q	n	E	T	
1	Pump quadrant	-	-	-	-	Reverse turbine
				-	+	Brake
				+	+	Pump
1/2		0	-	+	+	Zero discharge
2	Brake quadrant	+	-	+	+	Pump-brake
2/3		+	0	+	+	Zero speed
3	Turbine quadrant	+	+	+	+	Turbine
				+	0	Runaway
				+	-	Turbine-brake
				-	-	Reverse rotation pump (axial machines only)
3/4		0	+	+/-	-	Zero discharge
4	Reverse pump quadrant	-	+	+	-	Reverse rotation pump (radial machines only)
4/1		-	0	-	-	Brake
				-	-	Zero speed

In each of these four quadrants several modes of operation are possible due to:

- the sign of power (output/input), corresponding to the direction of torque;
- the sign of specific hydraulic energy in special cases of application (e.g. tidal power plant).

In the following subclause 4.7.2.2 the normal cases of hydroelectric application with positive value of E are described.

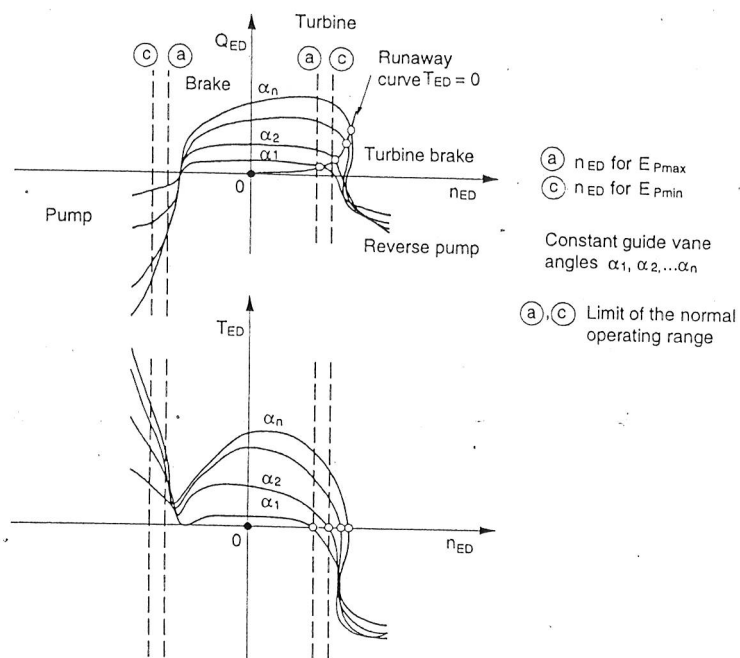


Figure 113 – Example of four quadrants operation of a radial-type pump-turbine

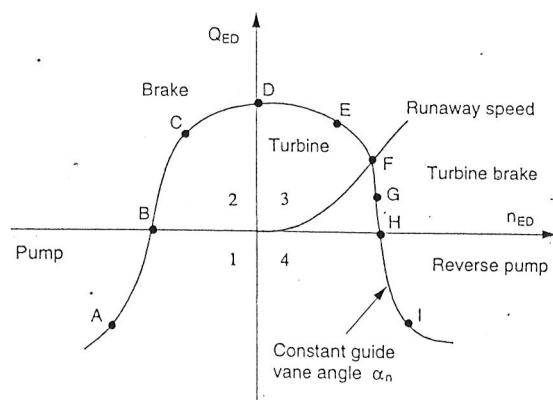


Figure 114 – Chart illustrating the various operating modes

#### 4.7.2.2 Operating modes

##### 4.7.2.2.1 Pump mode

The pump mode is characterized by negative discharge and negative rotational speed (see operating point A on Figure 114).

##### 4.7.2.2.2 Pump brake mode

This mode is characterized by negative direction of rotation but positive direction of discharge (see point C). This mode is of importance in case of power failure in pump operation.

##### 4.7.2.2.3 Turbine mode

This mode has positive direction of discharge and rotational speed and a positive torque is delivered to the machine shaft (see point E). The particular case of zero torque corresponds to turbine runaway (see point F).

##### 4.7.2.2.4 Turbine brake mode

This mode has positive direction of discharge and rotational speed but negative torque (see point G).

##### 4.7.2.2.5 Reverse rotation pump mode

This mode is characterized by a positive direction of rotational speed. However, the direction of discharge is negative (see point I). This mode can only be reached in transient condition.

#### 4.7.2.3 Operation at zero speed and zero discharge

Besides the operating modes within the quadrants, the operating points at the axes of coordinate are of interest (see Figure 114):

- the zero-discharge specific hydraulic energy  $E_0$  in pump mode (see point B);
- the zero-speed discharge and break-away torque (see point D);
- the zero-discharge specific hydraulic energy in turbine mode (see point H).

#### 4.7.3 Scope of tests

##### 4.7.3.1 Relevant modes of operation

Depending on the type of hydraulic machine one up to four quadrants are of interest:

- a) impulse turbine: only turbine mode and turbine brake mode exist because flow and speed have both obviously positive direction;
- b) reaction turbine: depending on specific speed and on guide vane opening, reverse rotation pump mode can reach importance in addition to normal turbine mode, particularly during load rejection and start up;
- c) axial-type pump-turbine: operation in three quadrants is feasible. Besides quadrants for normal pump and turbine modes, the brake quadrant can be passed during transient conditions. Reverse pump quadrant cannot be reached;
- d) radial-type pump or pump-turbine: operation in all four quadrants is feasible. Besides quadrants for normal pump and turbine modes, the turbine brake mode and even the reverse pump mode due to the radial extension of runner can be reached during transient conditions.

### 7.3.2 Performance data

performance data achieved during testing within normal operating range are taken also during four quadrant testing. The main hydraulic quantities to be measured are:

specific hydraulic energy;  
discharge;  
shaft torque;  
rotational speed;  
net positive suction specific energy.

Intervals between the measured points can be considerably increased compared to these in the guaranteed range of operation. On the other hand, it is recommended to extend the testing range to the maximum possible guide vane and/or runner/impeller blade openings which would be useful for the future operation of the prototype.

Hydraulic similarity laws still apply, however, secondary effects can change considerably the characteristics found in model testing. Particular attention has to be paid to the influence of cavitation on the hydraulic characteristics in extreme conditions.

### 7.3.3 Additional hydraulic data

In addition to the above listed main hydraulic data, specific measurements can be relevant. The content of test should be clearly defined prior to the test:

axial thrust;  
radial thrust;  
pressure fluctuations;  
hydraulic guide vane torque;  
runner blade torque;  
needle force;  
deflector torque;  
shaft torque fluctuations.

Specific requirements for above tests are discussed in subclauses 4.2 through 4.6 of this standard. Some of them are measured simultaneously with the main hydraulic data. Some of them need to have special arrangements and data acquisition systems.

## 7.4 Provisions for particular tests

There are no particular arrangements necessary for model tests outside the normal operating range. However, as there is no demand to get these hydraulic data with the same high accuracy as for the normal range, the specific hydraulic energy for these tests can be reduced in order to protect the model and the measurement system.

### 7.4.1 S-shape characteristics in turbine brake mode

Depending on the specific speed of a hydraulic reaction machine, the  $Q_{ED} - n_{ED}$  characteristics at constant guide vane opening can be S-shaped (see Figure 115). Testing under steady state conditions can then be difficult.

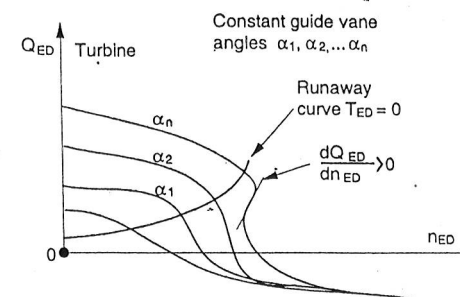


Figure 115 – S-shape characteristics in turbine brake mode

### 4.7.4.2 Pump characteristic

Depending on the design of a pump or pump-turbine, the slope of the  $E_{nD} - Q_{nD}$  characteristic can be positive in a limited range of discharge (see Figure 116). This positive slope can cause instability in operation. Therefore, this zone should be explored carefully, particularly considering maximum specific hydraulic energy under transient conditions.

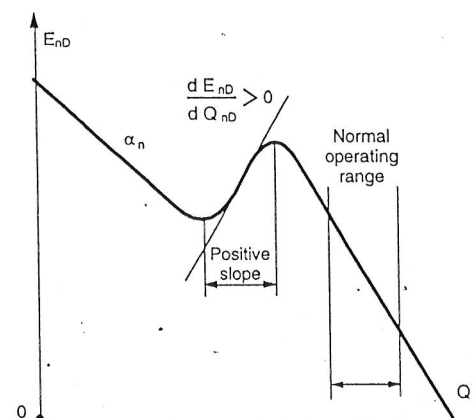


Figure 116 – Pump characteristic with positive slope in a limited discharge range

### 4.7.4.3 Runaway

For this type of testing a reduced specific hydraulic energy is recommended in order to protect the measurement equipment. Also, deviations from a full homology with increased clearances between rotating and stationary parts of the model machine are acceptable for the same reason. Special attention should be paid to the influence of Thoma number  $\sigma$  on the runaway characteristics particularly with high specific speed machines.

#### 7.4.4 Zero-discharge specific hydraulic energy

to keep the discharge exactly zero over the full range of guide vane opening, the test circuit is to be interrupted by e.g. a valve or a blind flange.

Important information at zero-discharge specific hydraulic energy are the power input and also the amplitude and frequency of pressure pulsation, while the runner/impeller is spinning in water.

It can be also of interest to test the power for an impeller spinning in air. The corresponding torques are low, so a high sensitivity torque measuring system is required. Measurements of shaft torque of an impeller spinning in air show increased uncertainties of up to  $\pm 10\%$ . Furthermore, the conversion of test results to the prototype conditions is questionable due to a low Reynolds number in the model and the difference of Froude number.

Another very specific scope of tests consists in measuring the shaft torque of the runner/impeller spinning in air with guide vanes closed but keeping the cooling water fed to the labyrinth seals.

#### 7.4.5 Zero-speed discharge and break-away torque

For this specific test it is necessary to block the model runner shaft. In case of a hydrostatic bearing system the rotating part has to be linked to the swinging system connected with the torque measuring instrument in order to determine the break-away torque. When a torque-meter is used, the rotating shaft has to be blocked against the stationary part of the system.

### 8 Differential pressure measurement in view of prototype index test

#### 8.1 General

When index testing at the prototype machine (in pump or turbine mode) is anticipated, some additional measurements can be performed during model testing. This subclause only deals with index testing using differential pressure as an index value. Index tests in the model can never be a substitute for an absolute discharge measurement at the prototype.

Differential pressure measurement for index testing is made on a well chosen pair of taps showing a significant pressure difference related to local kinetic energy.

Index testing using differential pressure measurement is therefore well represented by the following equation:

$$Q = f(\Delta p) \cdot \Delta p^{0.5}$$

where

a) is the differential pressure measured with a differential manometer or a differential pressure transducer connected between the taps, and

b) is a function of the flow condition, the Reynolds number and the wall roughness.

According to IEC 60041, clause 15, the equation can be written:

$$Q = k \cdot \Delta p^n$$

where  $k$  and  $n$  are constants.

The value of  $n$  is usually taken in the range of 0,48 to 0,52.

#### 4.8.2 Purpose of test

The purposes of additional measurements in the model are:

- to select a proper position of pressure taps giving a significant differential pressure;
- to determine the maximum differential pressure to be expected at the prototype. This information enables a proper selection of instrumentation;
- to check the stability of the differential pressure at the selected pressure taps;
- to verify that the relationship between pressure difference and the discharge is not influenced by other operating parameters (e.g. guide vane opening,  $\eta_{ED}$ , etc.).

The purpose of the tests described is not to establish a calibration curve for an absolute determination of discharge at the prototype.

#### 4.8.3 Execution of test

##### 4.8.3.1 Pressure taps

Depending on the type of machine, different locations of pressure taps can be chosen. Typical examples are given in clause 15 of IEC 60041.

The design of pressure taps shall be in accordance with the requirements stated in subclause 3.3.3.

##### 4.8.3.2 Instrumentation

Differential manometers or differential pressure transducers shall be selected to cover the complete range of expected differential pressure and used within their optimum measuring range.

##### 4.8.3.3 Test procedure

To demonstrate that the chosen pair of pressure taps has been suitably located, the following procedures are recommended:

- vary model discharge by varying guide vane opening while maintaining constant specific hydraulic energy;
- in a second step vary discharge by varying specific hydraulic energy at a constant guide vane opening;
- in case of double regulated machines the same procedure should be repeated for another blade angle in order to enlarge the range of discharge;
- in case of pump operation consistency of results should be checked also at different speed factors rather than by variation of guide vane opening.

It is possible to simultaneously measure these differential pressures and hydraulic performance characteristics.

Suitability of a chosen pair of taps can be assumed if all the readings taken under various conditions of flow form a power function of discharge within a reasonable band.

#### 4. Transposition to prototype conditions

$$Q_P = k_P \cdot (\Delta p)_P^{0,5} \qquad Q_M = k_M \cdot (\Delta p)_M^{0,5}$$

$$k_p = k_M \cdot \frac{D_p^2}{D_M^2}$$

$$(\Delta p)_P = \frac{1}{k_M^2} \cdot \frac{D_M^{4^*}}{D_P^2} \cdot Q_P^2$$

## .5 Uncertainty

an under favorable circumstances, applicable tolerances for prototype fabrication and for operation of pressure taps together with deviations in inflow conditions result in an uncertainty in determination of prototype discharge based on model test results of about  $\pm 5\%$ . Therefore,  $k$  values determined during model tests shall not be used for a determination of solute discharge for contractual purposes.

Annex A (informative)  
Dimensionless terms

Dimensionless terms

Definition in 1.3.3.123<sup>1)</sup>

Relation to other existing definitions

I		II		III						
Clause	Term	Sym- bol	Definition	Relations	Sym- bol	Definition	Relation to term	Sym- bol	Definition	Relation to term
1.3.3.12.1	Speed factor	$n_{ED}$	$\frac{nD}{E_{ED}^{0.5}}$	$= \frac{1}{E_{ED}^{0.5}}$	$n_{11}$	$\frac{nD}{H^{0.5}}$ ( $n$ in $\text{min}^{-1}$ )	$\frac{1}{60g^{0.25}n_{11}}$	$K_u$	$\psi^{-0.5} = \frac{\omega D/2}{\sqrt{2} E_{ED}^{0.5}}$	$\frac{\omega_{ED}}{2\pi}$
1.3.3.12.2	Discharge factor	$Q_{ED}$	$\frac{Q_1}{D^3 E_{ED}^{0.5}}$	$= \frac{Q_{ED}}{E_{ED}^{0.5}}$	$Q_{11}$	$\frac{Q_1}{D^3 H^{0.5}}$ ( $n$ in $\text{min}^{-1}$ )	$\frac{1}{g^{0.25} Q_{11}}$	$K_{cm}$	$\frac{Q_1}{D^3 E_{ED}^{0.5}}$	1
1.3.3.12.3	Torque factor	$T_{ED}$	$\frac{T_m}{\rho D^3 E_{ED}}$	$= \frac{T_{ED}}{E_{ED}}$ $= \frac{Q_{ED}}{E_{ED}}$ (turbine) $= \frac{Q_{ED}}{E_{ED}}$ (pump)	$T_{11}$	$\frac{T_m}{D^3 H}$ ( $T_m$ in kpm)	$\frac{1}{g^{0.25} T_{11}}$	$K_T$	$\frac{T_m}{\rho D^3 E_{ED}}$	1
1.3.3.12.4	Power factor	$P_{ED}$	$\frac{P_m}{\rho D^3 E_{ED}^{1.5}}$	$= \frac{P_m}{\rho D^3 E_{ED}^{1.5}}$ $= \frac{P_{ED}}{E_{ED}^{1.5}}$ (turbine) $= \frac{P_{ED}}{E_{ED}^{1.5}}$ (pump)	$P_{11}$	$\frac{P_m}{D^3 H^{1.5}}$ ( $P$ in kW)	$\frac{1000}{g^{0.75} P_{11}}$	$K_P$	$\frac{P_m}{\rho D^3 E_{ED}^{1.5}}$	1
1.3.3.12.5	Energy coefficient	$E_{ED}$	$\frac{E}{n D^2}$	$= \frac{P_{ED}}{n D^2}$ $= \frac{P_{ED}}{n D^2}$				$\psi$	$\frac{2E}{(\omega D/2)^2}$	$4\pi^2 E_{ED}$
1.3.3.12.6	Discharge coefficient	$Q_{ED}$	$\frac{Q_1}{n D^3}$	$= \frac{Q_{ED}}{n D^3}$				$\varphi$	$\frac{Q_1}{K_u \pi \omega (D/2)^3}$	$2\pi Q_{ED}$
1.3.3.12.7	Torque coefficient	$T_{ED}$	$\frac{T_m}{\rho n^2 D^3}$	$= \frac{T_{ED}}{n^2 D^3}$				$\tau$	$\frac{2T_m}{\rho_1 \pi \omega^2 (D/2)^5}$	$4\pi^2 T_{ED}$
1.3.3.12.8	Power coefficient	$P_{ED}$	$\frac{P_m}{\rho n^3 D^3}$	$= \frac{P_{ED}}{n^3 D^3}$				$\lambda$	$\frac{2P_m}{\rho_1 \pi \omega^3 (D/2)^5}$	$8\pi^3 P_{ED}$
1.3.3.12.9	Thoma number	$\sigma$	$\frac{NPSE}{E}$	$= \frac{P_{ED}}{E}$				$\psi_c$	$\frac{2NPSE}{(\omega D/2)^2}$	
1.3.3.12.10	Cavitation coefficient	$\sigma_D$	$\frac{NPSE}{n^2 D^2}$	$= \frac{NPSE}{n^2 D^2}$				$\psi$	$\frac{\omega Q_1 / n^{0.5}}{(2E)^{0.75}} = \frac{\varphi}{\psi}$	
1.3.3.12.11	Specific speed	$n_{OE}$	$\frac{n Q_{ED}^{0.5}}{E_{ED}^{0.75}}$	$= \frac{n Q_{ED}^{0.5}}{E_{ED}^{0.75}}$	$n_{q2}$	$\frac{n Q_{ED}^{0.5}}{H^{0.75}}$ ( $n$ in $\text{min}^{-1}$ )	$\frac{n_q}{60g^{0.75}}$	$\psi$	$\frac{\omega Q_1^{0.5}}{E_{ED}^{0.75}}$	$\frac{\omega_1}{2\pi}$

<sup>1)</sup> Reference is made to the mechanical power of the runner/impeller, usually measured on the model.

	(in mm)	(in mm)
1) Reference is made to the mechanical power of the runner/impeller, usually measured on the model.		

$$\frac{nP^{0.5}}{m}$$
 is applied for turbines.

# Annex B

(normative)

## Physical properties, data

Table B.1 – Acceleration due to gravity  $g$  ( $\text{m}\cdot\text{s}^{-2}$ )

Latitude $\phi$ °	Altitude above mean sea level $z$ m				
	0	1 000	2 000	3 000	4 000
0	9,780	9,777	9,774	9,771	9,768
5	9,781	9,778	9,775	9,772	9,769
10	9,782	9,779	9,776	9,773	9,770
15	9,784	9,781	9,778	9,775	9,772
20	9,786	9,783	9,780	9,777	9,774
25	9,790	9,787	9,784	9,781	9,778
30	9,793	9,790	9,787	9,784	9,781
35	9,797	9,794	9,791	9,788	9,785
40	9,802	9,799	9,796	9,793	9,790
45	9,806	9,803	9,800	9,797	9,794
50	9,811	9,808	9,805	9,802	9,799
55	9,815	9,812	9,809	9,806	9,803
60	9,819	9,816	9,813	9,810	9,807
65	9,822	9,820	9,817	9,814	9,811
70	9,826	9,823	9,820	9,817	9,814

NOTES

1 Values for  $g$  are given as a function of latitude and altitude.

2 Definition and formula: see 1.3.3.3.1 and 2.5.2.

Table B.2 – Density of distilled water  $\rho_{\text{wd}}$  ( $\text{kg}\cdot\text{m}^{-3}$ )

Temperature $\theta$ °C	Absolute pressure $10^5 \text{ Pa}$							
	1	10	20	30	40	50	60	70
0	999,8	1 000,3	1 000,8	1 001,3	1 001,8	1 002,3	1 002,8	1 003,3
1	999,9	1 000,4	1 000,9	1 001,4	1 001,9	1 002,4	1 002,9	1 003,4
2	1 000,0	1 000,4	1 000,9	1 001,4	1 001,9	1 002,4	1 002,9	1 003,4
3	1 000,0	1 000,4	1 000,9	1 001,4	1 001,9	1 002,4	1 002,9	1 003,4
4	1 000,0	1 000,4	1 000,9	1 001,4	1 001,9	1 002,4	1 002,9	1 003,4
5	999,9	1 000,4	1 000,9	1 001,4	1 001,9	1 002,4	1 002,8	1 003,3
6	999,9	1 000,4	1 000,9	1 001,4	1 001,8	1 002,3	1 002,8	1 003,3
7	999,9	1 000,3	1 000,8	1 001,3	1 001,8	1 002,3	1 002,7	1 003,2
8	999,9	1 000,3	1 000,8	1 001,2	1 001,7	1 002,2	1 002,7	1 003,2
9	999,8	1 000,2	1 000,7	1 001,2	1 001,6	1 002,1	1 002,6	1 003,1
10	999,7	1 000,1	1 000,6	1 001,1	1 001,6	1 002,0	1 002,5	1 003,0
11	999,6	1 000,0	1 000,5	1 001,0	1 001,4	1 001,9	1 002,4	1 002,9
12	999,5	999,9	1 000,4	1 000,9	1 001,3	1 001,8	1 002,3	1 002,7
13	999,4	999,8	1 000,3	1 000,7	1 001,2	1 001,7	1 002,1	1 002,6
14	999,2	999,7	1 000,1	1 000,6	1 001,1	1 001,5	1 002,0	1 002,4
15	999,1	999,5	1 000,0	1 000,4	1 000,9	1 001,4	1 001,8	1 002,3
16	998,9	999,4	999,8	1 000,3	1 000,7	1 001,2	1 001,7	1 002,1
17	998,8	999,2	999,6	1 000,1	1 000,6	1 001,0	1 001,5	1 001,9
18	998,6	999,0	999,5	999,9	1 000,4	1 000,8	1 001,3	1 001,7
19	998,4	998,8	999,3	999,7	1 000,2	1 000,6	1 001,1	1 001,5
20	998,2	998,6	999,1	999,5	1 000,0	1 000,4	1 000,9	1 001,3
21	998,0	998,4	998,9	999,3	999,8	1 000,2	1 000,7	1 001,1
22	997,8	998,2	998,6	999,1	999,5	1 000,0	1 000,4	1 000,9
23	997,5	997,9	998,4	998,8	999,3	999,7	1 000,2	1 000,6
24	997,3	997,7	998,1	998,6	999,0	999,5	999,9	1 000,4
25	997,0	997,4	997,9	998,3	998,8	999,2	999,7	1 000,1
26	996,8	997,2	997,6	998,1	998,5	999,0	999,4	999,9
27	996,5	996,9	997,4	997,8	998,3	998,7	999,1	999,6
28	996,2	996,6	997,1	997,5	998,0	998,4	998,9	999,3
29	995,9	996,3	996,8	997,2	997,7	998,1	998,6	999,0
30	995,7	996,1	996,5	996,9	997,4	997,8	998,3	998,7
31	995,3	995,7	996,2	996,6	997,1	997,5	997,9	998,4
32	995,0	995,4	995,9	996,3	996,8	997,2	997,6	998,1
33	994,7	995,1	995,5	996,0	996,4	996,9	997,3	997,7
34	994,4	994,8	995,2	995,7	996,1	996,5	997,0	997,4
35	994,0	994,4	994,9	995,3	995,8	996,2	996,6	997,1
36	993,7	994,1	994,5	995,0	995,4	995,8	996,3	996,7
37	993,3	993,7	994,2	994,6	995,0	995,5	995,9	996,3
38	993,0	993,4	993,8	994,2	994,7	995,1	995,5	996,0
39	992,6	993,0	993,4	993,9	994,3	994,7	995,2	995,6
40	992,2	992,6	993,1	993,5	993,9	994,4	994,8	995,2

NOTES

1 Values for  $\rho_{\text{wd}}$  are given as a function of temperature  $\theta$  (°C) and absolute pressure  $p_{\text{abs}}$  ( $10^5 \text{ Pa}$ ).

2 Definition and formula: see 1.3.3.3.3 and 2.5.3.1.3.

Table B.2 (continued)

Temperature $\theta$ °C	Absolute pressure $10^5$ Pa							
	80	90	100	110	120	130	140	150
0	1 003,8	1 004,3	1 004,8	1 005,3	1 005,8	1 006,3	1 006,8	1 007,3
1	1 003,9	1 004,3	1 004,8	1 005,3	1 005,8	1 006,3	1 006,8	1 007,3
2	1 003,9	1 004,4	1 004,8	1 005,3	1 005,8	1 006,3	1 006,8	1 007,3
3	1 003,9	1 004,4	1 004,8	1 005,3	1 005,8	1 006,3	1 006,8	1 007,3
4	1 003,8	1 003,4	1 004,8	1 005,3	1 005,8	1 006,3	1 006,8	1 007,3
5	1 003,8	1 004,3	1 004,8	1 005,3	1 005,7	1 006,2	1 006,7	1 007,2
6	1 003,8	1 004,2	1 004,7	1 005,2	1 005,7	1 006,2	1 006,2	1 007,1
7	1 003,7	1 004,2	1 004,7	1 005,1	1 005,6	1 006,1	1 006,5	1 007,0
8	1 003,6	1 004,1	1 004,6	1 005,0	1 005,5	1 006,0	1 006,5	1 006,9
9	1 003,5	1 004,0	1 004,5	1 005,0	1 005,4	1 005,9	1 006,4	1 006,8
10	1 003,4	1 003,9	1 004,4	1 004,8	1 005,3	1 005,8	1 006,2	1 006,7
11	1 003,3	1 003,8	1 004,3	1 004,7	1 005,2	1 005,6	1 006,1	1 006,6
12	1 003,2	1 003,7	1 004,1	1 004,6	1 005,0	1 005,5	1 006,0	1 006,4
13	1 003,1	1 003,5	1 004,0	1 004,4	1 004,9	1 005,4	1 005,8	1 006,3
14	1 002,9	1 003,4	1 003,8	1 004,3	1 004,7	1 005,2	1 005,7	1 006,1
15	1 002,7	1 003,2	1 003,7	1 004,1	1 004,6	1 005,0	1 005,5	1 005,9
16	1 002,6	1 003,0	1 003,5	1 003,9	1 004,4	1 004,8	1 005,3	1 005,8
17	1 002,4	1 002,8	1 003,3	1 003,8	1 004,2	1 004,7	1 005,1	1 005,6
18	1 002,2	1 002,7	1 003,1	1 003,6	1 004,0	1 004,5	1 004,9	1 005,4
19	1 002,0	1 002,4	1 002,9	1 003,3	1 003,8	1 004,2	1 004,7	1 005,1
20	1 001,8	1 002,2	1 002,7	1 003,1	1 003,6	1 004,0	1 004,5	1 004,9
21	1 001,6	1 002,0	1 002,5	1 002,9	1 003,3	1 003,8	1 004,2	1 004,7
22	1 001,3	1 001,8	1 002,2	1 002,7	1 003,1	1 003,5	1 004,0	1 004,4
23	1 001,1	1 001,5	1 002,0	1 002,4	1 002,9	1 003,3	1 003,7	1 004,2
24	1 000,8	1 001,3	1 001,7	1 002,2	1 002,6	1 003,0	1 003,5	1 003,9
25	1 000,6	1 001,0	1 001,5	1 001,9	1 002,3	1 002,8	1 003,2	1 003,7
26	1 000,3	1 000,7	1 001,2	1 001,6	1 002,1	1 002,5	1 002,9	1 003,4
27	1 000,0	1 000,5	1 000,9	1 001,3	1 001,8	1 002,2	1 002,7	1 003,1
28	999,7	1 000,2	1 000,6	1 001,1	1 001,5	1 001,9	1 002,4	1 002,8
29	999,4	999,9	1 000,3	1 000,8	1 001,2	1 001,6	1 002,1	1 002,5
30	999,1	999,6	1 000,0	1 000,4	1 000,9	1 001,3	1 001,7	1 002,2
31	998,8	999,3	999,7	1 000,1	1 000,6	1 001,0	1 001,4	1 001,9
32	998,5	998,9	999,4	999,8	1 000,2	1 000,7	1 001,1	1 001,5
33	998,2	998,6	999,0	999,5	999,9	1 000,3	1 000,8	1 001,2
34	997,8	998,3	998,7	999,1	999,6	1 000,0	1 000,4	1 000,9
35	997,5	997,9	998,4	998,8	999,2	999,7	1 000,1	1 000,5
36	997,1	997,6	998,0	998,4	998,9	999,3	999,7	1 000,2
37	996,8	997,2	997,6	998,1	998,5	998,9	999,4	999,8
38	996,4	996,8	997,3	997,7	998,1	998,6	999,0	999,4
39	996,0	996,5	996,9	997,3	997,8	998,2	998,6	999,0
40	995,7	996,1	996,5	996,9	997,4	997,8	998,2	998,7

Table B.3 - Kinematic viscosity of distilled water  $\nu$  ( $\text{m}^2 \cdot \text{s}^{-1}$ )

Water temperature $\theta$ °C	Kinematic viscosity $\nu$ $\text{m}^2 \cdot \text{s}^{-1}$	Water temperature $\theta$ °C	Kinematic viscosity $\nu$ $\text{m}^2 \cdot \text{s}^{-1}$
0	$1,791 \times 10^{-6}$	21	$0,980 \times 10^{-6}$
1	$1,731 \times 10^{-6}$	22	$0,957 \times 10^{-6}$
2	$1,674 \times 10^{-6}$	23	$0,934 \times 10^{-6}$
3	$1,620 \times 10^{-6}$	24	$0,913 \times 10^{-6}$
4	$1,568 \times 10^{-6}$	25	$0,892 \times 10^{-6}$
5	$1,520 \times 10^{-6}$	26	$0,873 \times 10^{-6}$
6	$1,473 \times 10^{-6}$	27	$0,854 \times 10^{-6}$
7	$1,429 \times 10^{-6}$	28	$0,835 \times 10^{-6}$
8	$1,387 \times 10^{-6}$	29	$0,817 \times 10^{-6}$
9	$1,346 \times 10^{-6}$	30	$0,800 \times 10^{-6}$
10	$1,308 \times 10^{-6}$	31	$0,784 \times 10^{-6}$
11	$1,271 \times 10^{-6}$	32	$0,768 \times 10^{-6}$
12	$1,236 \times 10^{-6}$	33	$0,753 \times 10^{-6}$
13	$1,202 \times 10^{-6}$	34	$0,738 \times 10^{-6}$
14	$1,170 \times 10^{-6}$	35	$0,723 \times 10^{-6}$
15	$1,140 \times 10^{-6}$	36	$0,709 \times 10^{-6}$
16	$1,110 \times 10^{-6}$	37	$0,696 \times 10^{-6}$
17	$1,082 \times 10^{-6}$	38	$0,683 \times 10^{-6}$
18	$1,055 \times 10^{-6}$	39	$0,670 \times 10^{-6}$
19	$1,029 \times 10^{-6}$	40	$0,658 \times 10^{-6}$
20	$1,004 \times 10^{-6}$		

## NOTES

1 Values for  $\nu$  are given as a function of water temperature  $\theta$  (°C) at absolute pressure  $p_{\text{abs}} = 10^5$  Pa.

2 Definition and formula: see 1.3.3.3.6 and 2.5.3.3.

Table B.4 – Vapour pressure of distilled water  $p_{va}$  (Pa)

Temperature $\theta$ °C	Vapour pressure $p_{va}$ Pa	Temperature $\theta$ °C	Vapour pressure $p_{va}$ Pa
0	611		
1	657	21	2 488
2	706	22	2 645
3	758	23	2 810
4	814	24	2 985
5	873	25	3 169
6	935	26	3 363
7	1 002	27	3 567
8	1 073	28	3 782
9	1 148	29	4 008
10	1 228	30	4 246
11	1 313	31	4 495
12	1 403	32	4 758
13	1 498	33	5 034
14	1 599	34	5 323
15	1 706	35	5 627
16	1 819	36	5 945
17	1 938	37	6 280
18	2 064	38	6 630
19	2 198	39	6 997
20	2 339	40	7 381

NOTES:

1 Values for  $p_{va}$  are given as a function of water temperature  $\theta$  (°C).

2 Definition and formula: see 1.3.3.3.4 and 2.5.3.4.

Table B.5 – Density of dry air  $\rho_a$  ( $\text{kg} \cdot \text{m}^{-3}$ )

Air temperature $\theta_a$ (°C)	Density of dry air $\rho_a$ ( $\text{kg} \cdot \text{m}^{-3}$ )
0	1,293
2	1,284
4	1,274
6	1,265
8	1,256
10	1,247
12	1,238
14	1,230
16	1,221
18	1,213
20	1,205
22	1,196
24	1,188
26	1,180
28	1,173
30	1,165

NOTES

1 Values are given as a function of air temperature  $\theta_a$  (°C) at absolute ambient pressure  $p_{\text{amb},0} = 101\,325$  Pa.

2 Definition and formula: see 1.3.3.3.3 and 2.5.4.1.

Table B.6 – Ambient pressure  $p_{amb}$  (Pa)

Elevation $z$ m	Ambient pressure $p_{amb}$ Pa	Elevation $z$ m	Ambient pressure $p_{amb}$ Pa
0	101 325		
100	100 129	2 100	78 520
200	98 945	2 200	77 548
300	97 773	2 300	76 586
400	96 611	2 400	75 634
500	95 461	2 500	74 692
600	94 322	2 600	73 759
700	93 194	2 700	72 835
800	92 076	2 800	71 921
900	90 970	2 900	71 017
1 000	89 876	3 000	70 121
1 100	88 792	3 100	69 235
1 200	87 718	3 200	68 358
1 300	86 655	3 300	67 490
1 400	85 602	3 400	66 631
1 500	84 560	3 500	65 780
1 600	83 528	3 600	64 939
1 700	82 506	3 700	64 106
1 800	81 494	3 800	63 283
1 900	80 493	3 900	62 467
2 000	79 501	4 000	61 660

NOTES

1 Values are given as a function of elevation  $z$  (m).

2 Definition and formula: see 1.3.3.5.2 and 2.5.4.2.

Table B.7 – Density of mercury  $\rho_{Hg}$  ( $\text{kg}\cdot\text{m}^{-3}$ )

Temperature $\theta$ °C	Density $\rho_{Hg}$ $\text{kg}\cdot\text{m}^{-3}$	Temperature $\theta$ °C	Density $\rho_{Hg}$ $\text{kg}\cdot\text{m}^{-3}$
0	13 595	21	13 543
1	13 593	22	13 541
2	13 590	23	13 538
3	13 588	24	13 536
4	13 585	25	13 534
5	13 583	26	13 531
6	13 580	27	13 529
7	13 578	28	13 526
8	13 575	29	13 524
9	13 573	30	13 521
10	13 570	31	13 519
11	13 568	32	13 516
12	13 565	33	13 514
13	13 563	34	13 511
14	13 561	35	13 509
15	13 558	36	13 507
16	13 556	37	13 504
17	13 553	38	13 502
18	13 551	39	13 499
19	13 548	40	13 497
20	13 546		

NOTES

1 Values are given as a function of temperature  $\theta$  (°C) at absolute ambient pressure  $p_{amb-0} = 101\,325$  Pa (standard ambient pressure at sea level).

2 Definition and formula: see 1.3.3.3.3 and 2.5.5.

### Annex C (informative)

## Derivation of the equation for the specific hydraulic energy of a machine

### 1 Theoretical equation

The energy balance within the inner boundaries of a hydraulic machine is given by the Bernoulli equation in its differential form, supplemented by the energy loss term:

$$\frac{dp_{abs}}{\rho} + d\left(\frac{v^2}{2}\right) + g dz + de_L + de = 0$$

where

$\frac{dp_{abs}}{\rho}$  is the change of specific pressure energy;

$d\left(\frac{v^2}{2}\right)$  is the change of specific kinetic energy;

$g dz$  is the change of specific potential energy;

$de_L$  is the specific dissipated energy;

$de$  is the specific energy exchanged between the water and the runner/impeller (de < 0 for a turbine, de > 0 for a pump).

For an ideal machine without losses ( $de_L = 0$ ), the specific hydraulic energy  $E$  of the water which is available between the high and low pressure reference sections 1 and 2 of the machine is obtained by integration between these two sections:

$$\int_2^1 de = \int_2^1 \frac{dp_{abs}}{\rho} + \int_2^1 d\left(\frac{v^2}{2}\right) + \int_2^1 g dz \quad (C.1)$$

### 2 Specific pressure energy term

may be written:

$$\int_2^1 \frac{dp_{abs}}{\rho} = \frac{p_{abs1} - p_{abs2}}{\rho^*}$$

Taking into account the scope of this standard,  $\rho^*$  may be defined by the approximation:

$$\rho^* = \bar{\rho} = \frac{1}{2}(\rho_1 + \rho_2)$$

The relative error introduced by this approximation is less than  $2 \times 10^{-4}$ .

### C.3 Specific kinetic energy term

The value of the specific kinetic energy term in a streamline of the flow and its mean value in a cross-section ( $e_c = v^2/2$ ) are defined in note 1 of 3.5.2.4.

By convention, it is assumed that the change in specific kinetic energy is given by:

$$\int_2^1 d\left(\frac{v^2}{2}\right) = \frac{1}{2}(v_1^2 - v_2^2)$$

where  $v_1$  and  $v_2$  are the mean axial velocities (see 1.3.3.4.9) in the reference sections 1 and 2. (Strictly speaking, the tangential and radial components of the velocities should be taken into account.)

### C.4 Specific potential energy term

Since the change in gravitational acceleration with elevation between the reference sections 1 and 2 is small, it may be written:

$$\int_2^1 g dz = \bar{g}(z_1 - z_2)$$

where  $\bar{g} = \frac{1}{2}(g_1 + g_2)$

### C.5 Practical equation

With the above simplifications, equation (C.1) defining the specific hydraulic energy of the machine (see 1.3.3.6.2) becomes:

$$E = \frac{1}{\bar{\rho}}(p_{abs1} - p_{abs2}) + \frac{1}{2}(v_1^2 - v_2^2) + \bar{g}(z_1 - z_2)$$

In practice, the value of  $g$  at the reference level of the machine may be taken as  $\bar{g}$ . Furthermore, for low head machines,  $(p_1 - p_2) < 4 \times 10^5$  Pa for instance, the value of  $\rho$  at the low pressure reference section may be taken as  $\bar{\rho}$ .

## Annex D (informative)

### Influence of the density of actual water $\rho_{wa}$ on measurement and calibration

ie to chemically dissolved components, the density of actual test water  $\rho_{wa}$  (see 3.5.2.3 and 5.3.1.2) will always be higher than the density of distilled water  $\rho_{wd}$ , as given in 2.5.3.1.3 and 3.5.1.2. The deviation in general is less than 0,05 %.

the specific hydraulic energy  $E$  is determined primarily by pressure measurements and if the measuring instruments are mounted at approximately the same elevation,  $E$  can be expressed

$$E = \frac{p_1 - p_2}{\bar{\rho}} + \frac{v_1^2 - v_2^2}{2}$$

the hydraulic power becomes:

$$P_h = \left[ \frac{p_1 - p_2}{\bar{\rho}} + \frac{v_1^2 - v_2^2}{2} \right] \cdot \rho_1 \cdot Q_1$$

$$= \left[ p_1 - p_2 + \bar{\rho} \cdot \frac{v_1^2 - v_2^2}{2} \right] \cdot \frac{\rho_1}{\bar{\rho}} \cdot Q_1$$

here  $\rho_1 = \rho_{wa,1}$  and  $\bar{\rho} = \bar{\rho}_{wa}$ .

in practice, it may be assumed that in the model testing installation  $\rho_{wa}$  differs little from  $\rho_{wd}$  and that both vary with temperature and pressure in a similar manner:

$$\frac{\rho_{wa,1}}{\bar{\rho}_{wa}} = \frac{\rho_{wd,1}}{\bar{\rho}_{wd}} = \frac{\rho_1}{\bar{\rho}}$$

is completely justified to apply  $\bar{\rho}_{wd}$  in term  $\bar{\rho}_{wa} \frac{v_1^2 - v_2^2}{2}$  because  $\frac{v_1^2 - v_2^2}{2}$  will always be less than 10 % of the pressure energy term, even for high specific speed machines. Thus the error on  $E$  or  $\eta$  when applying the density of distilled water will always be less than 0,005 %. Therefore a good approximation for hydraulic power is:

$$P_h = \left[ p_1 - p_2 + \bar{\rho}_{wd} \frac{v_1^2 - v_2^2}{2} \right] \cdot \frac{\rho_{wd,1}}{\bar{\rho}_{wd}} \cdot Q_1$$

## Annex E (informative)

### Summarized test and calculation procedure

#### E.1 Premise

Annex E contains a list of agreements, checks and operations to be carried out before, during and after the tests.

Also the main aspects of a test point calculation, together with all the information necessary to make a comparison with the guarantees, including the evaluation of the measurement uncertainties are summarized below.

For each point, reference is made to the applicable subclauses of this standard.

#### E.2 Agreements to be reached prior to testing

Agreement between the parties shall be reached, in due time before the test, on:

- the model size (2.3.2.2) and the scale ratio  $\lambda$  (1.3.3.2.9);
- the model structural characteristics (2.1.3.2);
- similitude requirements (2.3.1);
- the test conditions (2.3.2.1);
- the values of  $Re_M$  or  $Re_{sp}$  (1.4.1.4) when the guarantees refer to the model (3.8.2.2), (for Pelton turbine, the value of Froude number, 2.3.1.5.2);
- the extent of the model (2.1.3.3);
- the reference sections (1.4.1.1);
- the pressure measuring sections (3.3.2 and 3.5.2.1) and the areas for the calculation of specific hydraulic energy (3.5.2) and net positive suction specific energy (3.5.4);
- the guaranteed values of power, discharge, efficiency, steady-state runaway speed and influence of cavitation on hydraulic performance (1.4.2);
- the  $\sigma_{PI}$  values (1.4.2.1.5);
- the cavitation test procedure (2.3.3.3.6 and 3.8.2.3.7) and the cavitation reference level (2.3.1.5.1);
- the injection of cavitation nuclei (2.1.2.3, 2.3.1.6.2 and 2.5.3.2) in the circuit water, if necessary;
- all other specifications for the model tests (2.3.3.1.1);
- the time schedule of the tests (2.3.3.1.2);
- the personnel and responsibilities (2.3.3.1.3);
- the type and extent of the tests to be performed (2.3.3.3);
- the calibration procedure for the instruments to be utilized (2.3.3.1.5);
- $g_P$  prototype value of gravitational acceleration (2.5.2);
- $\theta_P$  prototype water temperature and corresponding kinetic viscosity  $\nu_P$  (2.5.3.3);
- $\rho_P$  prototype water density (2.5.3.1);

$n_p$  steady-state prototype speed;  
 $Re_p$  steady-state Reynolds number of prototype;  
 $NPSE_p$  range of prototype operation (1.4.2.1.5);  
 $E_{pmax}$  maximum specific hydraulic energy applied to runaway condition (1.4.2.1.4);  
 mechanical power losses of the prototype (1.4.2.1.1 and 2.4.1.4);  
 electrical machine windage losses (annex G).

## Model, test facility and instrumentation

### 1 Model manufacture and dimensional checks

model shall be manufactured according to 2.1.3.2 and subjected to the dimensional checks outlined in 2.2 and 2.3.3.1.6. Particular attention shall be paid to:

the value of the reference diameter (1.3.3.2.6);  
 checking the runner/impeller seal clearances (2.2.2.1.6 and 2.3.3.2.1);  
 the roughness or surface quality of wetted surfaces (2.2.3).

### 2 Test facility instrumentation and data acquisition system

test stand and the complete circuit shall be carefully checked (2.3.3.2.2) before and during tests, paying particular attention to the condition of the gauge piping for any leakage.

instrumentation and the data acquisition system shall also be carefully checked and calibrated before and after the tests (2.3.3.2.3).

following is usually verified by means of specific operation tests:

the regularity of the pressure at the taps of the model inlet and outlet sections (3.3.3.1);  
 the proper response of the instrumentation at the same operating point tested under different test conditions (2.3.3.3.1).

## 4 Tests and calculation of the model values

usually, a complete preparatory test and preliminary test are carried out by, or in the presence of the manufacturer to verify all the guarantees prescribed in the contract and to define the role operating behaviour of the machine. The acceptance tests, witnessed by all the parties involved, are subsequently carried out (2.3.3.3.1).

### 4.1 Measurement of the main quantities during the test

for each test point, the average values of the readings of the instruments measuring the quantities listed below shall be obtained. Measurements are made in accordance with 3.1 and 3.2.1:

discharge (3.2);  
 pressure at the high pressure and low pressure measuring sections (or alternatively differential pressure between sections 1 and 2 and suction pressure at section 2) (3.3, 3.4, 3.5);  
 torque (3.6);  
 rotational speed (3.7);  
 test circuit water temperature;

– ambient temperature;  
 – instrument temperature;  
 – ambient pressure.

The calibrations of all the measurement instruments shall be made available and checked (2.3.3.1.5).

The value of the constants necessary for the calculation [for example:  $g$  (2.5.2),  $\rho$  (2.5.3.1),  $z_c$  (2.3.1.5.1),  $p_{va}$  (2.5.3.4),  $v$  (2.5.3.3), length of levers (3.6.2.1),  $T_{Lm}$  (3.6.5.3)] shall be known or calculated for the conditions of the tests.

### E.4.2 Total uncertainty

#### E.4.2.1 Systematic uncertainty of the measured quantities

The values of the systematic uncertainty necessary to determine the uncertainty band shall be fixed and agreed upon for each quantity (3.9.2.2.2 and annex J).

#### E.4.2.2 Random uncertainty of the measured quantities

The value of the random uncertainty shall be calculated from a test either near the maximum efficiency or, where necessary, at partial load (2.3.2.3.1, 3.9.2.2.1 and annex L).

#### E.4.2.3 Total uncertainty

The total uncertainty is the combination of the above systematic and random uncertainties and defines the uncertainty band of the curves used for the comparison to guarantees (3.9.2.2.4 and 3.10.2).

### E.4.3 Calculation of the quantities related to the main hydraulic performance

Using the constants and the measurements listed, and using the calibration data and the relations given in 2.4.1.1 for the hydraulic efficiency calculation, the values of  $\rho_M$ ,  $Q_M$ ,  $E_M$ ,  $P_{mM}$ ,  $\eta_{hM}$ ,  $NPSE_M$  and  $Re_M$  are calculated.

### E.4.4 Calculation of the dimensionless factors or coefficients and of the Thoma number

Using the relations of 1.3.3.12, the values of  $Q_{nD}$ ,  $E_{nD}$ ,  $P_{nD}$  and  $\sigma_{nD}$  and/or of  $Q_{ED}$ ,  $\eta_{ED}$ ,  $P_{ED}$  and  $\sigma$  may be calculated.

### E.4.5 Determination of $\delta_{ref}$ for the scale effect calculation

By specific tests, the value of  $\eta_{hM opt}$  and the value of  $Re_{M opt}$  at which it is measured shall be determined. From these, the value  $\delta_{ref}$  to be used in the formulae of 3.8.2.2 for the efficiency scale-up calculation may be determined by the formula given in the same subclause (see also annex F).

### E.4.6 Calculation of efficiency and power coefficients referred to $Re_M$

This calculation procedure may be applied as an alternative to the others described in the flow chart of figure 62. Values of  $\eta_{hM}$ ,  $P_{nD}$  and  $P_{ED}$  (3.8.2.2.3) may be calculated and then all the operation curves of the model referred to  $Re_M$  (3.8.2.2 and 3.8.2.2.3) can be obtained.

When the guarantee is given for model efficiency referred to a specified value  $Re_{Msp}$ ,  $Re_M$  may be chosen equal to  $Re_{Msp}$  (1.4.1.4 and 3.8.3.3.5).

### 1.7 Correction of the model-measured values taking into account the influence of cavitation

For the efficiency tests, see 2.3.3.3.5 and 3.8.2.3.7.

For the runaway tests, see 2.3.3.3.7 and 3.8.3.2.

## 5 Calculation of prototype quantities

Refer to the flow chart of figure 62.

Based on 3.8.2.4 and 3.8.2.5 for steady-state operation at a specified  $n_p$ , the values of  $Q_p$ ,  $E_p$ ,  $P_p$ ,  $NPSE_p$  and  $\eta_{hp}$  are obtained taking into account the efficiency scale-up  $(\Delta\eta_h)_{M \rightarrow P}$  and the influence of cavitation (3.8.2.4.2).

The efficiency  $\eta_p$  and the mechanical power  $P_p$  of the prototype machine shall be calculated taking into account the mechanical power losses of the prototype (1.3.3.8.4, 1.4.2.1.1 and 0.3.4) and the electrical machine windage losses (see annex G).

For runaway operation, see 3.8.3.3 and 3.8.3.4 for calculating  $\eta_{R,P}$ ,  $Q_{R,P}$  and  $NPSE_p$ . The influence of cavitation on steady-state runaway speed is considered in 3.8.3.2.

## 6 Plotting of model or prototype results

The points and/or curves of model or prototype results are plotted on the basis of a proper number of test points (3.8.2.3 and 3.10.2) after having removed any spurious point (see 3.1.3.1). If an interpolation curve is necessary, an example of its determination is given in annex H.

The above points or curves are plotted with the uncertainty band where necessary (3.10.2) for comparison with guarantees.

## 7 Comparison with the guarantees

The fulfilment of the guarantees will be established as outlined in 3.10.3.1, 3.10.3.2 and 3.10.3.3.

For the application of penalties and premiums, if any, see 3.10.3.5.

## 8 Final protocol

The final protocol, completed by the daily log and the test results documents, duly signed, shall be drawn up at the end of the acceptance tests (2.3.3.3.9) and, once signed by all the involved parties, it closes the acceptance model tests. All guarantees which were checked for compliance shall be mentioned and the protocol shall clearly state if the guarantee, for each as met or not.

## 9 Final test report

The final test report (2.3.3.5) shall contain all the documents pertaining to the official tests and shall be completed after the tests within a time mutually agreed (normally two months).

## Annex F (normative)

### Scale-up of the hydraulic efficiency of reaction machines

#### F.1 Basic statements and assumptions

Statements and formulae given in this annex are valid only for reaction machines<sup>1)</sup> (for Pelton turbines, see annex K). The scale-up of hydraulic efficiency of reaction machines is based on the dependence of friction losses on Reynolds number  $Re$ .

Scale-up in this standard applies only to efficiency and mechanical power of runner/impeller, not to discharge or specific hydraulic energy. The applied method of evaluation is based on the assumption that wetted surfaces are hydraulically smooth and no influence of roughness or other effects is taken into account<sup>2)</sup>.

In the scale-up formula (see F.3) the exponent of the scalable losses curve (0,16) and the ratio of scalable losses to total losses ( $V_{rel}$ ) are average experimentally based values derived from:

- a) model tests at different Reynolds numbers on models with hydraulically smooth surfaces;
- b) comparison of efficiency tests on models and homologous prototypes, having a surface roughness according to 2.2. The surface roughness is not greatly affected by cavitation and does not necessarily yield hydraulically smooth flow conditions.

As long as the deviations in geometric similarity of clearances are within the limits specified in 2.2.2.1.6 (see also 2.2.2.1.7 and 2.2.2.2.5), it is assumed that the formula for hydraulic efficiency scale-up given below remains valid.

It is conventionally agreed to calculate the hydraulic efficiency increase  $\Delta\eta_h$  at the point of maximum model hydraulic efficiency and to apply this value over the whole range of guaranteed efficiencies provided the hydraulic efficiency is not greatly affected by cavitation (see 3.8.2.4.2). The optimum hydraulic efficiency should not be affected by cavitation.

<sup>1)</sup> For reaction machines of special design, see table 7, note 1 of 3.8.2.2.1.

<sup>2)</sup> Although various procedures on how to consider the scale effects on specific hydraulic energy and discharge or the roughness effects have been presented, there is yet no commonly accepted basis to quantify these effects. For more information, see references in F.5.

## 2 Amount of relative scalable losses in the range of guaranteed efficiencies

For a given hydraulic turbomachine, the amount of relative scalable losses  $\delta$  as a function of Reynolds number  $Re$  is the same over the range  $R$  of guaranteed efficiencies (range  $R$  is shown schematically in figure F.1).

This means that for a given constant Reynolds number, for example  $Re_M$ , the amount of relative scalable losses  $\delta$  is constant for each operating point within the whole range  $R$ , whereas the amount of non-scalable losses  $\delta_{ns}$  depends on the amount of the relative total loss  $(1 - \eta_h)$  of the operating point.

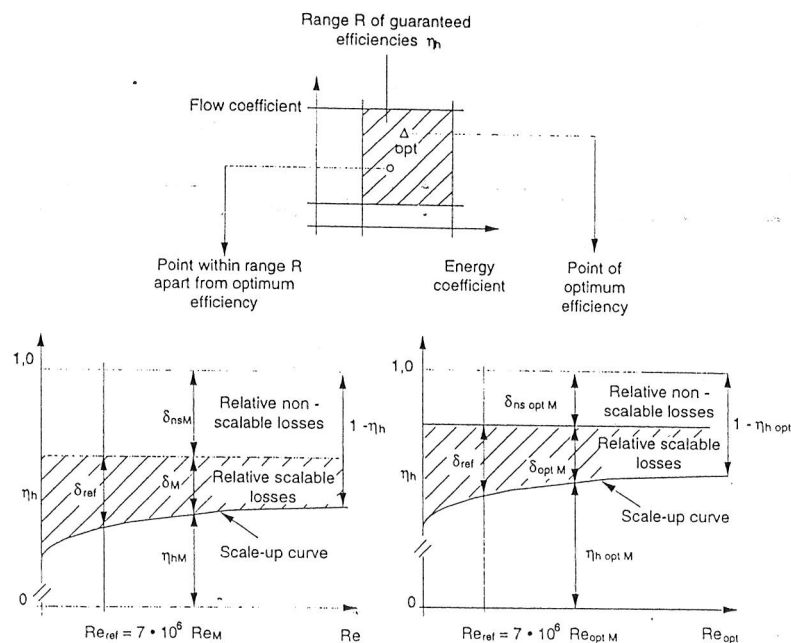


Figure F.1 – Variation of relative scalable losses

## F.3 Derivation of the general scale formula

Two points A and B representing hydraulically similar operating conditions according to the assumptions in 2.3.1.2 are shown in figure F.2.

The relative scalable losses for the Reynolds numbers  $Re_{ref}$ ,  $Re_A$  and  $Re_B$  (see figure F.2) are related as follows:

$$\frac{\delta_A}{\delta_{ref}} = \left( \frac{Re_{ref}}{Re_A} \right)^{0,16}$$

$$\frac{\delta_B}{\delta_{ref}} = \left( \frac{Re_{ref}}{Re_B} \right)^{0,16}$$

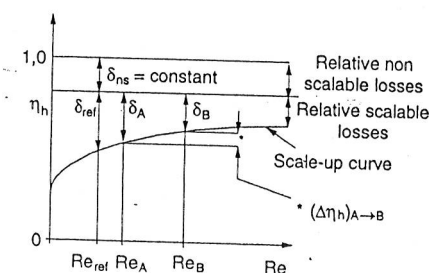


Figure F.2 – Efficiency change in hydraulically similar operating conditions A and B having different  $Re$  values

Using

$$(\Delta\eta_h)_{A \rightarrow B} = \delta_A - \delta_B$$

the following general scale formula is obtained:

$$(\Delta\eta_h)_{A \rightarrow B} = \delta_{ref} \left[ \left( \frac{Re_{ref}}{Re_A} \right)^{0,16} - \left( \frac{Re_{ref}}{Re_B} \right)^{0,16} \right]$$

of which the formulae quoted in 3.8.2.2 and 3.8.2.4.1 are particular cases.

Using the assumptions of F.1 and 3.8.2.2 for the point of optimum efficiency, the following three equations result:

$$\frac{\delta_{opt M}}{\delta_{ref}} = \left( \frac{Re_{ref}}{Re_{opt M}} \right)^{0,16}$$

$$V_{ref} = \frac{\delta_{ref}}{\delta_{ref} + \delta_{ns opt M}}$$

$$\delta_{opt M} + \delta_{ns opt M} = 1 - \eta_{h opt M}$$

three unknown values are:

$\delta_{opt M}$ : relative scalable losses at the point of optimum efficiency

$\delta_{ref}$ : relative non-scalable losses at the point of optimum efficiency

$\delta_{ref}$ : relative scalable losses at the point  $Re_{ref}$  with  $\delta_{ref} = (1 - \eta_{href}) \cdot V_{ref}$

The result is the equation given in 3.8.2.2:

$$\delta_{ref} = \frac{1 - \eta_{hopt M}}{\left( \frac{Re_{ref}}{Re_{opt M}} \right)^{0.16} + \frac{1 - V_{ref}}{V_{ref}}}$$

#### 4 Determination of efficiency increase from model to prototype

For the following it is assumed that the Reynolds number of the prototype machine  $Re_P$  has a constant value within the range of guarantee and that the value  $\delta_{ref}$  has been determined according to 3.8.2.2.1.

When the model efficiencies have been referred to a constant Reynolds number  $Re_{M^*}$ , the following formula is applied to calculate the resulting efficiency increase  $(\Delta\eta_h)_{M^* \rightarrow P}$ . Within the whole range of guarantee only one constant numerical value is considered.

$$(\Delta\eta_h)_{M^* \rightarrow P} = \delta_{ref} \left[ \left( \frac{Re_{ref}}{Re_{M^*}} \right)^{0.16} - \left( \frac{Re_{ref}}{Re_P} \right)^{0.16} \right]$$

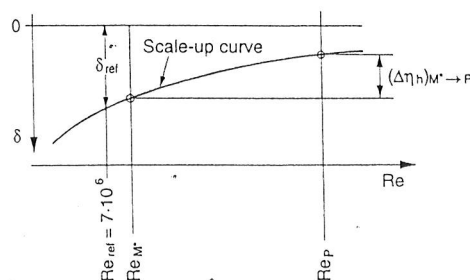


Figure F.3 – Efficiency scale-up from constant  $Re_M$  to constant  $Re_P$

When the model efficiencies have been measured at different Reynolds numbers  $Re_M$ , the following formula is used to calculate the resulting values of efficiency increase  $(\Delta\eta_h)_{M_i \rightarrow P}$  for each value  $Re_M$ . Within the whole range of guarantee more than one numerical value is considered.

$$(\Delta\eta_h)_{M_i \rightarrow P} = \delta_{ref} \left[ \left( \frac{Re_{ref}}{Re_{M_i}} \right)^{0.16} - \left( \frac{Re_{ref}}{Re_P} \right)^{0.16} \right]$$

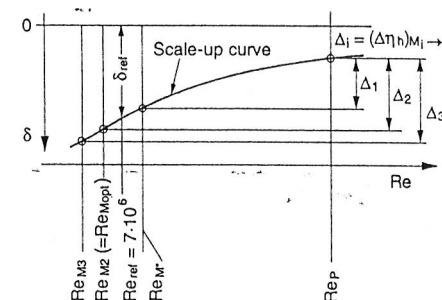


Figure F.4 – Efficiency scale-up from variable  $Re_M$  to constant  $Re_P$

#### F.5 Bibliography

- F.5.1 Osterwalder, J., "Efficiency scale-up for hydraulic turbomachines with due consideration of surface roughness", *Journal of Hydraulic Research* 16 (1978) No. 1, pp. 55 to 76.
- F.5.2 Ida, T., *Recent research of scale effects on performance characteristics of hydraulic turbomachines*, Kanagawa University, Yokohama, April 1983.
- F.5.3 Osterwalder, J., Hippe L., "Guidelines for efficiency scaling process of hydraulic turbomachines with different technical roughness of flow passages", *Journal of Hydraulic Research* 22 (1984), No. 2, pp. 77 to 102.
- F.5.4 Ida, T., "Scale effects of water turbine performances considering only surface roughness", *Proceedings from 14th Symposium IAHR* 1988, pp. 813 to 824.
- F.5.5 Henry, P., Leroux, A., Levesque, J.M., Miron, J.G., "Performance of the LG-4 turbines", *Proceedings from 14th Symposium IAHR* 1988, pp. 787 to 799.
- F.5.6 Ida, T., "New formula for efficiency step-up of hydraulic turbine", *Proceedings from 17th Symposium IAHR* 1994, pp. 827 to 840.
- F.5.7 Nichtawitz, A., "Discussion on step-up procedures in hydraulic machines", *Proceedings from 17th Symposium IAHR* 1994, pp. 841 to 852.
- F.5.8 Spurk, J.H., Grein, H., "Performance conversion method for hydraulic turbines and pumps", *Water Power & Dam Construction*, (1993-11), pp. 42-49.
- F.5.9 Fay, Á.Á., "On the accuracy of hydro turbine performance prediction based on model tests", *Modelling, Testing & Monitoring for Hydro Powerplants*, Budapest, Hungary, July 1994, pp. 425-434.

## Annex G (normative)

### Computation of the prototype runaway characteristics taking into account friction and windage losses of the unit

The prototype maximum runaway speed and discharge computed from the model tests according to 3.8.3.3 shall be corrected for the friction losses of the unit bearings and shaft seal and the windage losses of the electrical machine, which determine a decrease of the maximum runaway speed from  $n_{Rmax,P}$  to  $n'_{Rmax,P}$ .

The procedure is the following:

Using the measured points  $X_1, X_2, X_3$ , etc. at constant guide vane opening or needle stroke in a range near to runaway, plot the curve  $P_{mP}(n_P)$  for a single-regulated turbine (see figure G.1). If the chosen opening corresponds to the maximum runaway speed ( $\alpha = \alpha_{max}$  usually for Francis turbine), the intersection point Y of the curve  $P_{mP}(n_P)$  with the curve  $(P_{Lm} + P_W)(n_P)$ , representing the sum of the bearing and shaft seal friction losses of the unit and of the electrical machine windage losses<sup>1)</sup>, is at the maximum steady-state runaway speed  $n'_{Rmax,P}$  expected for the unit.

For a double-regulated turbine, the procedure described above should be applied for each inner blade angle; the highest maximum value of  $n'_{R,P}$  may then be determined.

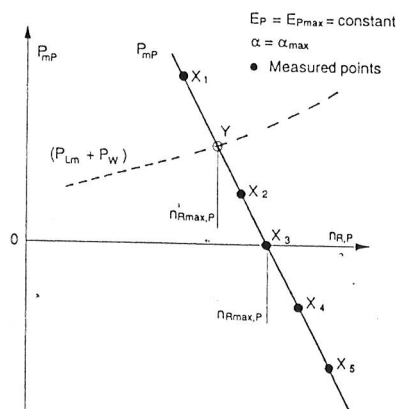


Figure G.1 – Single-regulated turbine. Determination of the maximum runaway speed of the prototype taking into account the friction and windage losses of the unit

<sup>1)</sup> For the determination of these losses, see IEC 60041.

## Annex H (informative)

### Example of determination of the best smooth curve: method of separate segments

#### H.1 Premise

In model testing, unlike prototype testing, a large number of operating points are generally measured and sometimes, a measurement point is repeated very close to a previous one. Furthermore, the test range generally extends above and below the guaranteed range, but the measurement points are concentrated within the range of guarantees.

In such a case, the classical least squares method, based on a single function, may not be appropriate to determine the best fitted curve passing through the points: if the polynomial degree increases, the curve passes closer to the points but can deviate, sometimes notably, from the regular expected shape. As the mathematical form of the law expressing the physical phenomenon is in most cases unknown, a more convenient way to determine by computation the best fitted curve is to arbitrarily split the test range into segments. It is then possible to apply the least squares method to each segment using low degree polynomials which lead to reasonably smooth curves.

Several computerized methods of drawing the interpolation curves are available. There are methods based on:

- normal spline functions;
- B-splines;
- representation of surfaces.

As an example, a modified least squares method is described below.

NOTE – The measurement methods applied today result in relatively small random uncertainty. Therefore, the smoothing process can normally be restricted to averaging measurements at several points around a given operating point.

#### H.2 Principle of the method

A series of intervals along the abscissa are determined as described below. Three adjacent intervals (1, 2, 3 in figure H.1) form the range in which the least squares method is applied, but only the central segment 2 of the curve is directly defined by this way. The procedure is then repeated by shifting by two steps, left and right, in order to obtain a series of separate segments (a in figure H.2). The remaining intervals are then filled with segments of curve (b in figure H.2) passing through the extreme points of segments a with the same slope at these points. The two extreme segments at the ends of the test range are drawn directly by the least squares method (c in figure H.2), using the same numerical coefficients of the polynomials as in the corresponding adjacent segment.

A degree of 3 is assumed, as a rule, for the polynomials in segments of both types, a and b. Depending on the arrangement of the points and on the width of the intervals, it may happen that there are only sufficient points to define a group of two intervals, not three, at the end of the test range where the least squares methods should be applied. In this case, the polynomial is reduced to degree 2.

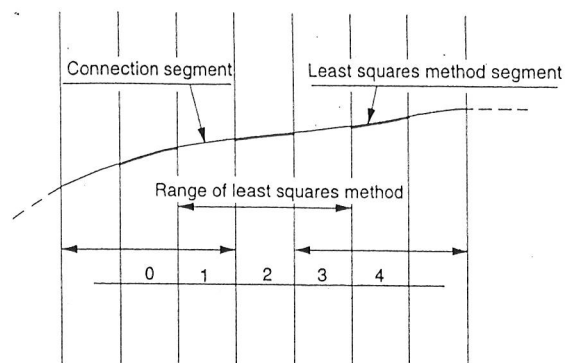


Figure H.1 – Principle of the method of separate segments

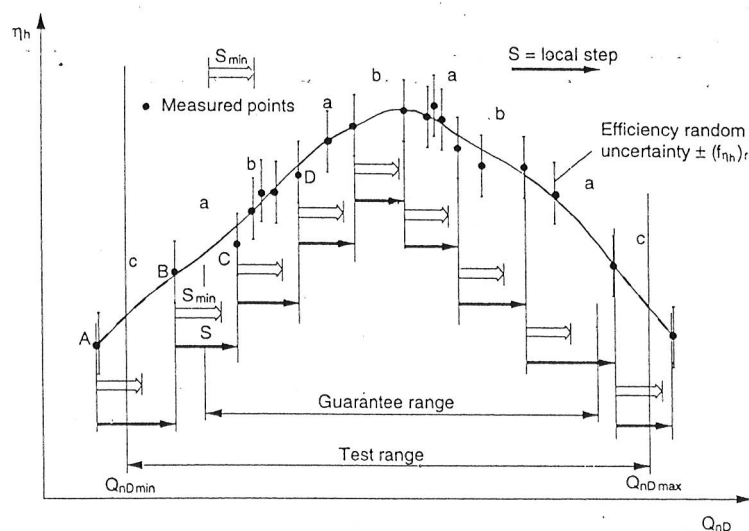


Figure H.2 – Example of determination of intervals

### H.3 Choice of the minimum width of the intervals

A value  $s_{\min}$  of the minimum width of the intervals shall be assumed. The most convenient value is small enough to give a good definition of the interpolation curve. Attention shall be drawn to the fact that the choice of  $s_{\min}$ , and thus of the number of intervals, influences the shape of the curve:

- choosing too large a  $s_{\min}$  value may result in an oversmoothed curve, which may not represent the actual physical phenomenon;
- choosing too small a  $s_{\min}$  value may result in a curve reflecting the random scatter of measurement points rather than the physical reality.

Therefore, the choice of an appropriate  $s_{\min}$  value shall be left to the judgement of the user, taking into account that the interpolation curve shall, as far as possible, consist of segments denoting the random uncertainty in each measurement point (see figure H.2).

For example, when drawing the efficiency curve  $\eta_h(Q_{nD})$  of a single-regulated turbine (see 3.8.2.3.1),  $s_{\min}$  may normally be chosen equal to approximately  $(Q_{nD\max} - Q_{nD\min})/10$ .  $Q_{nD\min}$  and  $Q_{nD\max}$  are the limiting values of the test range.

### H.4 Determination of the intervals

To simplify the statement below, it is assumed that the process starts from the left end of the test range, even if in the case of an efficiency curve it may be convenient to start from the centre of the range.

From the first measurement point considered, two cases can occur:

- the next point lies at a distance along the abscissa greater than or equal to  $s_{\min}$ : the interval  $s$  is then defined by these two points (A and B in figure H.2);
- the next point lies at a distance along the abscissa less than  $s_{\min}$ : proceeding towards the right side, the first measurement point lying at a distance from the starting point greater than  $s_{\min}$  shall then be sought; this point, together with the starting point, defines the interval  $s$  of the local interval (C and D in figure H.2).

This procedure proceeds to the end of the test range. For the least squares method with a degree polynomial being applicable, each group of three adjacent intervals shall contain at least four measurement points.

## Annex J (informative)

### Examples of analysis of sources of error and uncertainty evaluation

This annex may be used as a guide for analyzing sources of errors which may occur during the tests (see table 8 in 3.9.2.1). It contains the following three examples:

example of analysis of sources of error and of uncertainty evaluation in the measurement of a physical quantity (see J.1);

example of calculation of systematic uncertainty in the determination of the specific hydraulic energy, mechanical runner/impeller power and hydraulic efficiency (see J.2);

example of calculation of systematic uncertainty in the determination of the net positive suction specific energy (see J.3).

Due to the various ways of determining the required quantities, it is not possible to specify in a standard a general statement for the relevant systematic errors. In the case of specific hydraulic energy, for example, the value of the systematic uncertainty depends on the instruments and the installation with the choice of instrumentation depending on the value of specific hydraulic energy. At lower values of specific hydraulic energy, greater values of uncertainty ( $f_E$ ) are generally to be expected. For the same reason, the relative systematic uncertainty in the determination of the net positive suction specific energy is generally higher in the systematic uncertainty in the determination of the specific hydraulic energy.

#### 1 Example of analysis of sources of error and of uncertainty evaluation in the measurement of a physical quantity<sup>1)</sup>

The following example illustrates how the various sources of error arising in the measurement of a quantity using an electronic device can be identified and how the corresponding uncertainties can be evaluated and combined. Table 8 is used as a guide for this analysis. All values given below are uncertainties at 95 % confidence level.

##### 1.1 Errors arising during calibration

###### 1.1.1 Component errors

Bias of the primary method: this is the systematic component of the intrinsic error of the primary method used for the calibration:  $\pm f_a$ .

If, for example, the quantity to be measured is the discharge and if the calibration is made using the weighing method, and if the secondary instrument is an electronic device, the main sources of systematic error of the primary method are due to the mechanical operation of the weighing machine, to its proper calibration, to the operation of the diverter, to the chronometer, to the buoyancy correction and to the determination of the density. If all the requirements of ISO 4185 are complied with, the bias of the weighing method can be estimated by combining the component systematic uncertainties of the different error sources.

b) Repeatability of the primary method: this is the random component of the intrinsic error of the primary method used for the calibration:  $\pm f_b$ .

In the example of item a) the main sources of random error of the primary method when using the weighing method are the scatter of the readings of the weighing machine (which may be evaluated from the scatter of the readings during the calibration of the weighing machine) and the repeatability of the motion of the diverter.

c) Bias of the secondary instrument: this is the systematic component of the intrinsic error of the secondary instrument:  $\pm f_c$ .

In the example of item a) it is due mainly to a systematic error in the measurement of the output signal from the electronic device.

d) Repeatability of the secondary instrument: this is the random component of the intrinsic error of the secondary instrument:  $\pm f_d$ .

In the example of item a) it is due mainly to the random error in the output signal measurement. It may be evaluated from the scatter of the points around the calibration curve.

e) Errors due to physical phenomena and influence quantities:  $\pm f_e$ .

In this category there may be various sources of error. With reference to the example of point a) are:

- the influence of the flow pattern on the response of the electronic device;
- the unsteadiness of the flow;
- the possible effect of physical properties of the water (conductivity, temperature, etc) on the response of the electronic device;
- the effect of external influence quantities (fluctuations of power supply, ambient temperature, electromagnetic field, etc).

The combination of all these errors can lead to an uncertainty in the indicated discharge which may be partly systematic and partly random in nature.

f) Errors in physical properties: these are the errors arising in the determination of physical quantities either by direct measurement or from international standardized data:  $\pm f_f$ .

In the example of item a), the main source of error of this type is the determination of the water density when the volume flowrate is deduced from the mass flowrate measured by weighing.

##### J.1.1.2 Resulting uncertainty in the calibration

All the errors listed above being small, numerous and independent of each other, the systematic and random corresponding uncertainties may be combined by the root-sum-square method (as explained in 3.9.1.4) to obtain the resulting relative uncertainty in the calibration curve:

$$f_{\text{cal}} = \pm \left[ (f_a)^2 + (f_b)^2 + (f_c)^2 + (f_d)^2 + (f_e)^2 + (f_f)^2 \right]^{1/2}$$

##### J.1.2 Errors arising during the tests

###### J.1.2.1 Component errors

g) Systematic error in the calibration:  $\pm f_{\text{cal}}$ .

Although the uncertainty determined in J.1.1.2 is partly systematic and partly random in nature, it becomes entirely systematic when the calibration previously determined is used for subsequent tests.

<sup>1)</sup> All the specific terms used in this annex are defined in "International vocabulary of basic and general terms in metrology" (VIM).

Additional systematic error: this is the systematic component of the intrinsic error of the secondary instrument, not covered by the calibration:  $\pm f_h$ .

Errors in physical properties:  $\pm f_j$ .

In certain cases, for example in the case of item J.1.1.1 a), this category of errors may be omitted.

Errors due to physical phenomena and influence quantities:  $\pm f_k$ .

The sources of error in this category are the same as those listed in J.1.1.1 e), but their values can be different and vary with the operating point. They may be neglected if the conditions occurring during the calibration are kept the same during the tests.

If not, it is assumed that they result in a systematic component  $\pm f_{ks}$  and a random component  $\pm f_{kr}$ .

Random error: this includes the repeatability of the secondary instrument  $\pm f_l$ .

This error can be measured during the tests. In the example of J.1.1.1 a), it occurs once again in a similar manner as it did during calibration.

## 2.2 Total uncertainty

Combining the component uncertainties by the root-sum-square method, the relative total uncertainty is obtained:

systematic uncertainty:

$$= \pm [(f_{cal})^2 + (f_h)^2 + (f_j)^2 + (f_{ks})^2]^{1/2}$$

random uncertainty:

$$= \pm [(f_{kr})^2 + (f_l)^2]^{1/2}$$

total uncertainty:

$$= \pm [(f_s)^2 + (f_r)^2]^{1/2}$$

## 2 Example of calculation of systematic uncertainty in the determination of the specific hydraulic energy, mechanical runner/impeller power and hydraulic efficiency

Assumed that the methods of measurement and their respective uncertainties<sup>1)</sup> are as follows:

**2.1 Discharge:** measurement by electromagnetic flowmeter. The systematic uncertainty is estimated equal to  $\pm 0,20$  %.

**2.2 Pressure:** at the high and low pressure measuring sections, measurement by dead-weight manometer.

**2.3 Specific hydraulic energy:** in this case it is given by (see figure 40):

$$E = \frac{p_{abs1} - p_{abs2}}{\rho} + g \cdot (z_1 - z_2) + \frac{v_1^2 - v_2^2}{2}$$

<sup>1)</sup> The systematic uncertainties depend on many factors, therefore the values assumed here are to be considered only as examples.

If, in a general way,  $e_x$  is the absolute systematic uncertainty in the quantity  $x$  (thus, the relative systematic uncertainty is  $f_x = \frac{e_x}{x}$ ) then the relative systematic uncertainty in the specific hydraulic energy is given by<sup>1)</sup>:

$$(f_E)_s = \pm \frac{(e_E)_s}{E} = \pm \left\{ \frac{\left[ (e_{pabs1}/\bar{p})^2 + (e_{pabs2}/\bar{p})^2 + (ge_{z1})^2 + (ge_{z2})^2 + \left( \frac{e_{v1}^2}{2} \right)^2 + \left( \frac{e_{v2}^2}{2} \right)^2 \right]^{1/2}}{\frac{p_{abs1} - p_{abs2}}{\bar{p}} + g \cdot (z_1 - z_2) + \frac{v_1^2 - v_2^2}{2}} + f_{\Delta E} \right\}$$

Assuming that:

$p_{abs1} = 10,5 \times 10^5$ Pa	$f_{pabs1} = \pm 0,1$ %
$p_{abs2} = 0,5 \times 10^5$ Pa	$f_{pabs2} = \pm 0,2$ %
$z_1 = 4$ m	$e_{z1} = \pm 0,01$ m
$z_2 = 2$ m	$e_{z2} = \pm 0,01$ m
$v_1 = 6$ m·s <sup>-1</sup>	$f_{v1} = \pm 0,2$ %
$v_2 = 1,5$ m·s <sup>-1</sup>	$f_{v2} = \pm 0,4$ %
$\bar{p} = 1000$ kg·m <sup>-3</sup>	
$g = 9,81$ m·s <sup>-2</sup>	

and supposing that the uncertainties in  $\bar{p}$  and  $g$  may be neglected and  $f_{\Delta E}$  is zero (see 3.5.3), then:

$$e_{pabs1}/\bar{p} = (p_{abs1}/\bar{p}) f_{pabs1} = \pm 10,5 \times (10^5/10^3) \times (0,1/100) = \pm 1,05 \quad \text{J·kg}^{-1}$$

$$e_{pabs2}/\bar{p} = (p_{abs2}/\bar{p}) f_{pabs2} = \pm 0,5 \times (10^5/10^3) \times (0,2/100) = \pm 0,1 \quad \text{J·kg}^{-1}$$

$$ge_{z1} = \pm 9,81 \times 0,01 = \pm 0,1 \quad \text{J·kg}^{-1}$$

$$ge_{z2} = \pm 9,81 \times 0,01 = \pm 0,1 \quad \text{J·kg}^{-1}$$

$$\frac{e_{v1}^2}{2} = v_1^2 f_{v1} = \pm 36 \times 0,2/100 = \pm 0,072 \quad \text{J·kg}^{-1}$$

$$\frac{e_{v2}^2}{2} = v_2^2 f_{v2} = \pm 2,25 \times 0,4/100 = \pm 0,009 \quad \text{J·kg}^{-1}$$

$$\text{and } (f_E)_s = \pm \frac{[(1,05)^2 + (0,1)^2 + (0,1)^2 + (0,1)^2 + (0,072)^2 + (0,009)^2]^{1/2}}{(1050 - 50) + 9,81 \times (4 - 2) + \frac{(36 - 2,25)}{2}} = \pm \frac{1,07}{1037} = \pm 0,1\%$$

In such a case, the relative systematic uncertainty in the specific hydraulic energy is practically equal to that of pressure measurements.

<sup>1)</sup> In fact, this formula is only an approximation,  $v_1^2$  and  $v_2^2$  are not independent quantities.

**2.4 Power:** torque measured by the primary method with a systematic uncertainty of 1,14 %, the rotational speed by an electronic counter with a systematic uncertainty of 1,075 %.

the power systematic uncertainty is estimated as:

$$(f_p)_s = \pm [(0,14)^2 + (0,075)^2]^{1/2} \% = \pm 0,16 \%$$

**2.5 Hydraulic efficiency:** by combining the systematic uncertainties of the measured quantities, the systematic uncertainty in the hydraulic efficiency is:

$$(f_{\eta_h})_s = \pm \frac{(e_{\eta_h})_s}{\eta_h} = \pm \left[ (f_Q)_s^2 + (f_E)_s^2 + (f_p)_s^2 \right]^{1/2} = \pm [(0,2)^2 + (0,1)^2 + (0,16)^2]^{1/2} \% = \pm 0,27 \%$$

### 3 Example of calculation of systematic uncertainty in the determination of the net positive suction specific energy

assume that the methods of measurement and their respective uncertainties<sup>1)</sup> are as follows:

**3.1. Discharge:** measurement by electromagnetic flowmeter. The systematic uncertainty is estimated equal to  $\pm 0,20 \%$ .

**3.2 Pressure:** at the low pressure measuring section measured by a dead-weight manometer.

**3.3 Net positive suction specific energy:** in this case it is given by (see figure 45):

$$NPSE = \frac{(p_{abs2} - p_{va})}{\rho_2} + \frac{v_2^2}{2} - g \cdot (z_r - z_2)$$

in a general way,  $e_x$  is the absolute systematic uncertainty in the quantity  $x$  (thus, the relative systematic uncertainty is  $f_x = e_x/x$ ) then the relative systematic uncertainty in the net positive suction specific energy is given by:

$$(f_{NPSE})_s = \pm \frac{(e_{NPSE})_s}{NPSE} = \pm \frac{\left[ \left( \frac{e_{pabs2}}{\rho_2} \right)^2 + \left( \frac{e_{pva}}{\rho_2} \right)^2 + \left( \frac{e_{v2}^2}{2} \right)^2 + (ge_{zr})^2 + (ge_{z2})^2 \right]^{1/2}}{\frac{(p_{abs2} - p_{va})}{\rho_2} + \frac{v_2^2}{2} - g \cdot (z_r - z_2)}$$

Assuming that:

$p_{abs2} = 0,2 \times 10^5$	Pa	$f_{pabs2} = \pm 0,3 \%$
$z_r = 2$	m	$e_{zr} = \pm 0,01$ m
$z_2 = 1$	m	$e_{z2} = \pm 0,01$ m
$v_2 = 1,5$	$m \cdot s^{-1}$	$f_{v2} = \pm 0,4 \%$
$\rho_2 = 1\,000$	$kg \cdot m^{-3}$	
$p_{va} = 0,03 \times 10^5$	Pa	
$g = 9,81$	$m \cdot s^{-2}$	

and the uncertainties in  $\rho_2$ ,  $p_{va}$  and  $g$  may be neglected, then:

$$\frac{e_{pabs2}}{\rho_2} = \frac{p_{abs2}}{\rho_2} \times f_{pabs2} = \pm 0,2 \times (10^5 / 10^3) (0,3 / 100) = \pm 0,06 \quad J \cdot kg^{-1}$$

$$ge_{zr} = \pm 9,81 \times 0,01 = \pm 0,1 \quad J \cdot kg^{-1}$$

$$ge_{z2} = \pm 9,81 \times 0,01 = \pm 0,1 \quad J \cdot kg^{-1}$$

$$\frac{e_{v2}^2}{2} = \pm v_2^2 \cdot f_{v2} = \pm 2,25 \times 0,4 / 100 = \pm 0,009 \quad J \cdot kg^{-1}$$

$$(f_{NPSE})_s = \pm \frac{[(0,06)^2 + (0,1)^2 + (0,1)^2 + (0,009)^2]^{1/2}}{(20-3) + \frac{2,25}{2} - 9,81 \times (2-1)} = \pm \frac{0,1539}{8,315} = \pm 1,85 \%$$

<sup>1)</sup> The systematic uncertainties depend on many factors, therefore the values assumed here are to be considered only as examples.

## Annex K (normative)

### Efficiency scale-up for Pelton turbines

This annex, based on theoretical considerations and experimental data, summarizes the best approximation available at the present time. Research work currently in progress may lead to a more precise knowledge of the efficiency scale-up for Pelton turbines. Until these new results are available, it is good practice to apply the scale-up formula given in K.2 for transposition from a model to the prototype.

#### 1 Similarity considerations

It can be shown by dimensional analysis (see appendix A to reference K.4.1), the losses in Pelton machines are controlled by five dimensionless parameters:

- the Reynolds number  $Re$  (see 1.3.3.11.1);
- the Froude number  $Fr$  (see 1.3.3.11.2);
- the Weber number  $We$  (see 1.3.3.11.3);
- the speed factor  $n_{ED}$  (see 1.3.3.12.1) or energy coefficient  $E_{nD}$  (see 1.3.3.12.5);
- the specific flow rate  $\Phi_B$  defined as follows:

$$\Phi_B = \frac{4Q}{z_0 \cdot \pi \cdot (2E)^{1/2} \cdot B^2}$$

where

- $[m^3 \cdot s^{-1}]$  is the discharge (see 1.3.3.4.1);
- $[-]$  is the number of nozzles;
- $[J \cdot kg^{-1}]$  is the specific hydraulic energy of machine (see 1.3.3.6.1);
- $[m]$  is the bucket width (see 1.3.3.2.8).

Referring to 2.3.1.1, the following characteristic values are used to define the above dimensionless numbers:

$(2E)^{1/2}$  as characteristic velocity  $v_C$ ;

bucket width  $B$  as characteristic length  $L_C$ .

For two geometrically similar Pelton turbines (e.g. a prototype machine and a corresponding model machine), the following ratios of similitude numbers can be made:

$$C_{Fr} = \frac{Fr_P}{Fr_M} = \left( \frac{E_P}{E_M} \right)^{1/2} \cdot \left( \frac{B_M}{B_P} \right)^{1/2} \cdot \left( \frac{g_M}{g_P} \right)^{1/2}$$

$$C_{We} = \frac{We_P}{We_M} = \left( \frac{E_P}{E_M} \right)^{1/2} \cdot \left( \frac{B_P}{B_M} \right)^{1/2} \cdot \left( \frac{\rho_P}{\rho_M} \right)^{1/2} \cdot \left( \frac{\sigma_M^*}{\sigma_P^*} \right)^{1/2}$$

$$C_{Re} = \frac{Re_P}{Re_M} = \left( \frac{E_P}{E_M} \right)^{1/2} \cdot \frac{B_P}{B_M} \cdot \frac{v_M}{v_P}$$

These ratios are used to define functions which describe the efficiency scaling effects between two geometrically similar Pelton turbines when operating at the same speed factor  $n_{ED}$  or energy coefficient  $E_{nD}$ , with the specific flow rate  $\Phi_B$  being the most important parameter for  $C_{Re}$ ,  $C_{Fr}$  and  $C_{We}$ . The functions result from the analysis of numerous results of efficiency tests performed with the same model at different test conditions and from comparison of measured efficiencies of prototype and model turbines being fully or partly homologous.

The resulting differences in hydraulic efficiency  $\Delta\eta_h$  are presented in figure K.1 for the influence of Froude number, in figure K.2 for the influence of Weber number and in figure K.3 for the influence of Reynolds number.

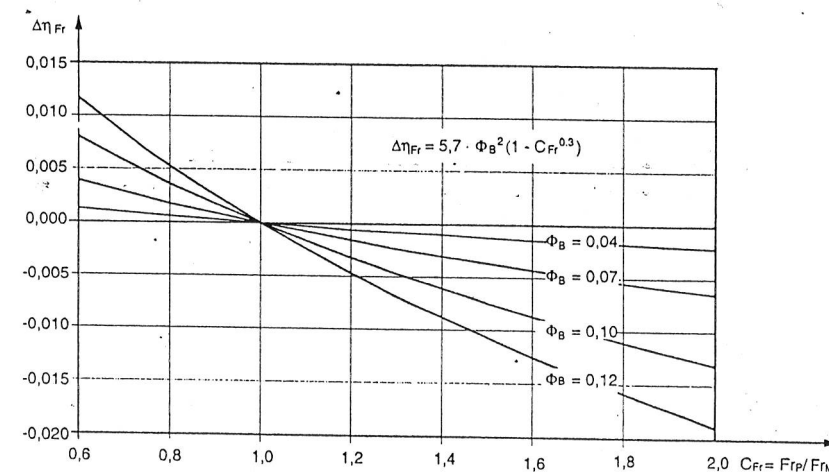


Figure K.1 – Influence of Froude number

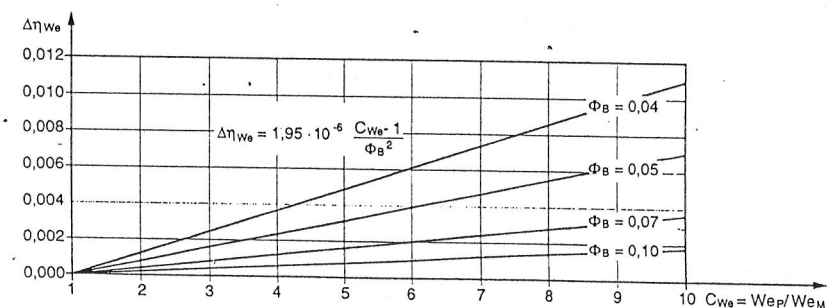


Figure K.2 – Influence of Weber number

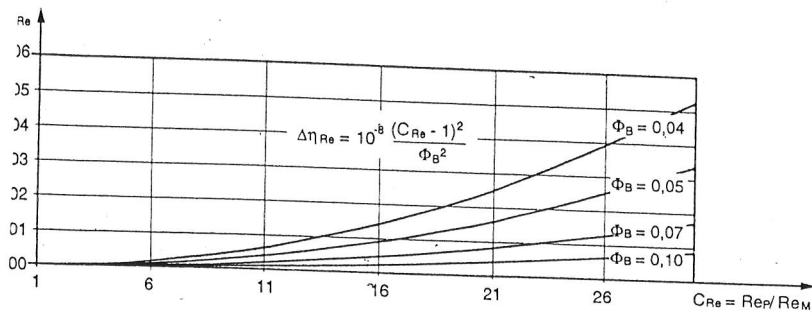


Figure K.3 – Influence of Reynolds number

## 2 Step-up procedure

he guarantees are referred to prototype, the model hydraulic efficiencies  $\eta_{hM}$  are scaled up to prototype conditions using the following formula:

$$\Delta\eta_h = \eta_{hP} - \eta_{hM} = \Delta\eta_{Fr} + \Delta\eta_{We} + \Delta\eta_{Re}$$

$$\Delta\eta_h = \eta_{hP} - \eta_{hM} = 5,7 \cdot \Phi_B^2 (1 - C_{Fr}^{0,3}) + 1,95 \cdot 10^{-6} \frac{C_{We} - 1}{\Phi_B^2} + 10^{-8} \frac{(C_{Re} - 1)^2}{\Phi_B^2}$$

## 3 Numerical data for surface tension $\sigma^*$

Temperature $\theta$ °C	Surface tension $\sigma^*$ J·m <sup>-2</sup>
5	0,0749
10	0,0742
15	0,0735
20	0,0728
25	0,0720
30	0,0712
35	0,0696

## 4 Bibliography

- 4.1 Grein, H., Meier, J., Klicov, D., "Efficiency scale effects in Pelton turbines", *Proceedings*, Vol. II, IAHR Symposium, Montreal, Canada, 1986, paper No. 76.
- 4.2 Grein, H., Klicov, D., Wieser, W., "Efficiency scale effects in Pelton turbines". *Water Power & Dam Construction*, May 1988, p. 32.
- 4.3 *Handbook of chemistry and physics*, editor Robert C. West, 58th edition 1977-78, CRC Press Inc., Cleveland, Ohio.

## Annex L (normative)

### Analysis of random uncertainties for a test at constant operating conditions<sup>1)</sup>

Repeated measurements at one operating point may be expected to show differences in measurements but their mean value is a better estimate of the true value than any individual measurement. The accuracy of the mean-value depends on the number of measurements and their individual deviations from the mean (scatter).

It is possible to calculate statistically the uncertainty in a measurement of a variable when the associated error is purely random in nature. To do this it is necessary to calculate the standard deviation and to decide on the confidence level which is to be attached to the uncertainty. For this standard, a 95 % confidence level shall be used.

#### L.1 Standard deviation

The exact value of standard deviation  $\sigma$  of any measured parameter is rarely known exactly; usually only an estimate  $s$  of  $\sigma$  is available, based on a limited number of observations.

If the error in the measurement of a quantity  $Y$  is purely random, then, when  $n$  independent measurements of the quantity are made, the standard deviation<sup>2)</sup> of the distribution of results  $s_Y$  is given by the equation:

$$s_Y = \left[ \frac{\sum_{r=1}^n (Y_r - \bar{Y})^2}{n-1} \right]^{1/2}$$

where

$\bar{Y}$  is the arithmetic mean of the  $n$  measurements of the variable  $Y$ ;

$Y_r$  is the value obtained by the  $r$ th measurement of the variable  $Y$ ;

$n$  is the total number of measurements of the variable  $Y$ .

For brevity,  $s_Y$  is normally referred to as "the standard deviation of  $Y$ ". The square of the standard deviation  $s_Y^2$ , is called the variance.

The random error in the result can be reduced by making as many measurements as possible of the variable and using the arithmetic mean value, since the standard deviation of the mean of  $n$  independent measurements is  $\sqrt{n}$  times smaller than the standard deviation of the measurements themselves.

Thus, the standard deviation of the mean,  $s_{\bar{Y}}$  is given by the equation:

$$s_{\bar{Y}} = \frac{s_Y}{\sqrt{n}}$$

<sup>1)</sup> The text of this annex is based on ISO 5168.

<sup>2)</sup> Standard deviation, as defined here, is what is more accurately referred to as the "estimated standard deviation" by statisticians.

## 2 Confidence levels

the true standard deviation  $\sigma_Y$ , is known (as  $n$  approaches infinity,  $s_Y$  approaches  $\sigma_Y$ ), the confidence level can be related to the uncertainty of measurements as indicated in table L.1.

Table L.1 – Confidence levels

Uncertainty	Confidence level
$\pm 0,674 \cdot \sigma_Y$	0,50
$\pm 0,954 \cdot \sigma_Y$	0,66
$\pm 1,960 \cdot \sigma_Y$	0,95
$\pm 2,576 \cdot \sigma_Y$	0,99

For example, the interval  $Y_r \pm 1,96 \cdot \sigma_Y$  would be expected to contain 95 % of the population. That is to say, where a single measurement of the variable  $Y$  is made and where the value of  $\sigma_Y$  is independently known, there would be a probability of 0,05 of the interval  $Y_r \pm 1,96 \cdot \sigma_Y$  not including the true value.

In practice, of course, it is only possible to obtain an estimate of the standard deviation since an infinite number of measurements would be required in order to determine it precisely, and the confidence limits must be based on this estimate. The Student's "t distribution" for small samples should be used to relate the required confidence level to the interval.

## 3 Student's t distribution

The uncertainty at 95 % confidence level may be found as follows:

- if  $n$  is the number of measurements,  $(n-1)$  is taken as the number of degrees of freedom,  $v$ ;
- the value of  $t$  for the appropriate number of degrees of freedom is read in the table L.2;
- the standard deviation  $s_Y$  of the distribution of the measurements of the quantity  $Y$  is calculated as stated in clause L.1;
- the range of values within which any reading would be expected to be with 95 % confidence is

$$\bar{Y} \pm t \cdot s_Y;$$

- the difference between a new reading and the average of the sample should be less than

$$t \cdot s_Y \cdot \sqrt{1 + 1/n};$$

the range of values within which the true value of the quantity would be expected to lie with 95 % confidence, i.e. the band of uncertainty, is

$$\bar{Y} \pm \frac{t \cdot s_Y}{\sqrt{n}} = \bar{Y} \pm t \cdot s_{\bar{Y}}$$

Table L.2 – Values of Student's t

Degrees of freedom	Student's t	$\frac{t}{\sqrt{n}}$
$v = n - 1$	For 95 % confidence level	
1	12,706	8,984
2	4,303	2,484
3	3,182	1,591
4	2,776	1,241
5	2,571	1,050
6	2,447	0,925
7	2,365	0,836
8	2,306	0,769
9	2,262	0,715
10	2,228	0,672
11	2,201	0,635
12	2,179	0,604
13	2,160	0,577
14	2,145	0,554
15	2,131	0,533
20	2,086	0,455
30	2,042	0,367
60	2,000	0,256
$\infty$	1,960	0

For other values of  $v$ ,  $t$  can be computed from the following empirical equation:

$$t = 1,96 + 2,36/v + 3,2/v^2 + 5,2/v^{3,84}$$

## L.4 Maximum permissible value of random uncertainty

If the required range of accepted random uncertainty associated with  $\bar{Y}$  is  $\pm e_{r, \max}$ , then

$$e_r = \frac{t \cdot s_Y}{\sqrt{n}}$$

should not exceed  $e_{r, \max}$ .

Alternatively, for a value of  $e_{r, \max}$  associated with the 95 % confidence level, the estimated standard deviation  $s_Y$  should not exceed the value of

$$s_{Y, \max} = \frac{e_{r, \max} \cdot \sqrt{n}}{t}$$

For convenience, values of  $\frac{t}{\sqrt{n}}$  are given in table L.2.

The mean value of a series of points which meet the above criteria will be acceptable. Table 1 applies only to repeated points at constant operating conditions.

## 5 Example of calculation

The following example illustrates the computation of the estimated standard deviation and the certainty for  $n = 8$  observations of a quantity  $Y$ .

Table L.3

Measured values		
$Y_i$	$\bar{Y} - Y_i$	$(\bar{Y} - Y_i)^2$
92,80	-0,15625	0,024414
92,70	-0,05625	0,003164
92,60	+0,04375	0,0019141
92,50	+0,14375	0,0206641
92,70	-0,05625	0,0031641
92,75	-0,10625	0,0112891
92,50	+0,014375	0,00206641
92,60	+0,04375	0,0019141

$$\bar{Y} = \frac{1}{n} \sum_{i=1}^n Y_i = 92,64375$$

$$\sum_{i=1}^n (\bar{Y} - Y_i)^2 = 0,0871876$$

estimated standard deviation of the observations:

$$s_Y = \sqrt{\frac{\sum (\bar{Y} - Y_i)^2}{n-1}} = \sqrt{\frac{0,0871876}{8-1}} = 0,111604$$

random uncertainty associated with the mean value at the 95 % confidence level:

$$(e_Y)_r = \pm \frac{t \cdot s_Y}{\sqrt{n}} = \pm 0,111604 \times 0,836 = \pm 0,0933$$

$$(f_Y)_{r95} = \frac{(e_Y)_r}{\bar{Y}} = \pm \frac{0,0933}{92,6437} = \pm 0,1\%$$

In the case of the examined measure being the efficiency, it should then be verified that this value of the observed random uncertainty  $(f_{\eta})_t$  does not exceed the maximum permissible random uncertainty agreed prior to the test (see 3.9.2.2.1).

## Annex M

(normative)

### Calculation of plant Thoma number $\sigma_{pl}$

### M.1 Definition of $\sigma_{pl}$ , NPSE and NPSH

These terms are referred to the low pressure side of the machine and are in direct relation with the cavitation phenomenon. The symbol  $\sigma_{pl}$  denotes the range of the Thoma number (see 1.3.3.12.9) occurring at plant conditions and is defined as follows:

$$\sigma_{pl} = \frac{NPSE}{E} = \frac{NPSH}{H}$$

Subclause 11.3 of IEC 60041 explains various possibilities for calculating NPSE of a prototype machine, as illustrated and explained below. If the pressure  $p_{ab2}$  (see figure M.1) at point 2 inside the draft tube is known, NPSE can be calculated in case of a turbine or a pump according to the following formula:

$$NPSE = g_2 \cdot NPSH = \frac{p_{abs2} - p_{va}}{\rho_2} + \frac{v_2^2}{2} - g_2 \cdot (z_1 - z_2)$$

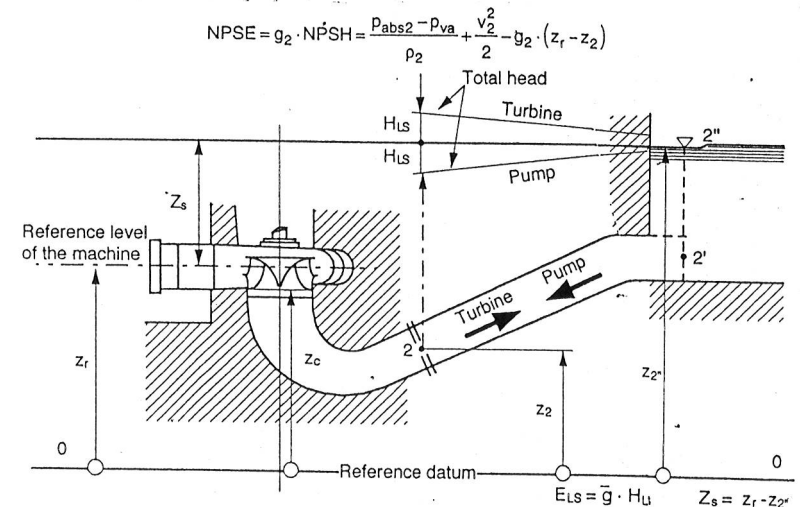


Figure M.1 – Definition for determination of net positive suction energy, NPSE, and net positive suction head, NPSH, of a prototype machine ( $E_{L1} \neq 0$ )

usually only the tailwater level for specified hydraulic conditions is known. In that case, NPSE calculated according to the following formula using the tailwater level  $z_2$  close to the draft tube outlet (turbine) or inlet (pump) and considering the specific hydraulic energy losses  $E_{LS}$  between sections 2 and 2':

$$NPSE = g_2 \cdot NPSH = \frac{p_{amb2} - p_{va}}{\rho_2} + \frac{v_2^2}{2} - g_2 (z_r - z_2) \pm E_{LS}$$

$$NPSE = g_2 \cdot NPSH = \frac{p_{amb2} - p_{va}}{\rho_2} + \frac{v_2^2}{2} - g_2 \cdot z_s \pm E_{LS}$$

(+ for turbines, - for pumps)

$\sigma_{pl}$  is usually referred to the reference level of the machine  $z_r$  (see 1.3.3.7.6). As recommended 2.3.1.5.1 the cavitation reference level  $z_c$  shall be chosen corresponding to the location where the relevant cavitation occurs. Consequently,  $\sigma_{pl}$  shall also be referred to  $z_c$ , and the corresponding definition is identified as  $\sigma_{plc}$ :

$$\sigma_{plc} = \frac{NPSE - g_2(z_c - z_r)}{E}$$

$$\sigma_{plc} = \frac{\frac{p_{amb2} - p_{va}}{\rho_2} + \frac{v_2^2}{2} - g_2(z_c - z_2) \pm E_{LS}}{E}$$

When section 2' and the corresponding tailwater level 2\* are far from the draft tube opening, and it can be assumed  $v_{2'} \approx 0$  the formula changes to:

$$\sigma_{plc} = \frac{\frac{p_{amb2} - p_{va}}{\rho_2} - g_2(z_c - z_{2*}) \pm E_{LS}}{E}$$

## 1.2 Data needed to calculate $\sigma_{plc}$

As stipulated in 1.4.1.1, most of the following site data shall be provided or specified by the purchaser:

### a) Constant plant data

The following data are usually assumed as constant data, i.e. they do not depend on operating conditions.

#### - Ambient pressure $p_{amb}$

If not specified,  $p_{amb}$  is taken from table B.6 as a function of the tailwater level  $z_2$  (average value).

#### - Water temperature $\theta_w$ , $\theta_{wmax}$

The average value  $\theta_w$  and the maximum value  $\theta_{wmax}$  shall be specified. The value  $\theta_w$  is to be used for calculation of  $E$ ,  $P_n$  and  $\eta_{hM}$ , whereas  $\theta_{wmax}$  shall be used to get the lowest possible value of  $\sigma_{plc}$ .

#### - Vapour pressure $p_{va}$

The value  $p_{va}$  is taken from table B.4 as a function of water temperature  $\theta_w$ . To determine the minimum value of  $\sigma_{plc}$ , it is necessary to use the value  $\theta_{wmax}$ .

#### - Draft tube cross section $A_2$ or measuring section $A_2'$

To calculate the mean flow velocity  $v_2$  or  $v_{2'}$ , it is to be agreed on which cross-section area shall be used (except if it is assumed that  $v_{2'} = 0$ ).

#### - Density of water $\rho_2$

This value is to be taken from table B.2 as a function of  $\theta_w$  or  $\theta_{wmax}$  (negligible impact on resulting  $\sigma_{plc}$ ).

#### - Reference level $z_r$

The reference level  $z_r$  is defined by figure 5 which corresponds to figure 8 in IEC 60041. This value is usually specified on the main section drawing and/or in the technical specification.

#### - Cavitation reference level $z_c$

The level  $z_c$  shall be defined by mutual agreement. For example, for large tubular turbines with horizontal shaft, more than one level  $z_c$  may be agreed on.

### b) Variable plant data

The following data usually depend on the operating conditions of the machine.

#### - Tailwater level $z_2$

The variation of  $z_2$  is usually specified as a function of the specific hydraulic energy  $E$ .

#### - Specific hydraulic energy $E$

The range and the relevant values of  $E$  shall be given in the technical specification. Sometimes only the headwater and tailwater levels and the resulting values of geodesic height (gross head) are given. In this case  $E$  shall be calculated by considering the relevant energy losses  $E_{LS}$  on the high and low pressure sides of the machine.

#### - Mean velocity $v_2$ or $v_{2'}$

$v_2$  or  $v_{2'}$  are calculated using the agreed relevant draft tube cross-section area  $A_2$  or  $A_{2'}$  and the discharge  $Q$  for each specified operating point where cavitation tests are to be performed.

#### - Specific hydraulic energy losses $E_{LS}$

In case such losses are to be considered, they are usually specified and depend on discharge, i.e. on  $Q^2$ .

In view of cavitation tests, it is recommended to summarize in a separate document the relevant data for calculation of the various  $\sigma_{plc}$  values. It is also helpful to add a schematic drawing similar to figure M.1. The following table M.1 illustrates as an example how the resulting  $\sigma_{plc}$  values and other relevant data can be summarized.

Table M.1 – Summary of calculated  $\sigma_{pl}$  values and other relevant data

E (J/kg)	z <sub>2</sub> (m)		Q (m <sup>3</sup> /s)		v <sub>2</sub> (m/s)		E <sub>LS</sub> (J/kg)		$\sigma_{plc}$ (-)	
	max.	min.	max.	min.	max.	min.	max.	min.	max.	min.
Maximum Specified										
---										
Minimum										

Annex N  
(informative)

Detailed flux diagram of specific hydraulic energy, flow and power

As a supplement to figure 6, a more detailed analysis of internal losses in the runner/impeller of a reaction machine is presented in figures N.1 and N.2. According to recent publications, this analysis is needed to determine the scale effect on efficiency and power and also on specific hydraulic energy.

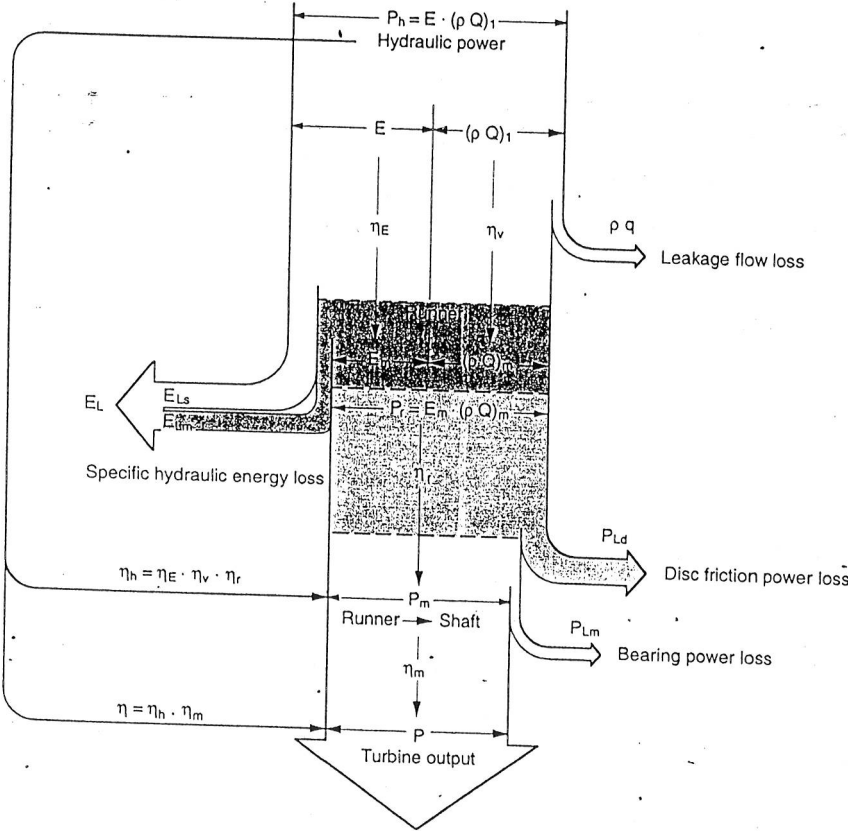


Figure N.1 – Turbine

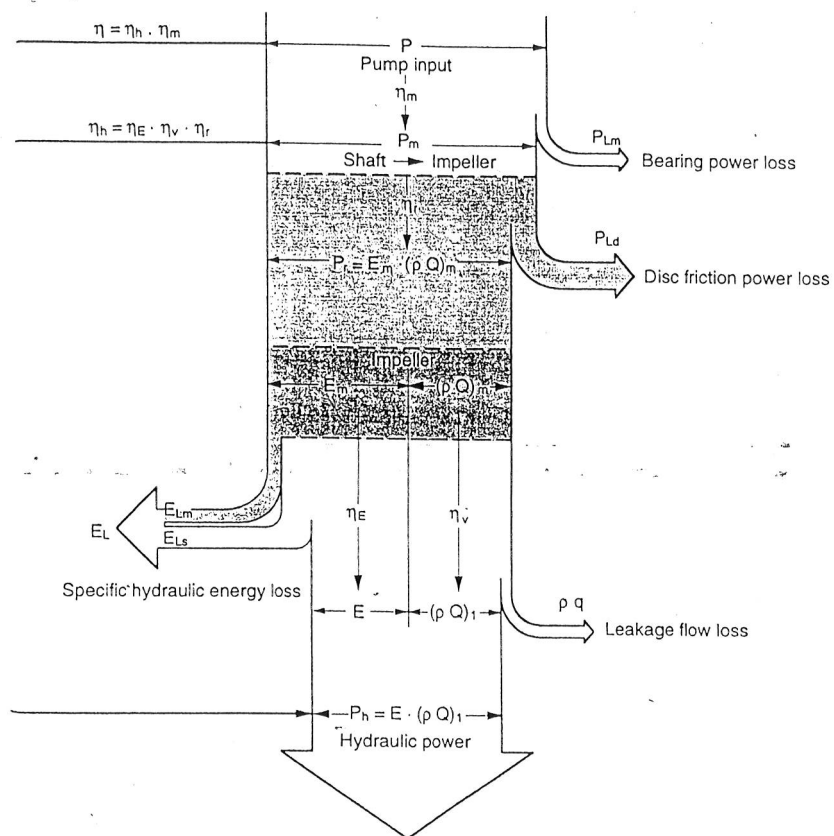


Figure N.2 – Pump

The following quantities:  $P$ ,  $P_h$ ,  $P_m$ ,  $P_{Lm}$ ,  $Q$ ,  $q$ ,  $E$ ,  $E_L$ ,  $p$ ,  $\eta$ ,  $\eta_h$ ,  $\eta_m$  and  $\eta_v$  are defined in 1.3. Other quantities are defined below:

- $P_r$  is the hydraulic power transmitted from water to the runner (turbine) or from impeller to water (pump);
- $P_{Ld}$  is the hydraulic power dissipated in the chambers between the outer surface of runner/impeller and the corresponding stationary walls;
- $E_m$  is the specific hydraulic energy available for runner to produce power (turbine) or imparted to the water by impeller (pump);
- $Q_m$  is the volume of water per unit time passing through runner/impeller blades;
- $E_{Lm}$  is the specific hydraulic energy loss in runner/impeller blades;
- $E_{Ls}$  is the specific hydraulic energy loss in stationary parts;
- $E_L$  is the specific hydraulic energy loss between high (low) pressure section and low (high) pressure section of turbine (pump);
- $\eta_E$  is the specific energy efficiency of runner/impeller given by the ratio of  $E_m/E$  (turbine) or by the ratio of  $E/E_m$  (pump);
- $\eta_r$  is the power efficiency of runner/impeller given by the ratio of  $P_m/P_r$  (turbine) or  $P_r/P_m$  (pump).

**Annex P**  
(informative)

**Bibliography**

- [1] Gindroz, B., *Lois de similitude dans les essais de cavitation des turbines Francis*. Thesis published in June 1991 by Ecole Polytechnique Fédérale, Institut de Machines Hydrauliques et de Mécanique des Fluides, Lausanne (Switzerland).
- [2] Osterwalder, J., Hippe, L., "Guidelines for efficiency scaling process of hydraulic turbomachines with different technical roughnesses of flow passages". *Journal of hydraulic research*, Vol. 11, 1984.
- [3] Gindroz, B., Henry, P., Avellan, F., "Similarity of cavitation inception in Francis turbines". *Proceedings* (Vol. 1) from 15th Symposium IAHR (Internal Association for Hydraulic Research), Belgrade, Sept. 1990.
- [4] Herbst, G., Roegener, H., "Neue kanonische Zustandsgleichung des Wassers", *Fortschritt-Berichte VDI-Z*, Reihe 6, Nr. 50 (1977).
- [5] Kell, G.S., Whalley, E., "Re-analysis of the density of liquid water in the range 0 to 150 °C and 0 to 1 kbar. Communication à la 8e Int. Conf. Prop. Steam, Giens, (1974).
- [6] Kell, G.S., McLaurin, G.E., Whalley, E., "The PVT properties of liquid water in the range of 150 to 350 °C and 0 to 1 kbar", Communication à la 8e Int. Conf. Prop. Steam, Giens, (1974).
- [7] Borel, L., Nguyen Dinh Lan., "Equations of state and Joule Thomson coefficient", 10th Int. Conf. Prop. Steam, Moscow (1984).
- [8] Haar, L., Gallagher, J.S., Kell, G.S., *NBS/NRC steam tables: thermodynamic and transport properties, and computer programs for vapor and liquid states of water in SI units*, Hemisphere Publ. Corp. (1984).
- [9] Weber, P., "Bemerkungen zur thermodynamischen Methode der Wirkungsgradbestimmung von Wasserturbinen und Speicherpumpen". *Bulletin des Schweiz. El. techn. Vereins* BD. 55, (1964), No. 24, pp. 1199-1208.
- [10] *Dissolved oxygen analyzer*, Beckman Instruments, Inc., Fullerton, CA 92634.
- [11] Van Slyke, D.D., Neil, J.M., "The determination of gases in blood and other solutions by vacuum extraction and measurement", *Journal of Biological Chemistry*, Vol. 2, Sept 1924.
- [12] Mohammed, W.A., Hutton S.P., "Improved monitoring of air in water", *Water Power & Dam Construction*, Sept. 1986, p. 48.
- [13] Brand, F.L., "A physical process for the determination of dissolved and un-dissolved gases in water", *Voith Research and Construction*, Vol. 27e (1980), Paper 7.
- [14] Kestin, J., Whitelaw, J.H., Sixth International Conference on the Properties of Steam-Transport Properties of Water Substance.
- [15] *VDI-Wärmeatlas*, VDI Verlag Düsseldorf 1984.
- [16] Landolt, Börnstein, "Zahlenwerte und Funktionen", Vol. IV, Technik, Part 1 und Physikalisch-Technische Bundesanstalt, Germany, 1953.
- [17] Kubota, T., Tsukamoto, T., "Calculation of prototype cavitation characteristics in large bulb turbines", *Water Power & Dam Construction*, September 1988.
- [18] JSME Standard S008, "Performance Conversion Method for Hydraulic Turbines and Pump-Turbines", The Japan Society of Mechanical Engineers, January 1999.
- [19] Kubota, T., Tsukamoto, T., "Scale effect on cavitation runaway speed of large bulb turbine for low head", presented at IAHR Symposium 1990.
- [20] Grubbs, F.E., "Procedures for detecting outlying observations in samples" *Technometrics*, Vol. 12, n.1, February 1969, pp 1-21.

The references listed below provide additional information on the topics covered by subclauses 4.2 and 4.3.

- [21] Bendat J., Piersol A. G., "Random data: analysis and measurements procedures". New York, John Wiley, (1986).
- [22] Fanelli M., "Research on off-design behaviour of Francis turbines: an overview of present state, difficulties, open problems, needs and strategies". IAHR WG, Milan (1991).
- [23] Hewlett Packard, "The fundamentals of signal analysis", HP application note 243 (1985)
- [24] Jacob T., "Evaluation sur modèle réduit et prédiction de la stabilité de fonctionnement des turbines Francis". Thesis No 1146, EPFL, Lausanne (1993).
- [25] Jacob T., Prénat J.E., "Francis turbine surge: Discussion and data base". XVIII IAHR Symposium, Valencia (1996)
- [26] Ouaked R., "Etude des phénomènes propagatifs en conduite dans un circuit hydraulique: intensimétrie hydroacoustique". Thesis 400, USTL Flandres-Artois (1989).
- [27] Doerfler P. A., "'Cross impedance' method for frequency-domain representation of oscillations in power plants with meshed waterways". BHRA Pressure Surges, Hannover (1986).
- [28] Jacob T., Prénat J.E., "Generation of hydroacoustic disturbances by a Francis turbine model and dynamic behavior analysis", IAHR Symposium, Belgrade (1990).

Customer Service Centre (CSC)  
International Electrotechnical Commission  
3, rue de Varembe  
1211 · GENEVA 20  
Switzerland